

## *Techniques expérimentales pour les métamatériaux acoustiques*

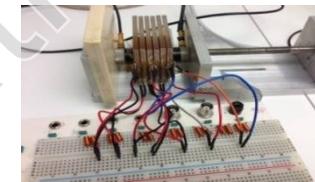
**Bruno Morvan,**  
LOMC, UMR 6294 CNRS  
Le Havre, France  
[Bruno.morvan@univ-lehavre.fr](mailto:Bruno.morvan@univ-lehavre.fr)



# Course outlines

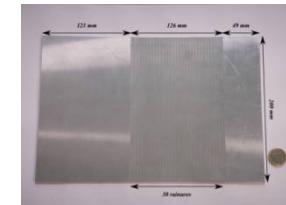
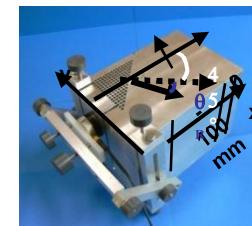
## PART 1 : Observation and characterisation of forbidden bands in a PC. Experimental Band structure determination

- 1D Phononic Crystal made of a stack of rectangular plates. Particular case of piezoelectric plates
- 2D square array of steel cylinders embedded in an epoxy matrix.



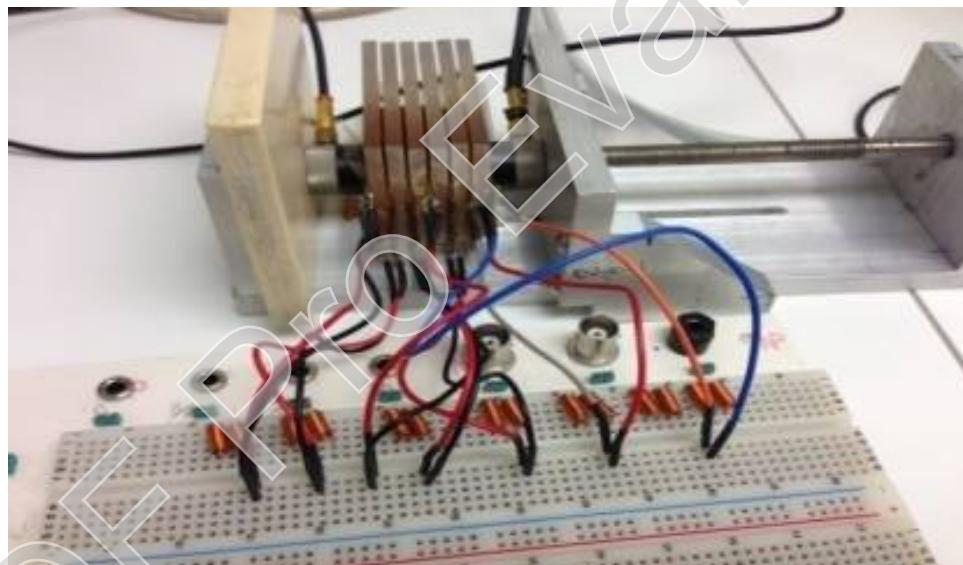
## PART 2 : Experimental demonstration of the negative refraction in a solid PC. Waves with opposite group and phase velocities

- Negative refraction in a solid phononic crystal
- Lamb waves in a plate with periodic corrugation



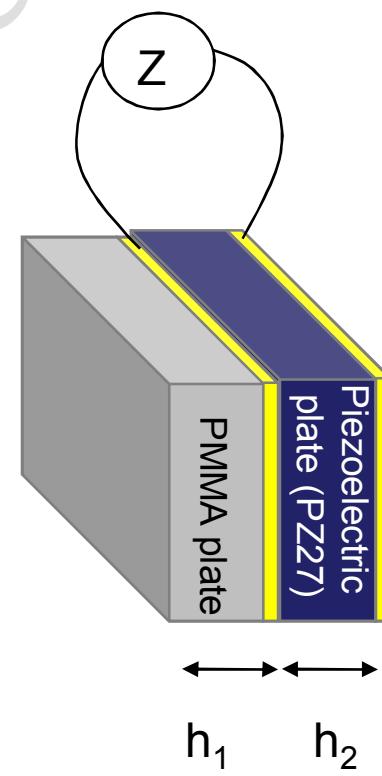
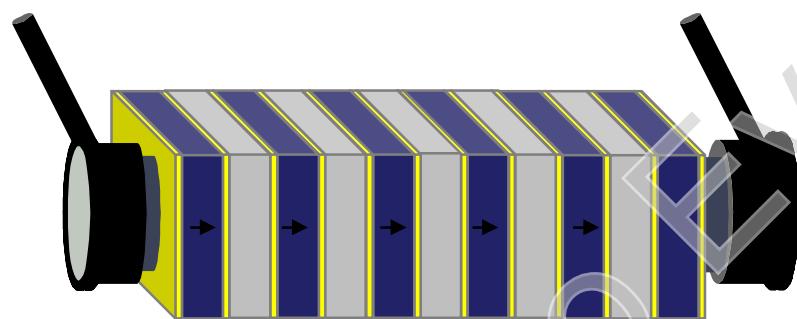
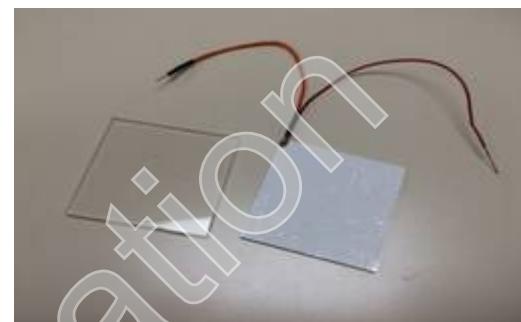
**PART 1 : Observation and characterisation of forbidden bands in a PC.  
Experimental Band structure determination**

1D Phononic Crystal made of a stack of rectangular plates. Particular case of piezoelectric plates



## Propagation through a stack of plates

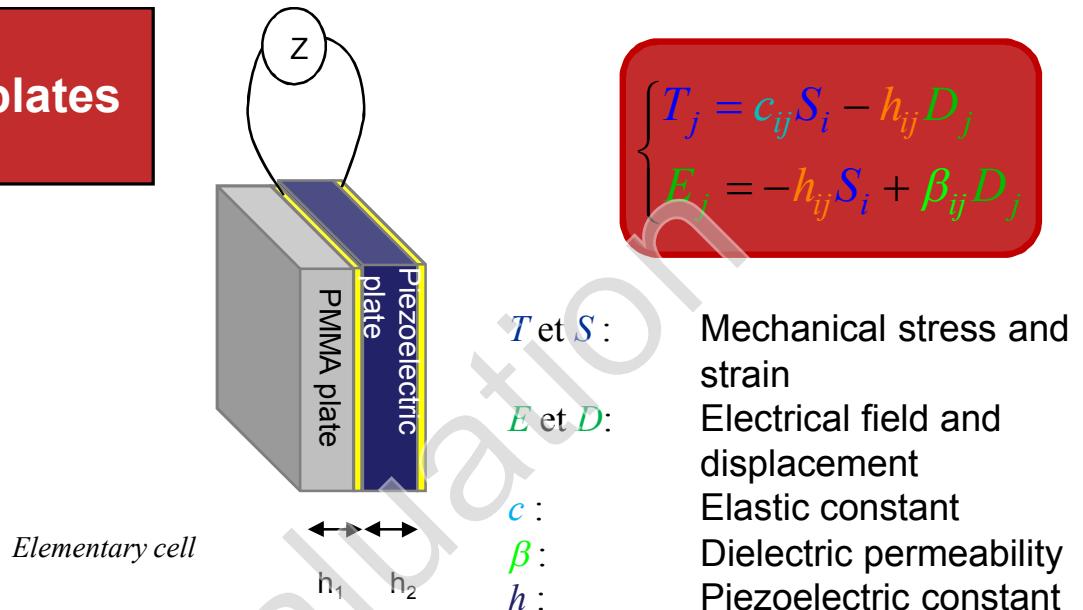
1D phononic crystal composed of alternating piezoelectric and PMMA plates



*Elementary cell*

## Propagation through a stack of plates

The dispersion relation is obtained by using the **Bloch-Floquet** relation and the piezoelectric constitutive equations



$$\cos k(h_1 + h_2) = \frac{\cos(k_1 h_1) \cos(k_2 h_2) - \frac{1}{2} \left( \gamma + \frac{1}{\gamma} \right) \sin(k_1 h_1) \sin(k_2 h_2) + \frac{\alpha}{\gamma} \left( \sin(k_1 h_1) (1 - \cos(k_2 h_2)) - \gamma \cos(k_1 h_1) \sin(k_2 h_2) \right)}{1 - \alpha \sin(k_2 h_2)}.$$

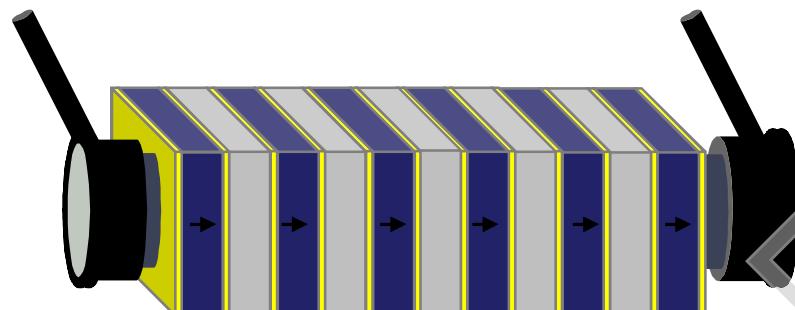
(Thèse de Sébastien Degraeve, 2013 (IEMN, Lille))

In this relation,  $\alpha = \frac{h_{33}^2}{C_{33}^D (\beta_{33}^S + j\omega Z)}$ . includes the electric boundary conditions.

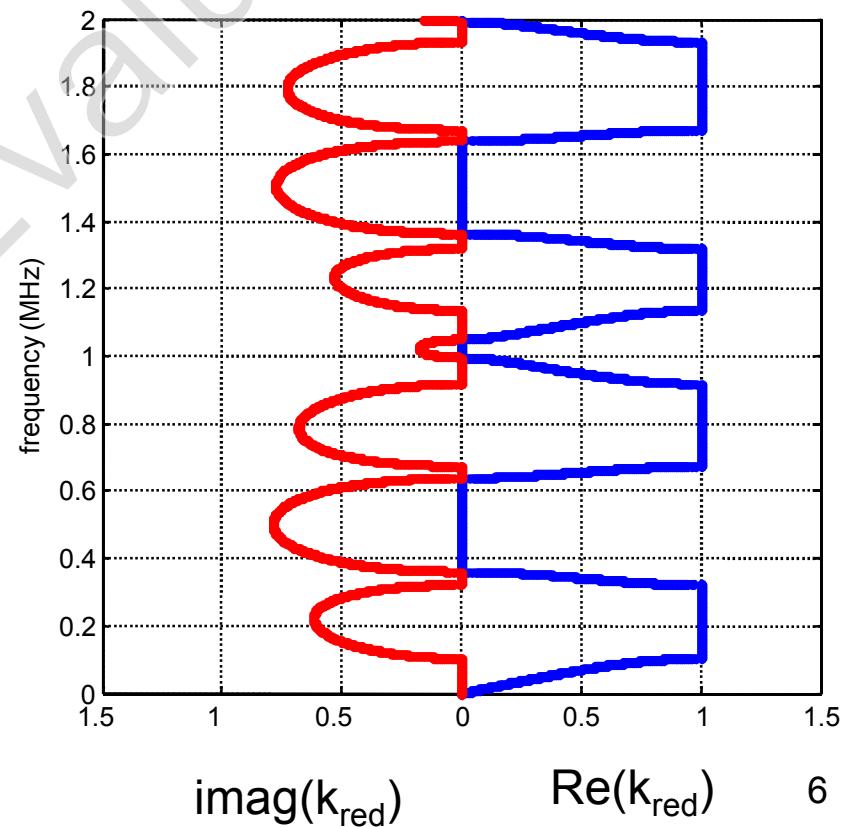
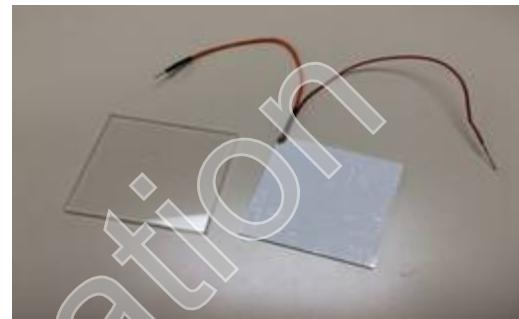
Depending on the electrical impedance charges  $Z$  connected on the piezoelectric plates, the band structure can be modified.

## Propagation through a stack of plates

1D phononic crystal composed of alternating piezoelectric and PMMA plates

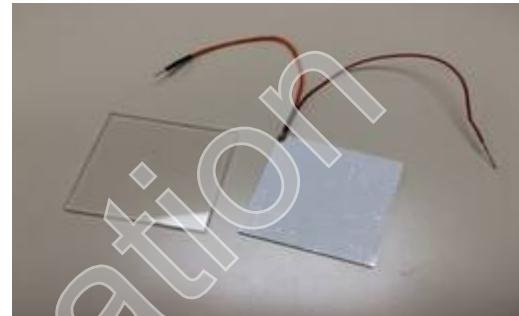
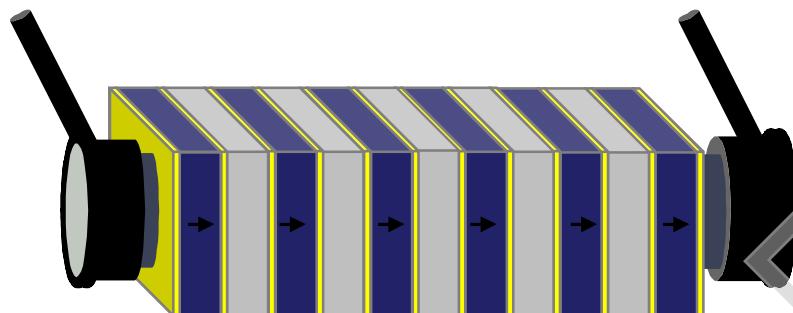


How to get experimentally both the band structure and the amplitude transmission coefficient through a slab of PC ?



## Propagation through a stack of plates

1D phononic crystal composed of alternating piezoelectric and PMMA plates



For a sake of simplicity, we consider a harmonic plane wave transmitted through a thickness  $d_n$  of PC:

$$s(t) = A e^{i(k_x d_n - \omega_0 t)} e^{-k_x^* d_n}$$

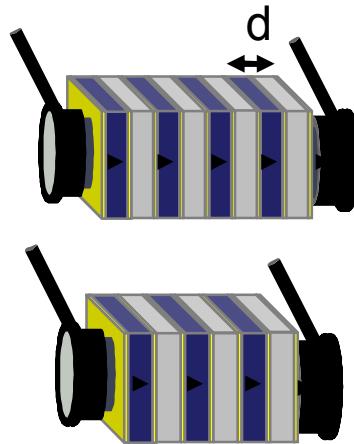
With complex wave number

$$k_x = k'_x + jk''_x$$

How to get experimentally both the band structure and the amplitude transmission coefficient of the waves through the PC ?

## Propagation through a stack of plates

Experiments : aquisitions with respectivelly 1,2,3 and 4 layers

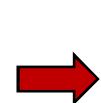


transmitted signal  
through the stack.  
Pulse excitation

Temporal  
signal  
 $s_{n+1}(t)$

Temporal  
signals  $s_n(t)$

$$Q = \frac{F_{n+1}(j\omega)}{F_n(j\omega)} = e^{jk_x' d} e^{-k_x'' d}$$



FFT

$$F_{n+1}(j\omega) = F(j\omega) e^{jk_x' (n+1)d} e^{-k_x'' (n+1)d}$$

$$F_n(j\omega) = F(j\omega) e^{jk_x' nd} e^{-k_x'' nd}$$

In previous expressions,  
 $F(j\omega)$  depends on the pass  
band of the transducers,  
the transmission at each  
interface, ....

- The real part of  
the wavenumber  
(dispersion)

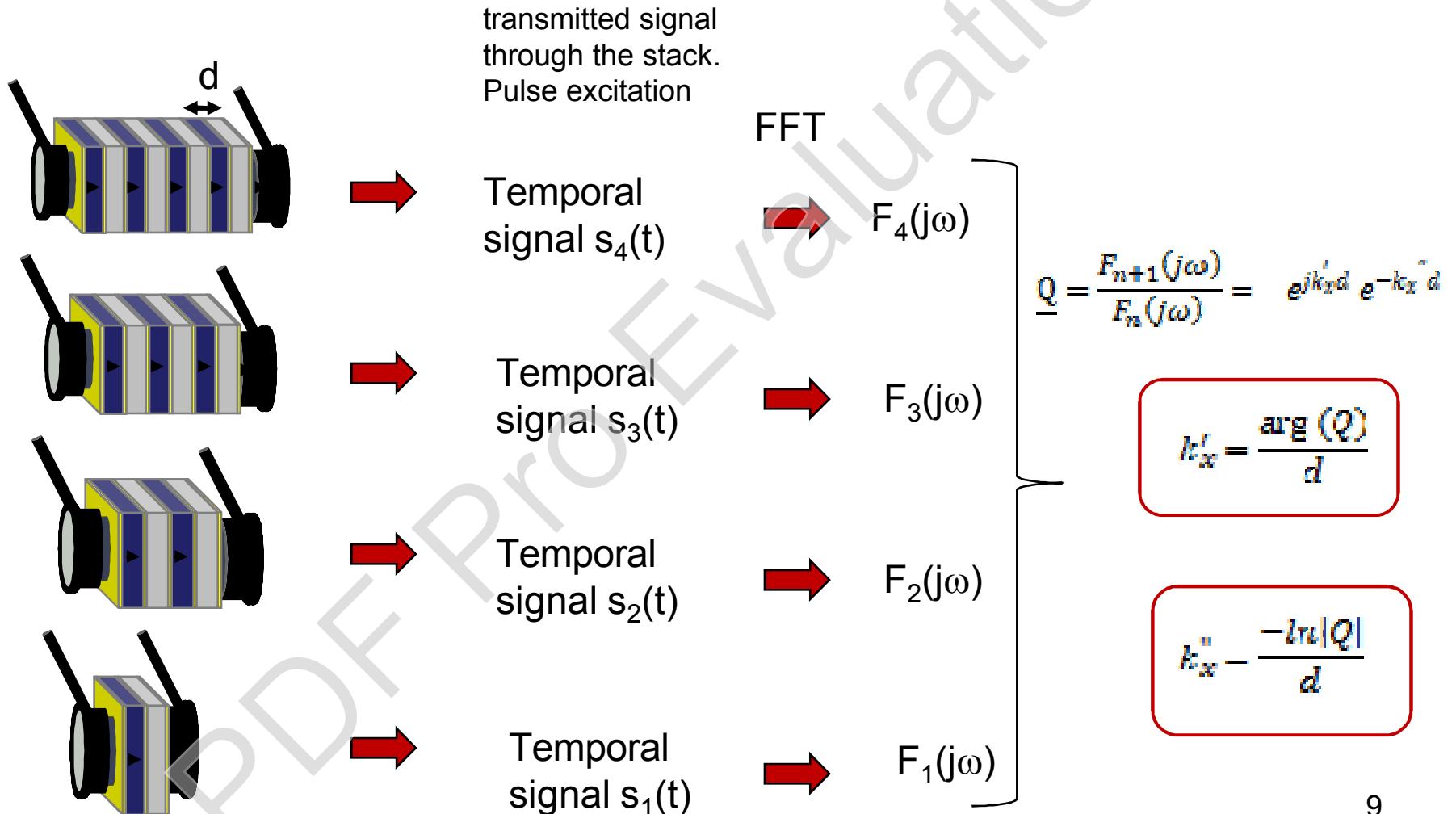
$$k_x' = \frac{\arg(Q)}{d}$$

- The imaginary part  
of the wavenumber  
(attenuation)

$$k_x'' = \frac{-\ln|Q|}{d}$$

## Propagation through a stack of plates

Experiments : aquisitions with respectively 1,2,3 and 4 layers



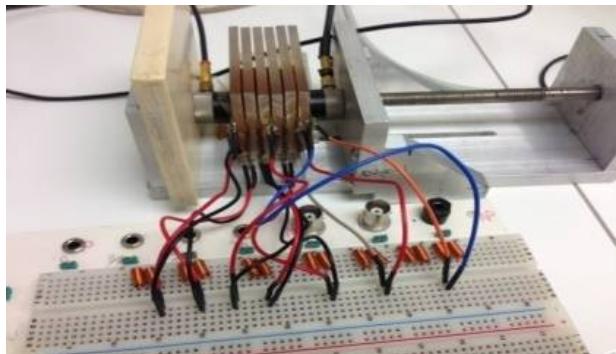
## Propagation through a stack of plates

## Frequency tunability of Phononic crystals

MIRAGES ANR-12-BS09-0015 project : Active metamaterials and phononic crystals controlled by electric and magnetic fields

Partners: IEMN CNRS 8520 (Lille, France), Thales RT, I2M (Bordeaux), LOMC UMR CNRS 6294, GREMAN UMR 7347 (Tours, France).

- 1D piezoelectric phononic crystal



PhD Thesis, Sid Ali Mansoura  
Collaboration with  
Anne-Christine Lhadky-Hennion, Bertrand Dubus  
IEMN, UMR 8520 CNRS, Lille, France



Mansoura *et al*, Smart Mater. Struct. 24 (2015)

- Lamb wave propagation in phononic piezoelectric plates



Kherraz *et al*, Appl.Phys.Lett 108, 093503 (2016)

PhD Thesis, Nesrine Kherraz  
Collaboration with  
Franck Levassort, Lionel Haumesser.  
GREMAN, UMR 7347 CNRS, Tours, France

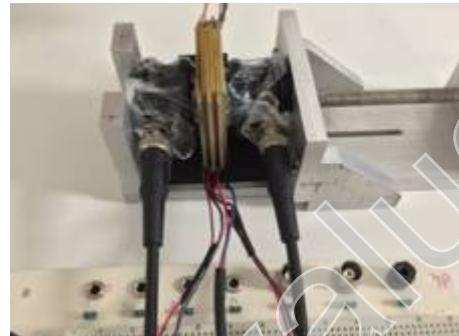


## Propagation through a stack of plates

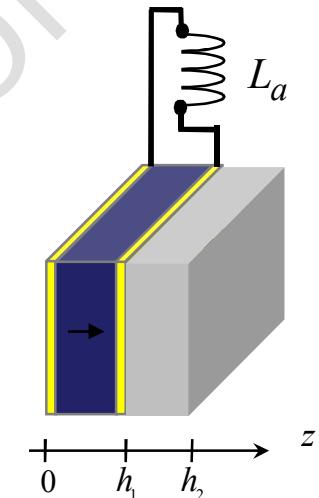
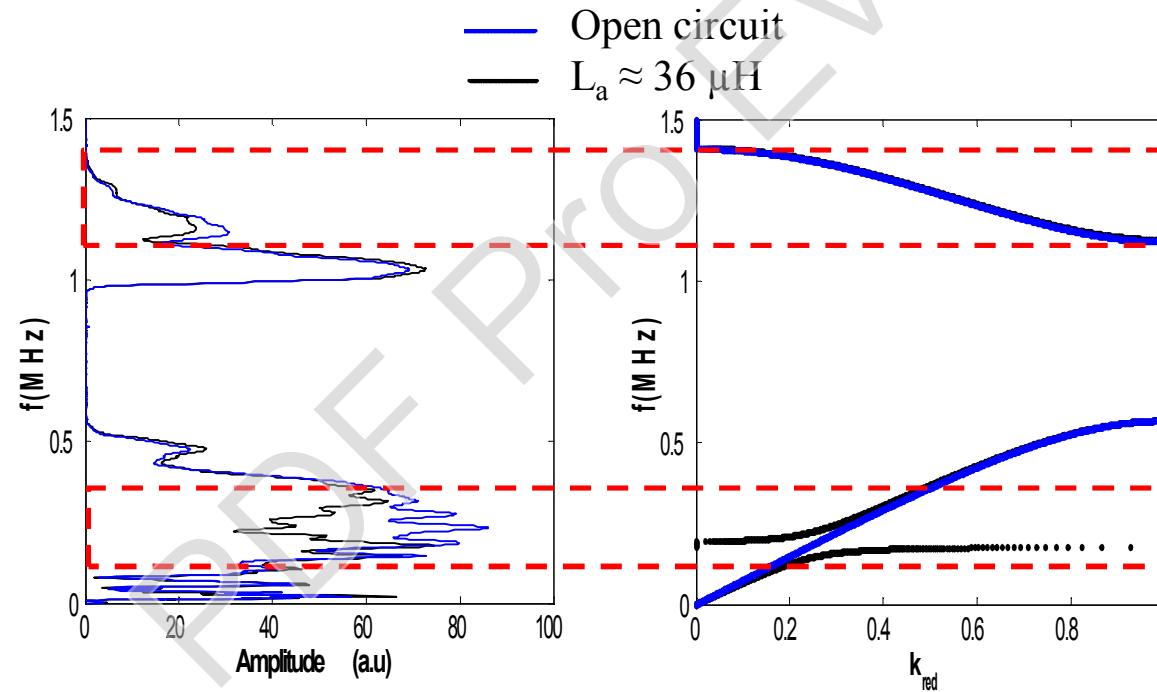
## Piezoelectric Phononic Crystal connected to inductances

### □ Hybridization gap: experimental measurements

Phononic crystal:  
stack of piezoelectric  
plates PZ27  
(50mm\*50mm) and et de  
plaques de plexiglass



### □ Opening a gap in LF range



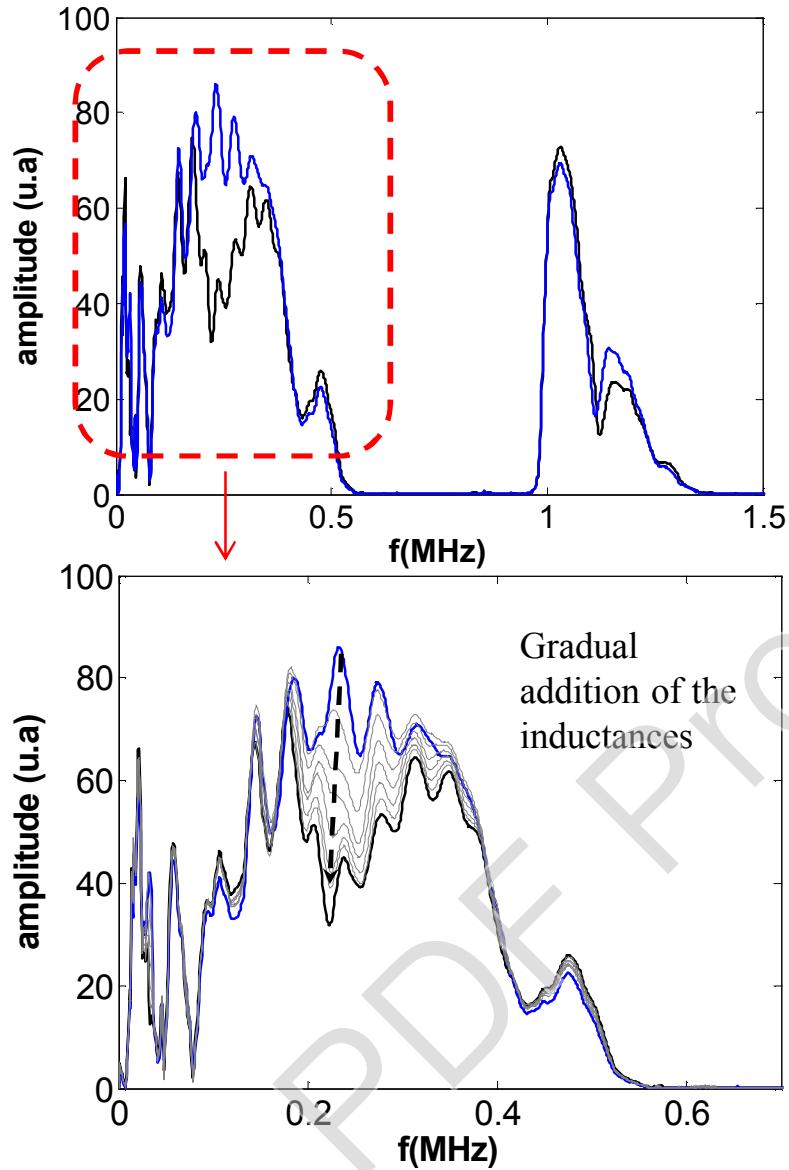
New band gap due to the  
electrical resonance

$$f_{\text{elec}} = \frac{1}{2\pi \sqrt{L_a C_0}}.$$

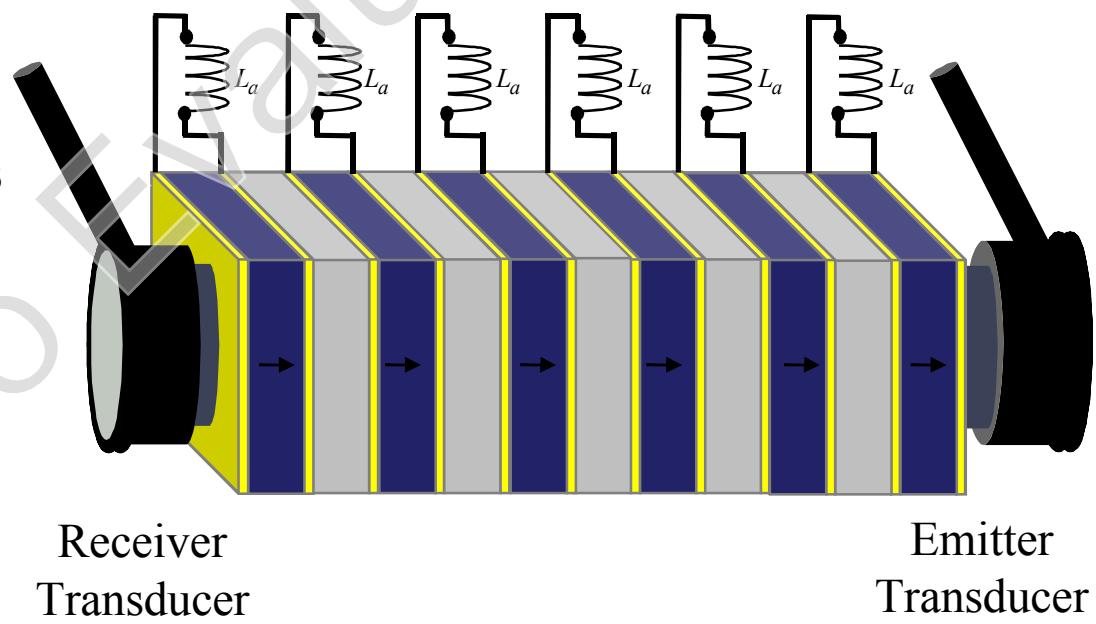
$C_0$  : Static capacitance of  
the piezo plate 11

## Propagation through a stack of plates

## Piezoelectric Phononic Crystal connected to inductances

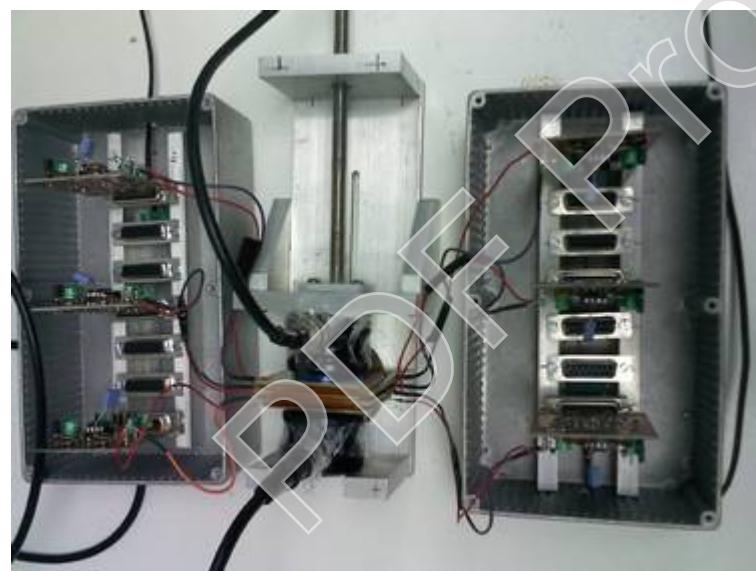
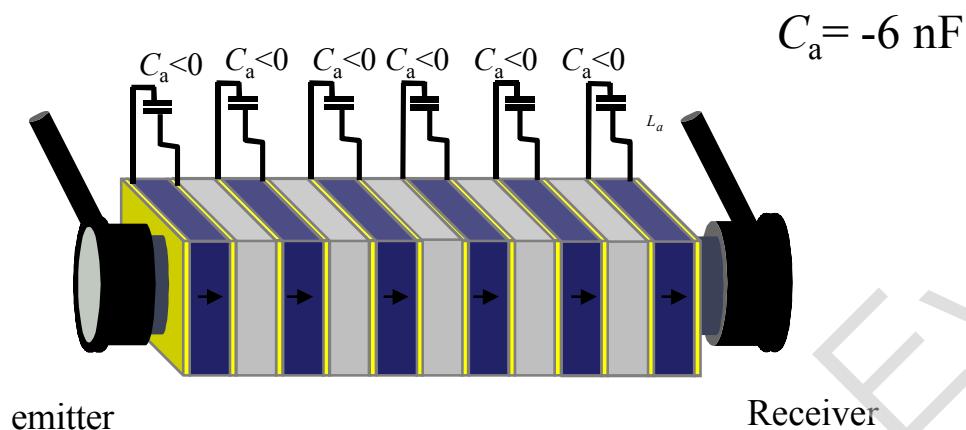


Experimental transmission  
through the PC connected to the  
inductances

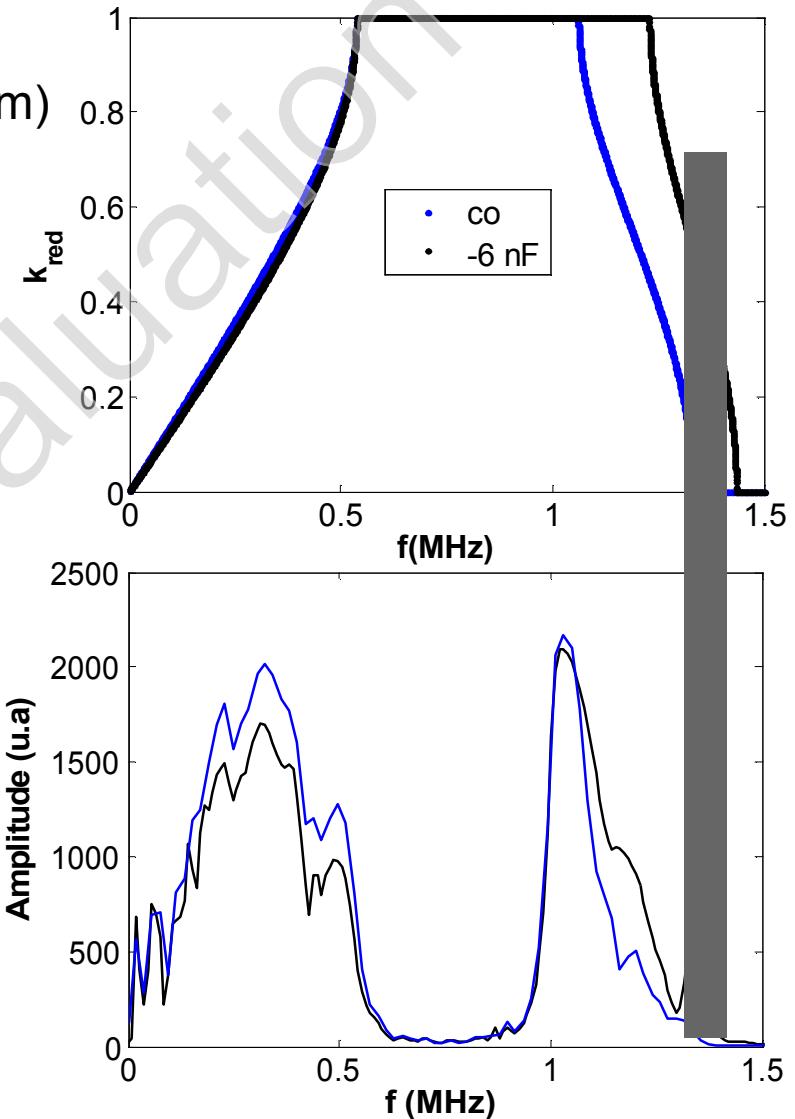


## Propagation through a stack of plates

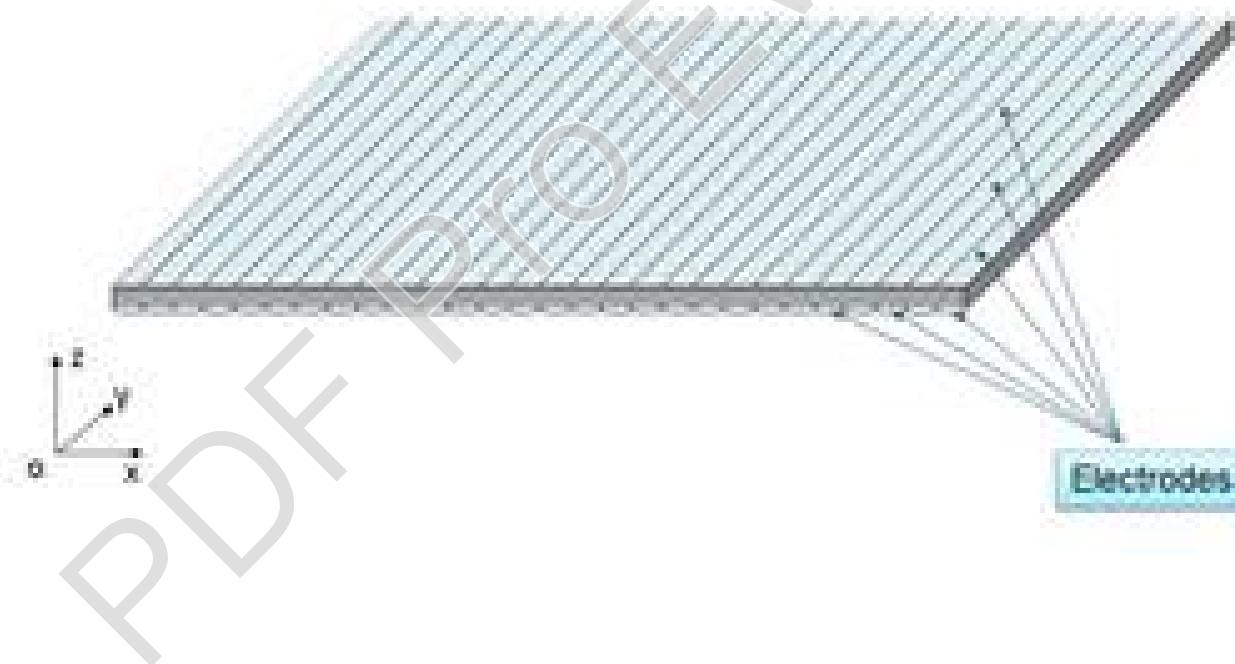
1D phononic crystal composed of alternating piezoelectric (PZ27) and PMMA plates ( $\epsilon_p=0.5\text{mm}$ ) (6 elementary cells)



## Piezoelectric Phononic Crystal connected to negative capacitances

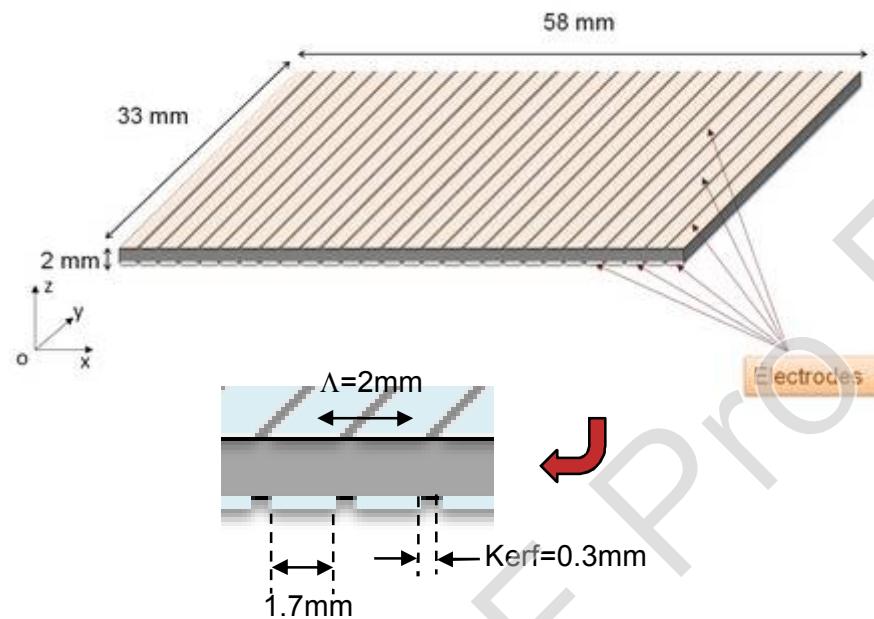


### Lamb wave propagation in phononic piezoelectric plates



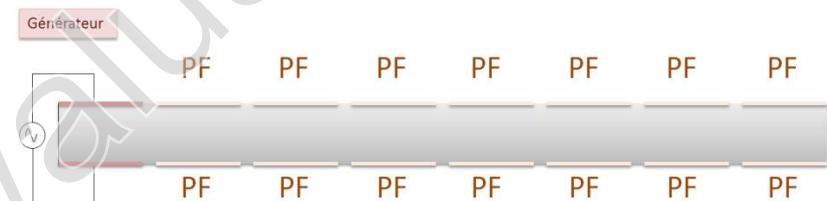
# Experimental implementation of the piezoelectric PC plate

Homogeneous piezoelectric plate (PZ26)

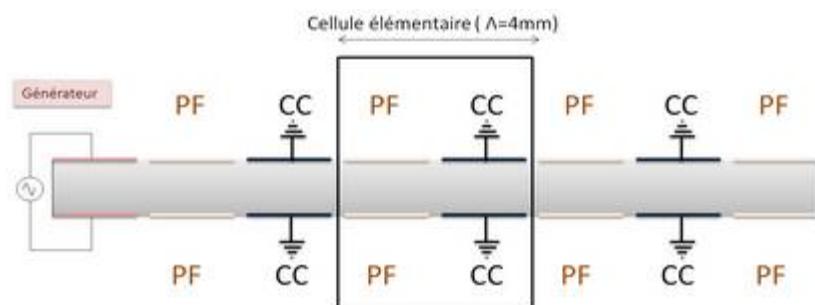


Configuration 1

PF : Floating potential  
CC : short circuit

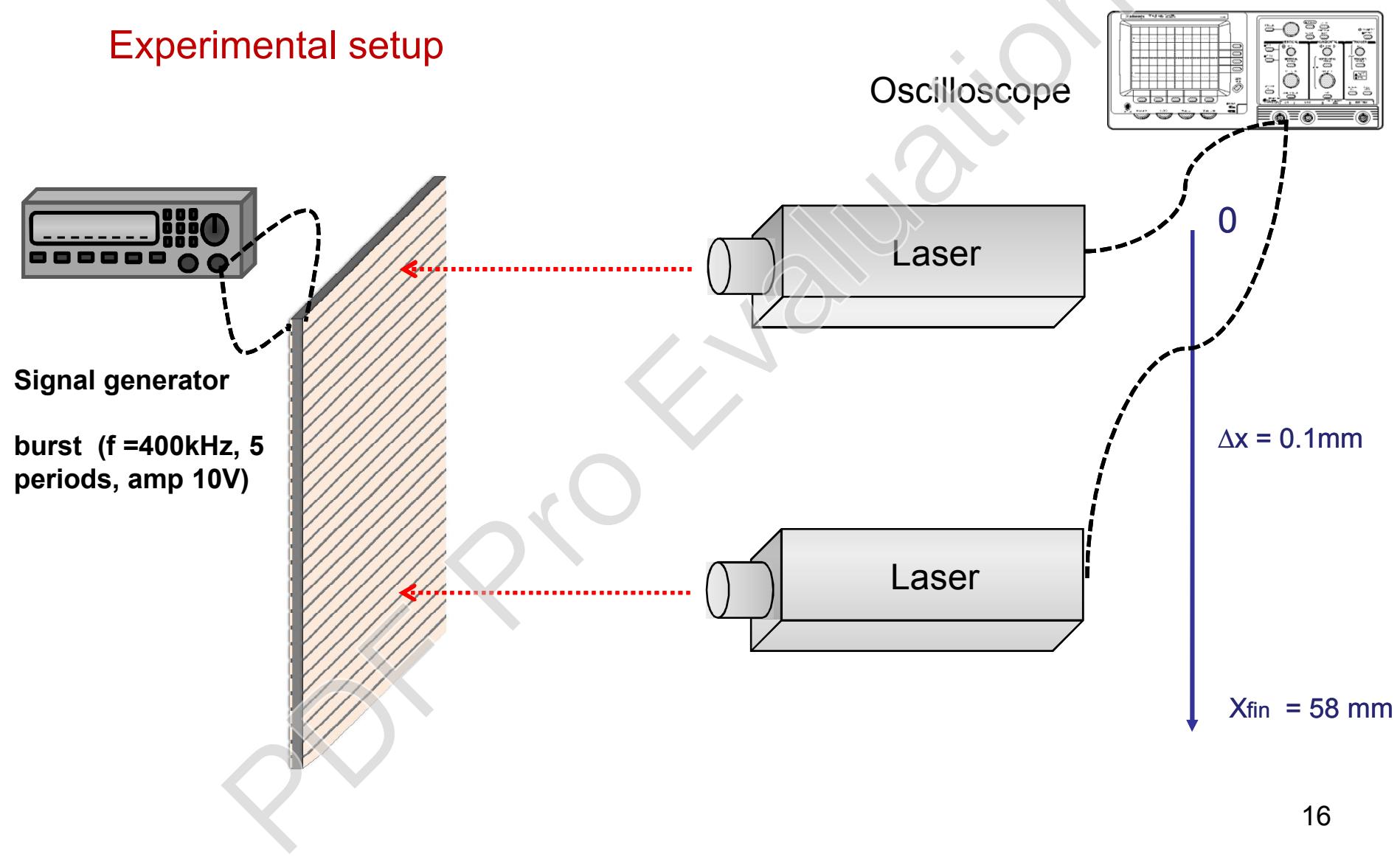


Configuration 2



# Piezoelectric PC plate : experimental study

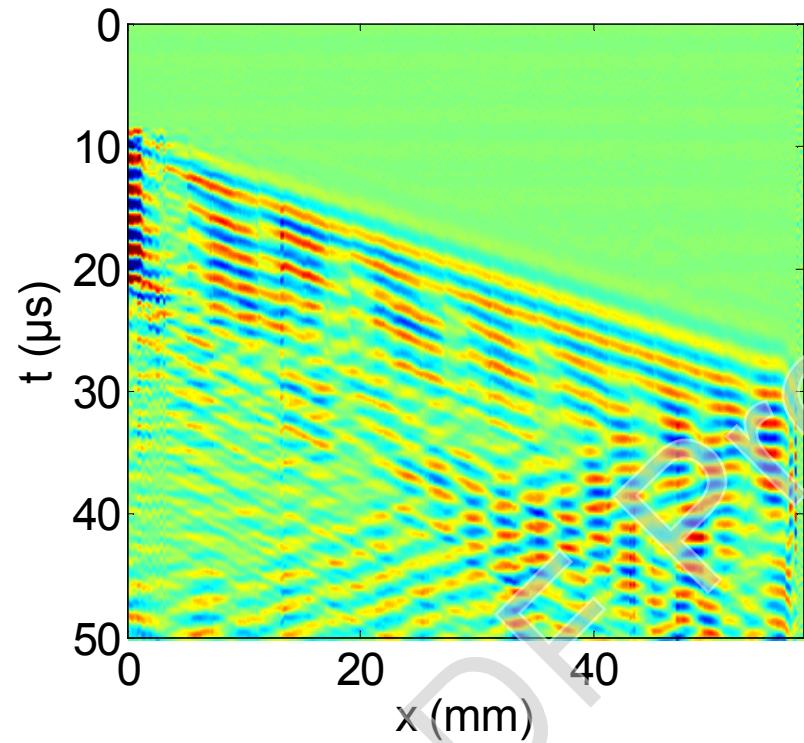
## Experimental setup



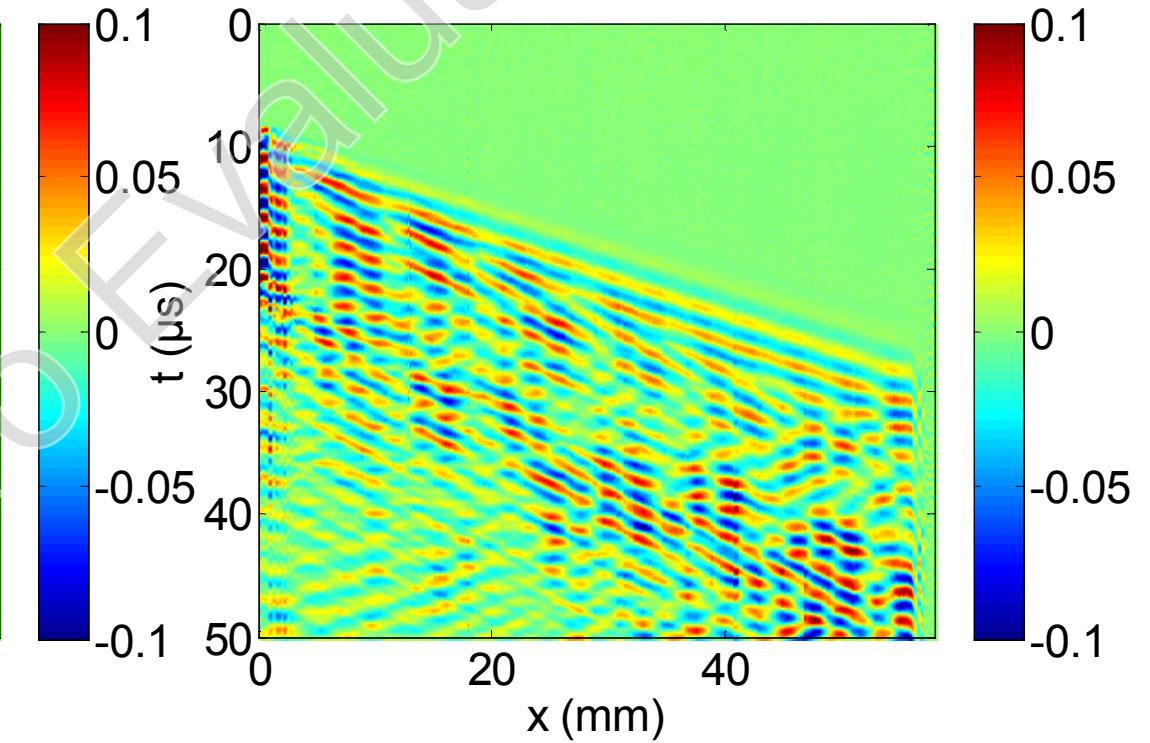
# Piezoelectric PC plate : experimental study

Temporal signals

Configuration 1

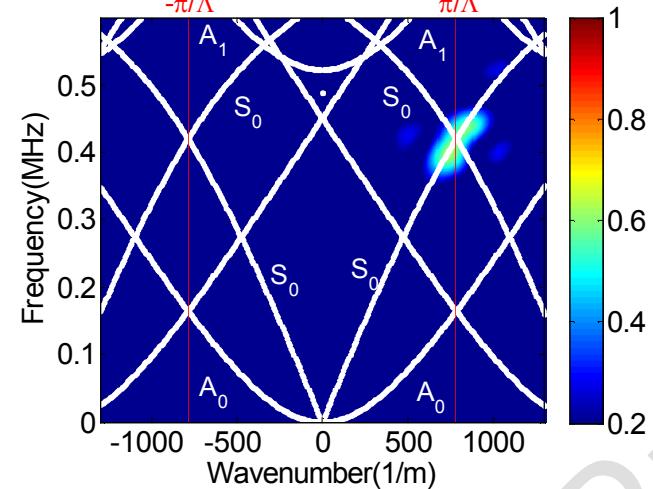
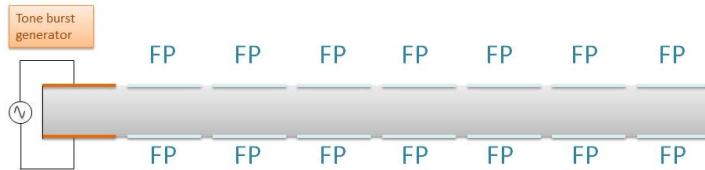


Configuration 2

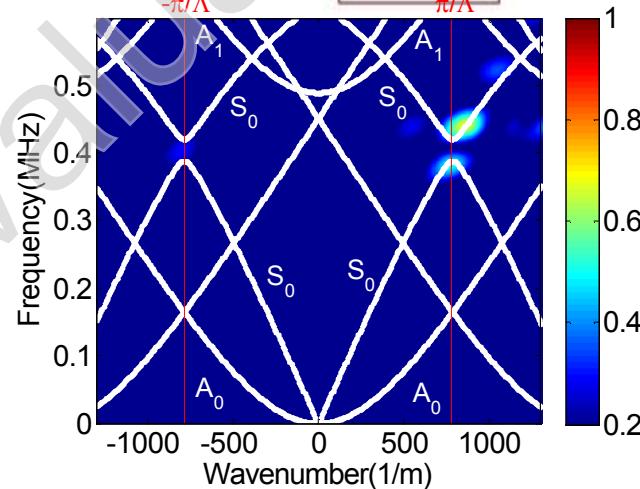
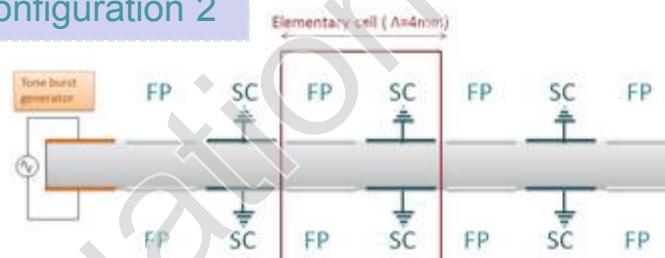


# Piezoelectric PC plate : experimental study

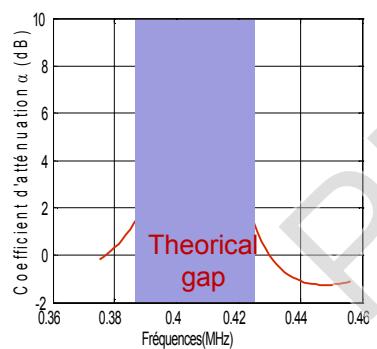
Configuration 1



Configuration 2



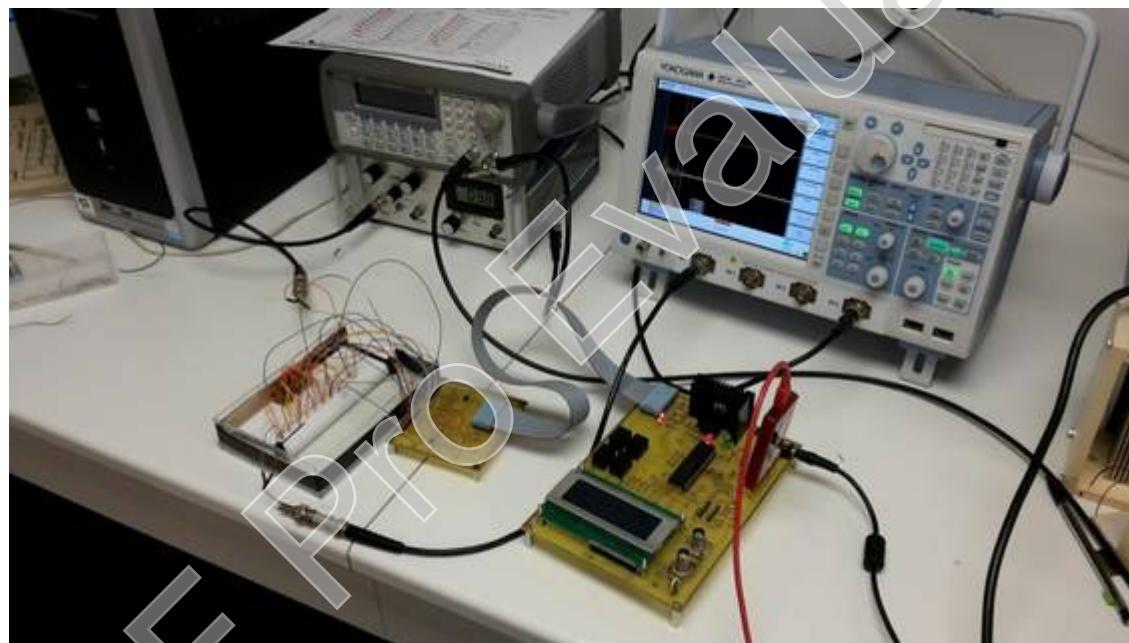
Attenuation coefficient



$$\approx 2 \log \left( \frac{\text{amplitude } E_0 \text{ (fig.1)}}{\text{amplitude } E_0 \text{ (fig.2)}} \right)$$

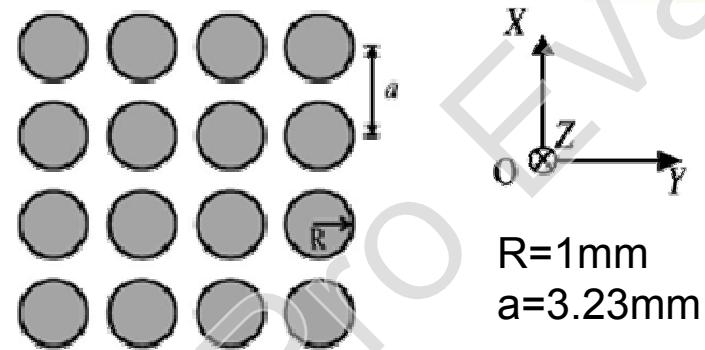
Attenuation of 10 dB for a length corresponding to 10 elementary cells at f=408kHz

- Tuning in real time the the EBCs thanks to a microcontroller and controlled switchs



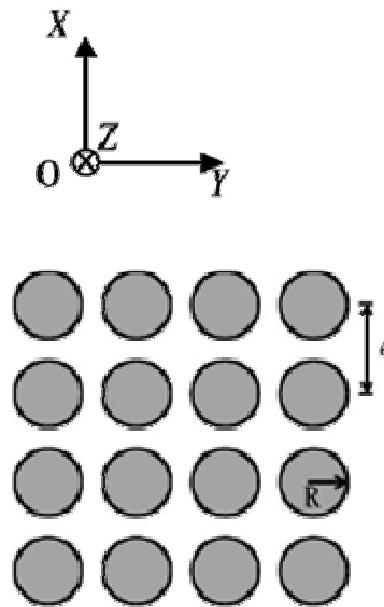
## Square array of steel cylinders embedded in an epoxy matrix.

Présentation de la structure périodique étudiée

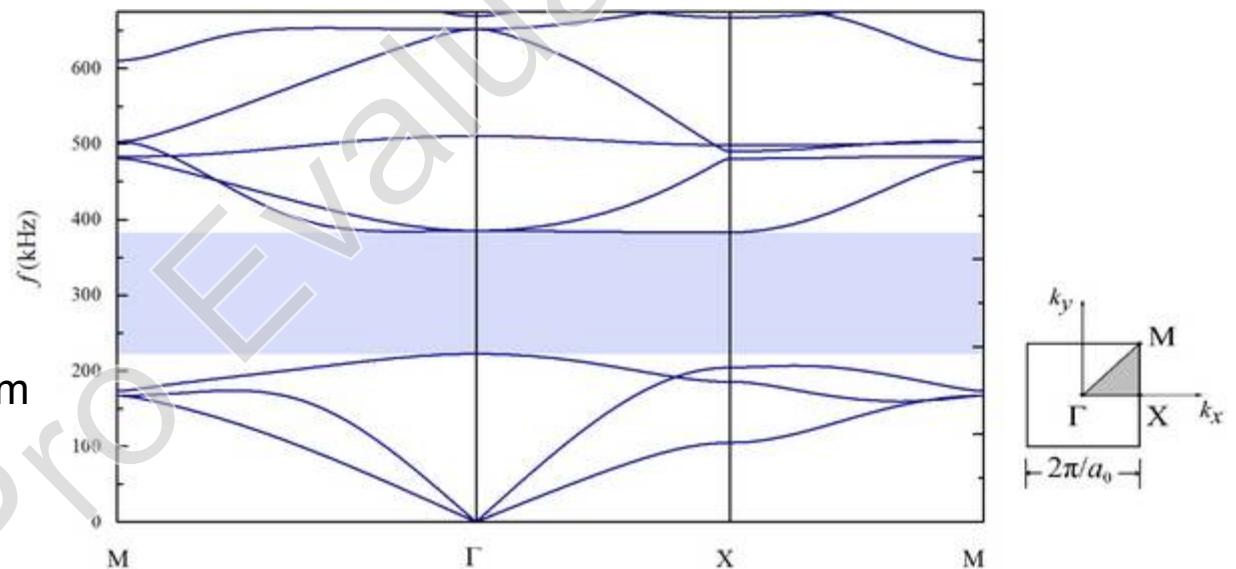


Square array (lattice constant  $a=3.23$  mm) of steel cylinders (diameter  $D=2$  mm) embedded in an epoxy matrix.

## Square array of steel cylinders embedded in an epoxy matrix.



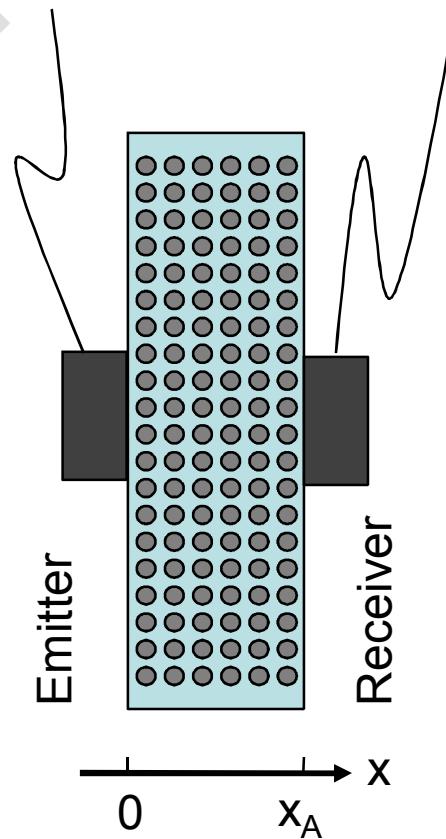
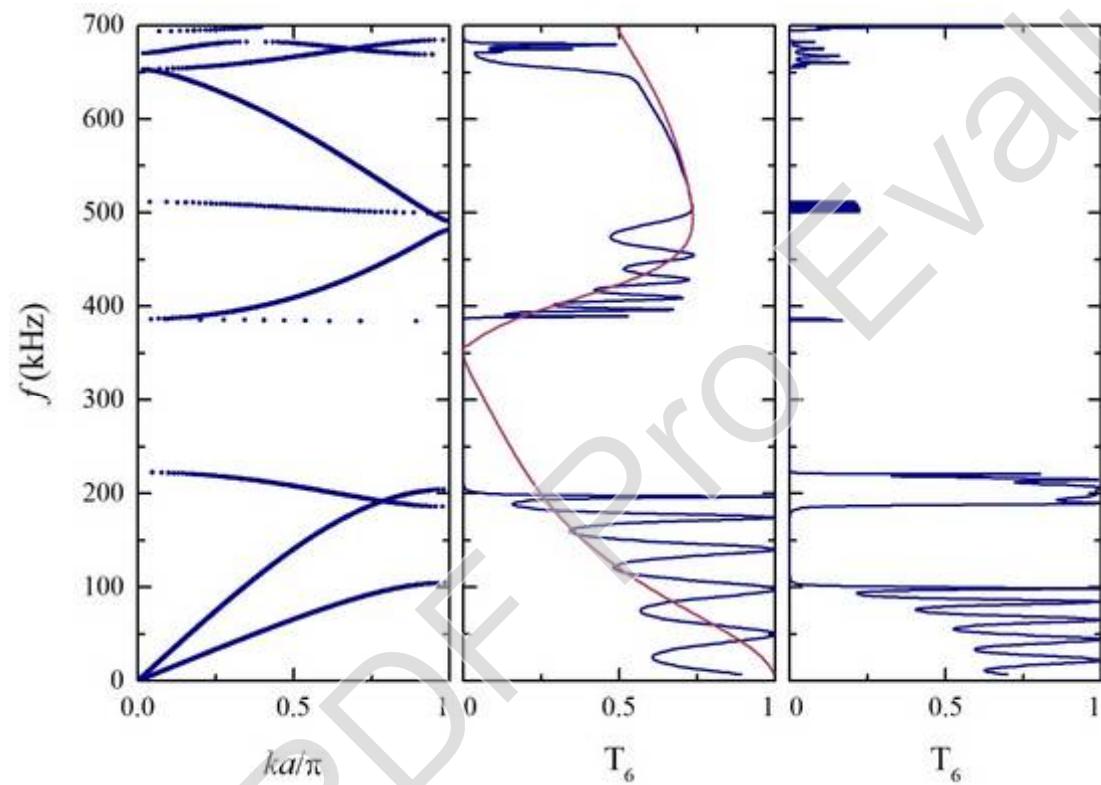
Band structure (only modes in the plane perpendicular to the inclusions are shown). Layered Multiple Scattering Method, (R. Sainidou)



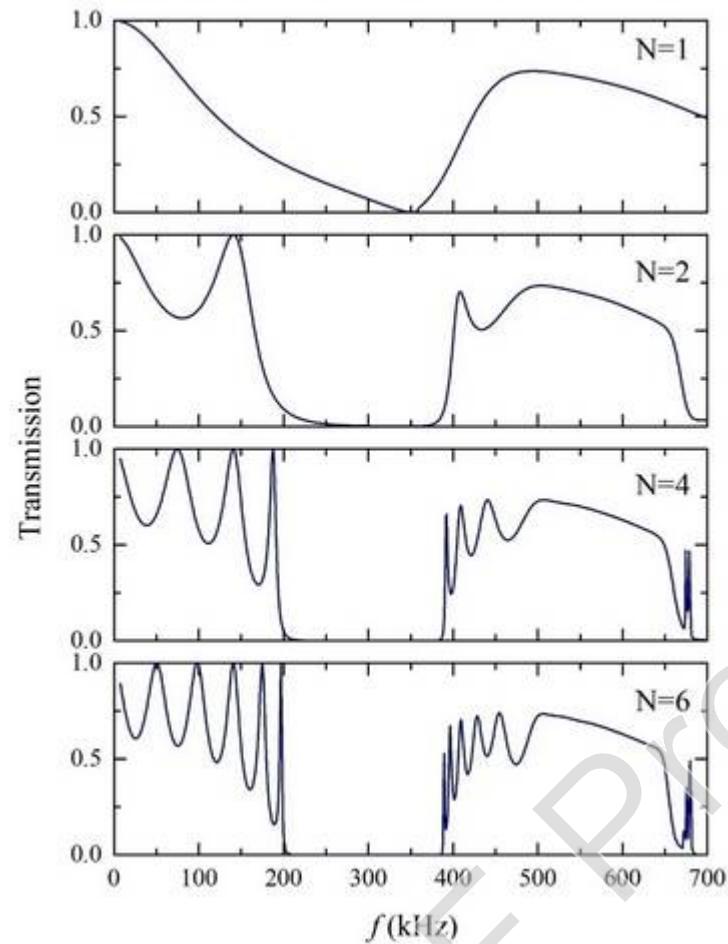
The shaded area represent the first absolute band gap : Hybridization gap for « longitudinal » bands and Bragg gap for « transverse » bands).

## Square array of steel cylinders embedded in an epoxy matrix.

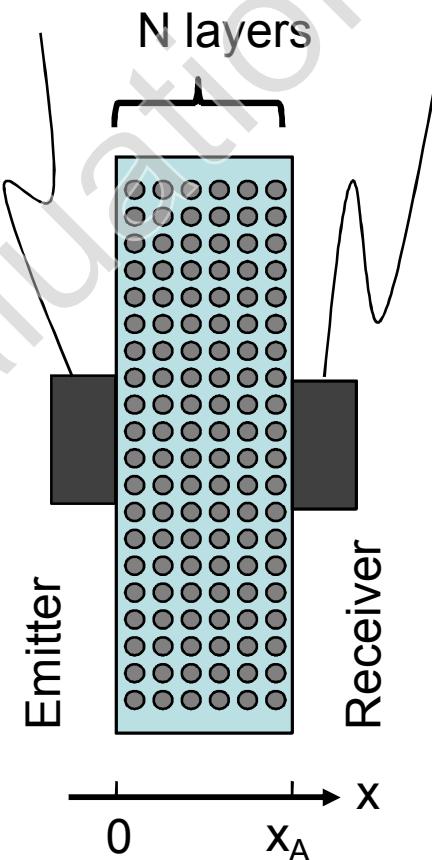
Transmission of a longitudinal (middle) and transverse (right) elastic wave incident normally on a six layers thick slab of the crystal whose band structure is also shown (left).



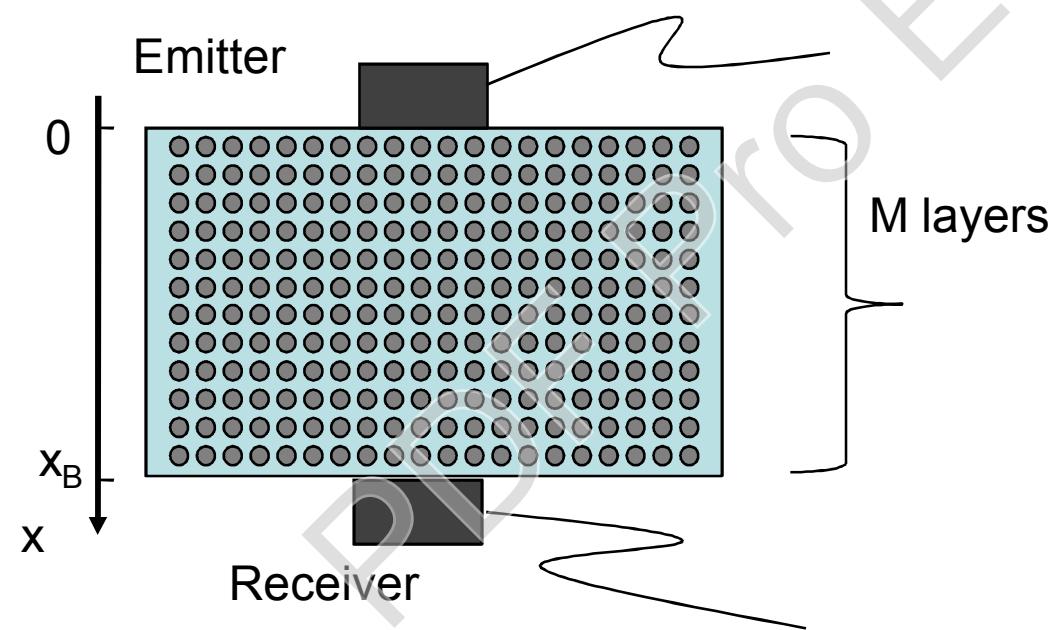
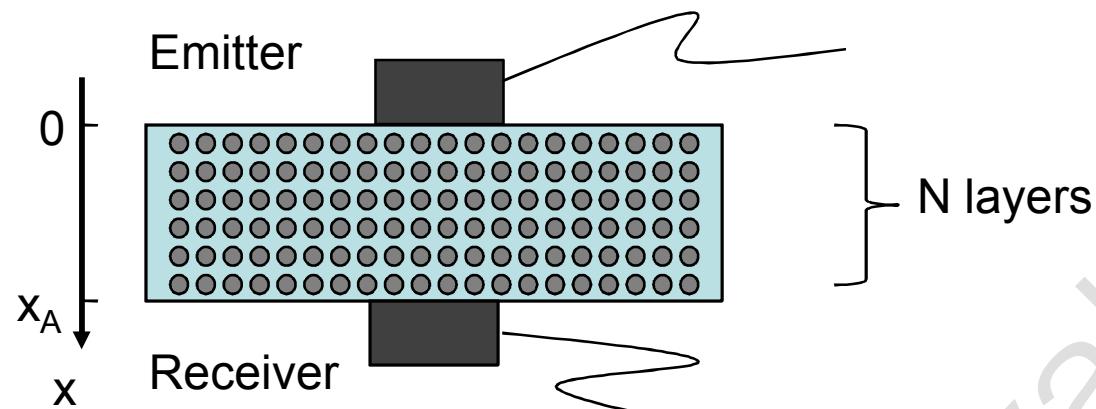
## Square array of steel cylinders embedded in an epoxy matrix.



Transmission of a **longitudinal elastic wave** incident normally on a finite slab of the crystal consisting of  $N$  linear arrays of cylinders.

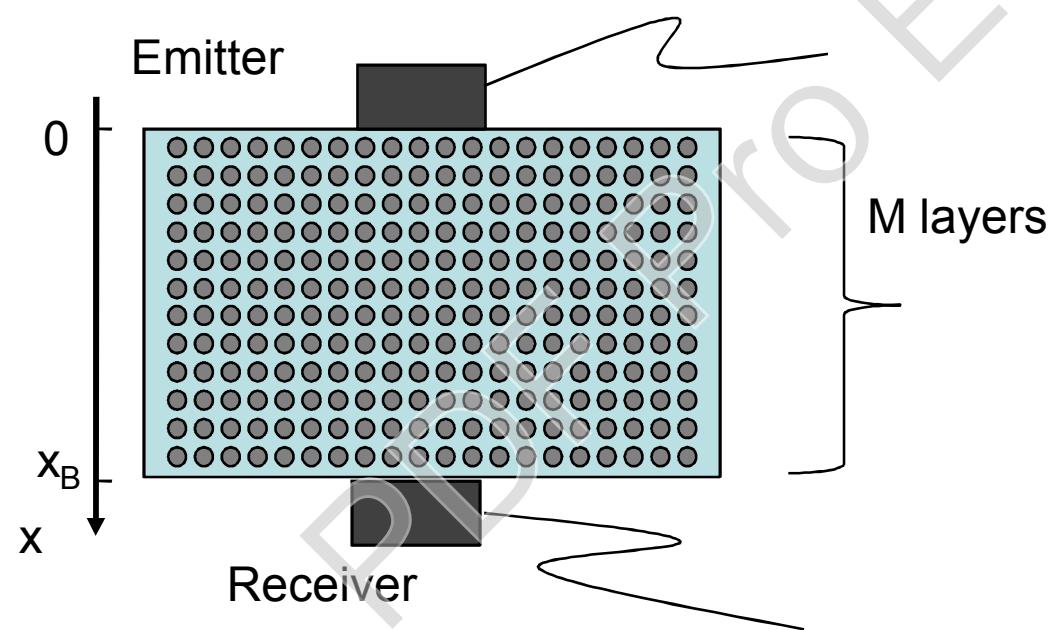
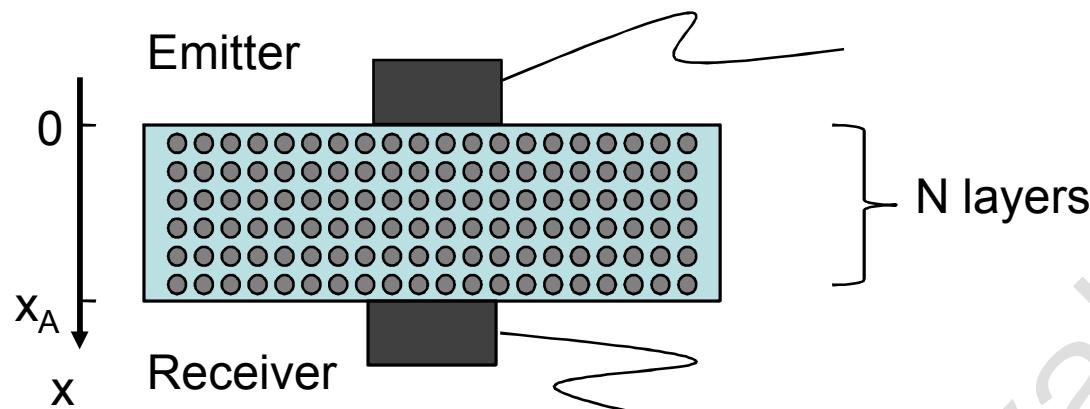


## Square array of steel cylinders embedded in an epoxy matrix.



The experimental transmission through two different CP slabs of different thicknesses will be used to obtain the band structure of the CP.

## Square array of steel cylinders embedded in an epoxy matrix.

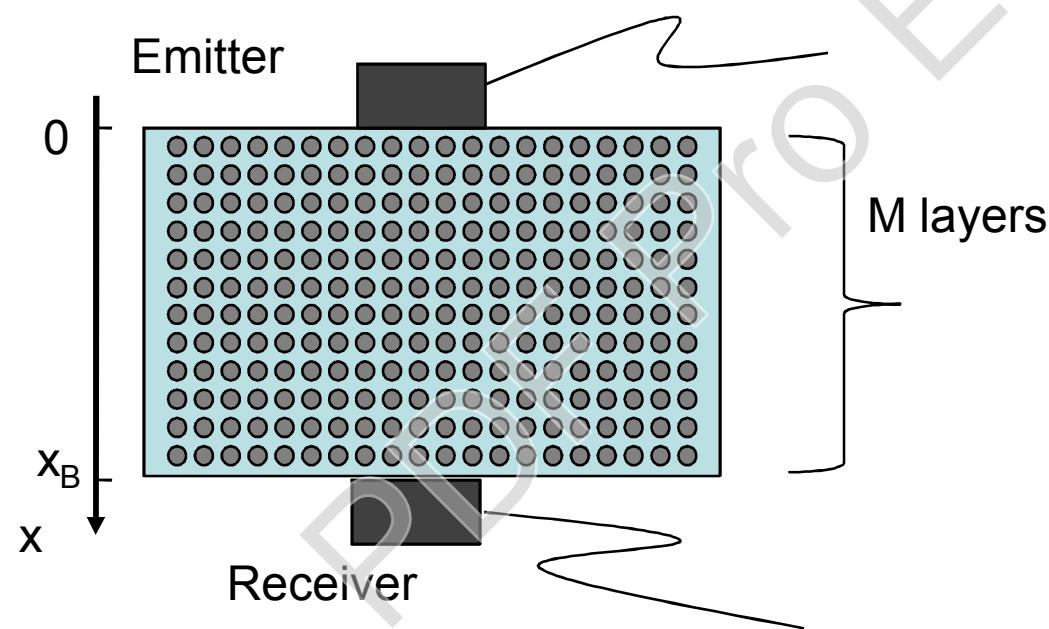
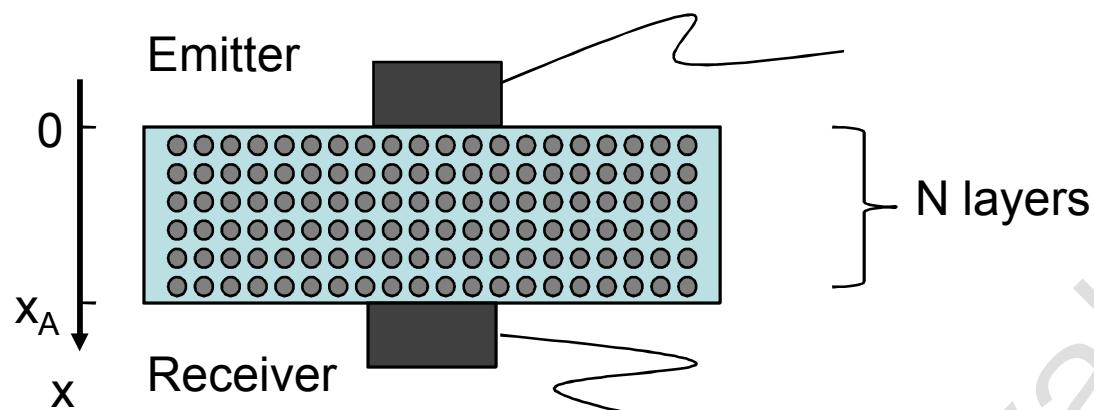


Fourier transform are performed on the transmitted signals through the PC with thicknesses respectively equal to  $x_A$  and  $x_B$  :

$$F_A(j\omega) = F(j\omega) e^{jk_x x_A} e^{-k_x^* x_A}$$

$$F_B(j\omega) = F(j\omega) e^{jk_x x_B} e^{-k_x^* x_B}$$

## Square array of steel cylinders embedded in an epoxy matrix.



The ratio of the two previous FFT gives

$$\underline{Q} = \frac{F_B(j\omega)}{F_A(j\omega)} = e^{ik_x'(x_B - x_A)} e^{-ik_x''(x_B - x_A)}$$

From which it is easy to deduced :

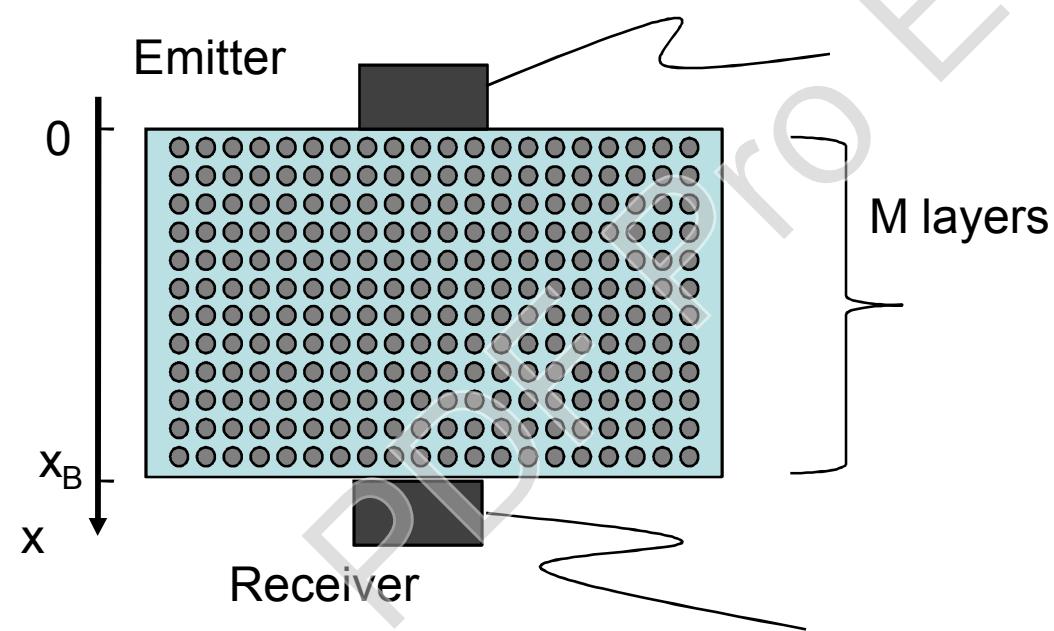
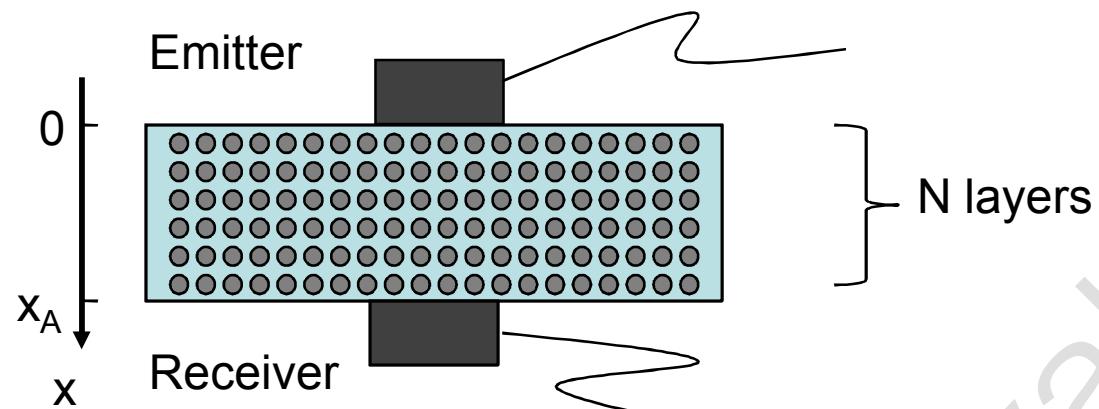
- The imaginary part of the wavenumber (attenuation)

$$k_x'' = \frac{-\ln|Q|}{(x_B - x_A)}$$

- The real part of the wavenumber (dispersion)

$$k_x' = \frac{\arg(Q)}{(x_B - x_A)}$$

**Square array of steel cylinders  
embedded in an epoxy matrix.**



# EXPERIMENTS

**Square array of steel cylinders  
embedded in an epoxy matrix.**

### ***MULTI-FUNCTIONAL PHONONIC CRYSTAL***



### **COLLABORATIONS**

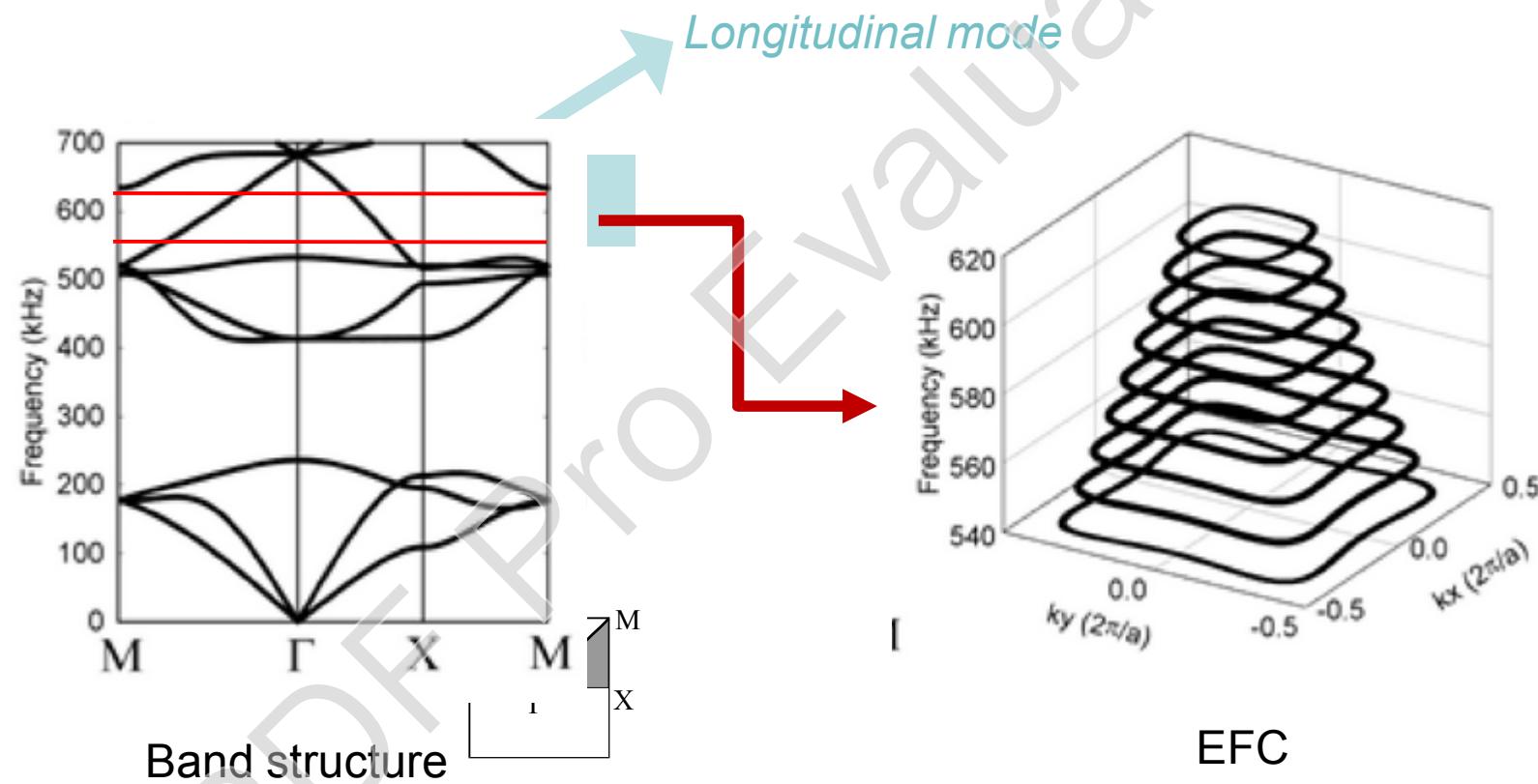
N. Swinteck, P.A. Deymier. *Department of Materials Science and Engineering, University of Arizona, Tucson, USA*

J. Vasseur. Institut d'Electronique, de Micro-électronique et de Nanotechnologie, UMR CNRS 8520.



**Square array of steel cylinders  
embedded in an epoxy matrix.**

EFC( $\omega = f(k_x, k_y)$ ) of square shape  
between 540 and 620 kHz



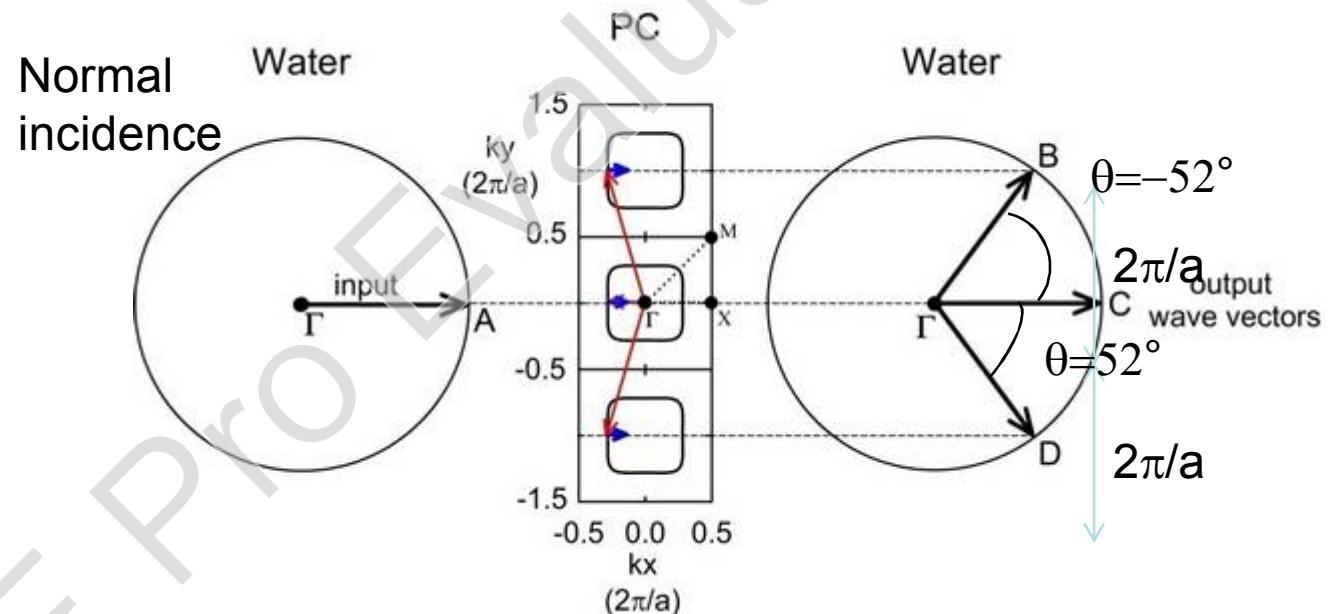
**Square array of steel cylinders  
embedded in an epoxy matrix.**

**MULTI-FUNCTIONAL PHONONIC CRYSTAL**

## Beam splitter

Conservation of the component of the  $\mathbf{k}$  vector parallel to the interface between the entrance (resp. exit) medium and the input (resp. output) side of the phononic crystal

k-diagram at frequency  $F=590\text{kHz}$



$$|\mathbf{k}_{\text{water}}| = \Gamma A = \omega / c_{\text{water}}$$

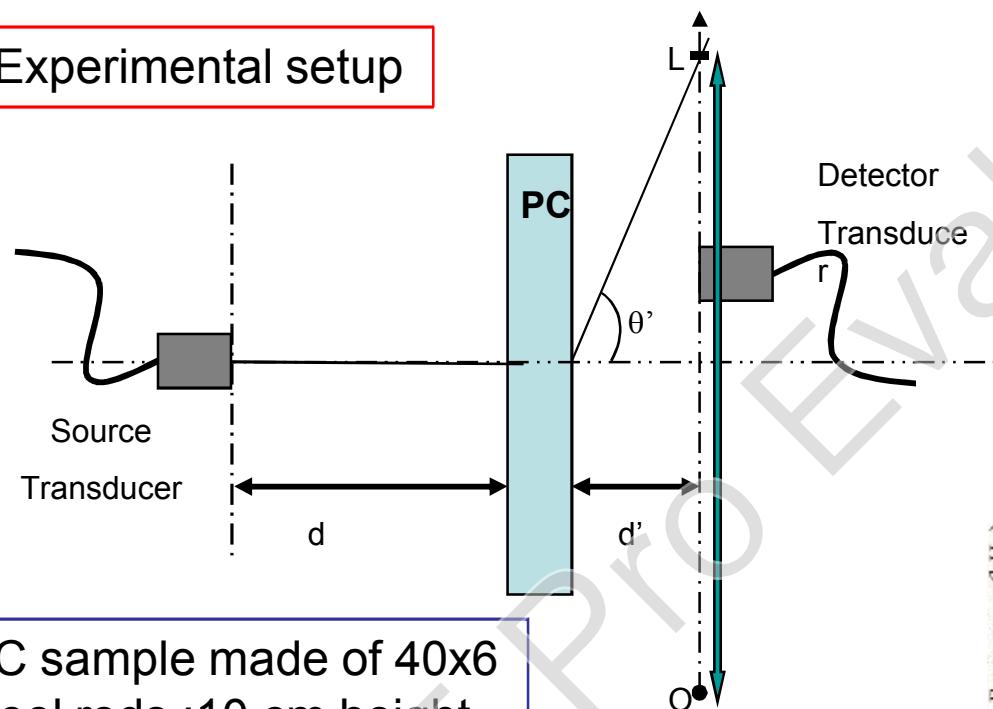
$$|\mathbf{k}_{\text{water}}| = \Gamma B = \Gamma C = \Gamma D = \omega / c_{\text{water}}$$

**Square array of steel cylinders  
embedded in an epoxy matrix.**

## MULTI-FUNCTIONAL PHONONIC CRYSTAL

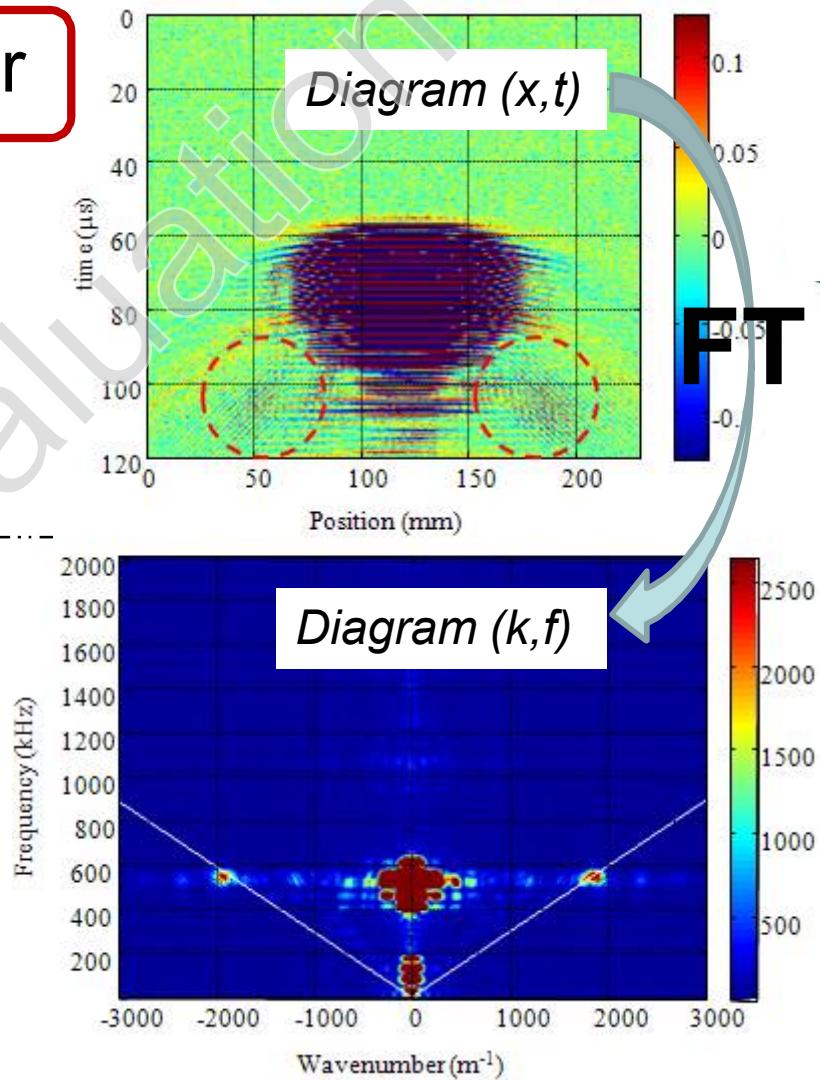
### Beam splitter

#### Experimental setup

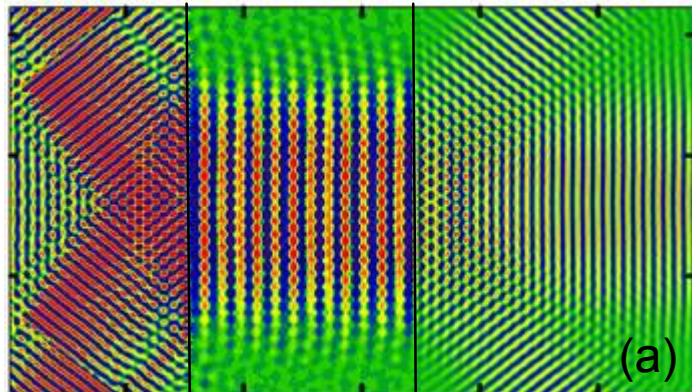


PC sample made of 40x6  
steel rods ;10 cm height

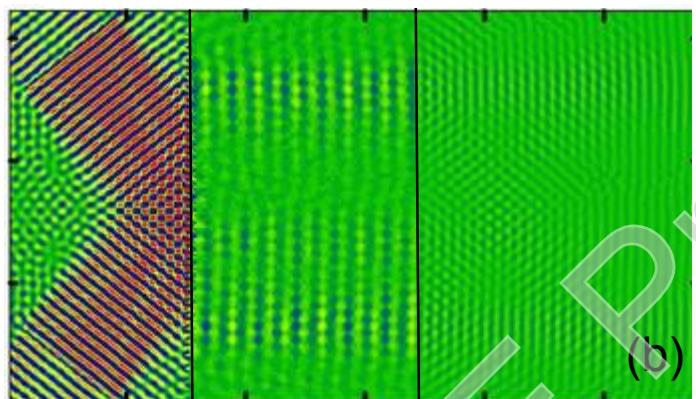
3 waves exit the PC at  $0^\circ$  and at  $\pm 51^\circ$



**Square array of steel cylinders  
embedded in an epoxy matrix.**



**Frequency = 590 kHz**



**Phase control device**

## MULTI-FUNCTIONAL PHONONIC CRYSTAL

### Phase control device

#### FDTD pressure field calculation

*Two acoustic waves (complementary angle inputs) in water impinge upon the PC surface at +52° and -52°.*

*(a) acoustic sources oscillate in-phase and excite identical Bloch modes in the PC k-space. Bloch wave amplitudes constructively interfere inside the PC and highly intense, collimated acoustic energy is observed inside the PC. On the backside of the PC, beam splitting is observed. The three exiting beams are very intense due to constructive wave interference.*

*(b) acoustic sources oscillate  $\pi$  radians out-of-phase. Wave amplitudes destructively interfere inside the PC, resulting in a near-zero pressure field on the backside of the crystal.*

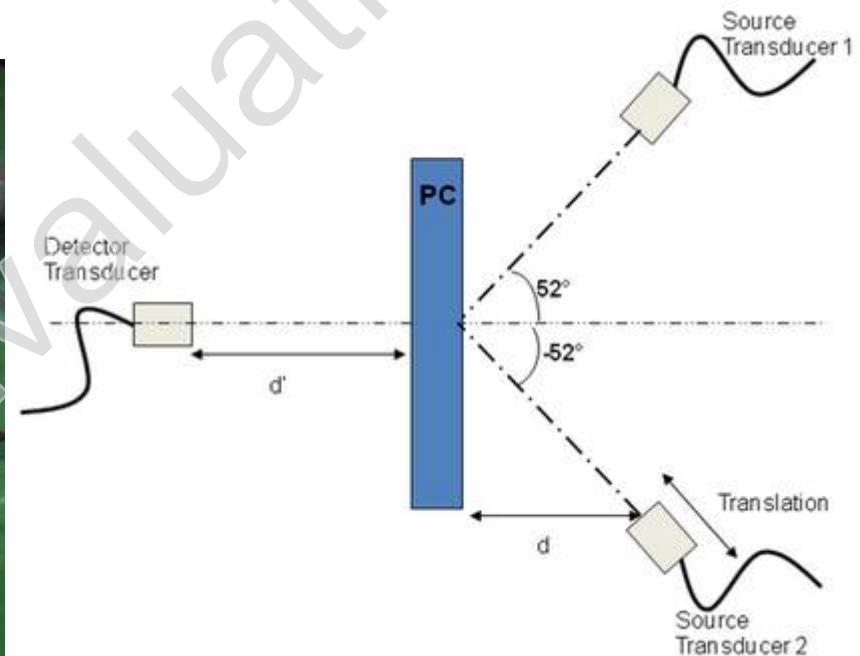
**Square array of steel cylinders  
embedded in an epoxy matrix.**

## MULTI-FUNCTIONAL PHONONIC CRYSTAL

### Experimental setup



### Phase control device

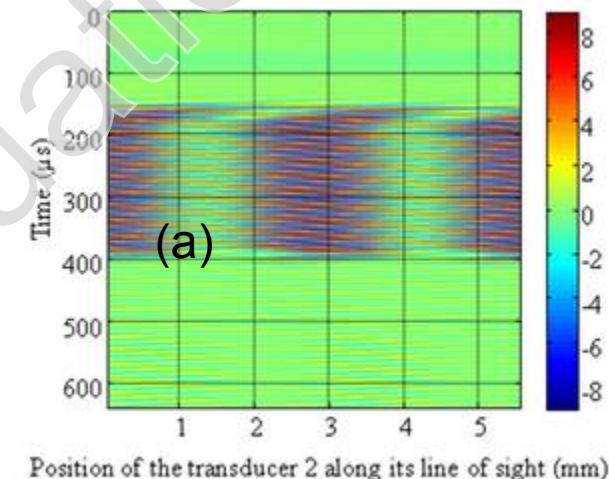


 Square array of steel cylinders  
embedded in an epoxy matrix.

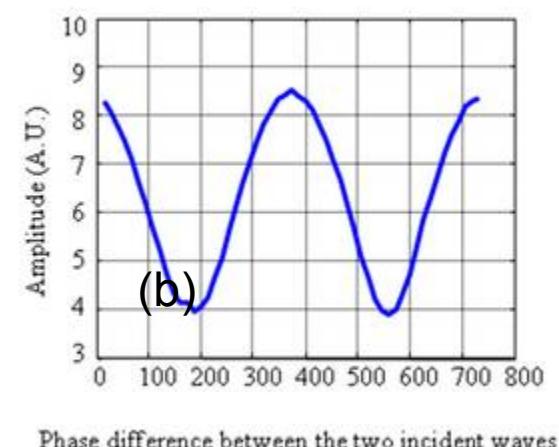
## MULTI-FUNCTIONAL PHONONIC CRYSTAL

### Phase control device

(a) Amplitude of the temporal response of a fixed detector transducer on the exit side of the PC subjected to two acoustic beams. The horizontal axis corresponds to the position of the second source along its line of sight;

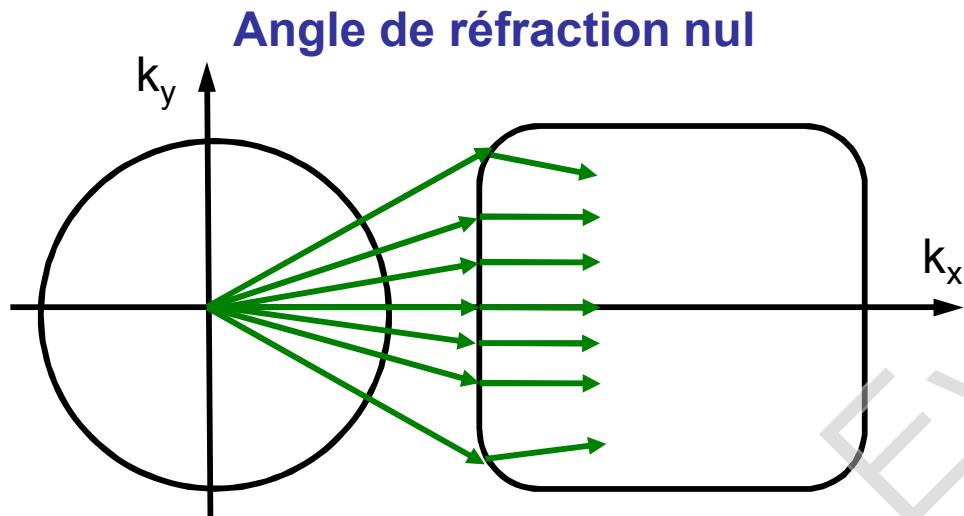


(b) Response of the detection transducer as a function of the phase difference between the two incident beams. Maxima (resp. minima) occur for phase difference equal to an even (resp. odd) multiple of  $180^\circ = \pi$  rad.



**Square array of steel cylinders  
embedded in an epoxy matrix.**

**MULTI-FUNCTIONAL PHONONIC  
CRYSTAL**



## Collimated beam

- Exploitation de la forme carré des courbes équi-fréquences

Contour équi-fréquence carré. La région plate du contour permet la collimation du faisceau.

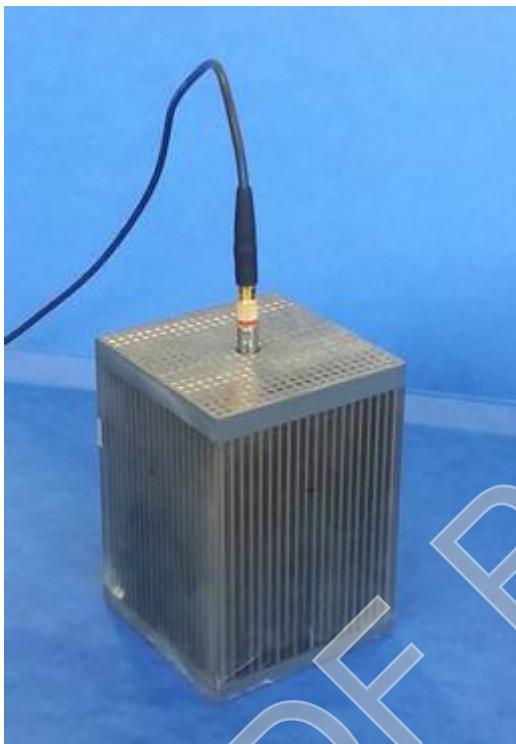
Si on place la source dans le cristal phononique ?

**Square array of steel cylinders  
embedded in an epoxy matrix.**

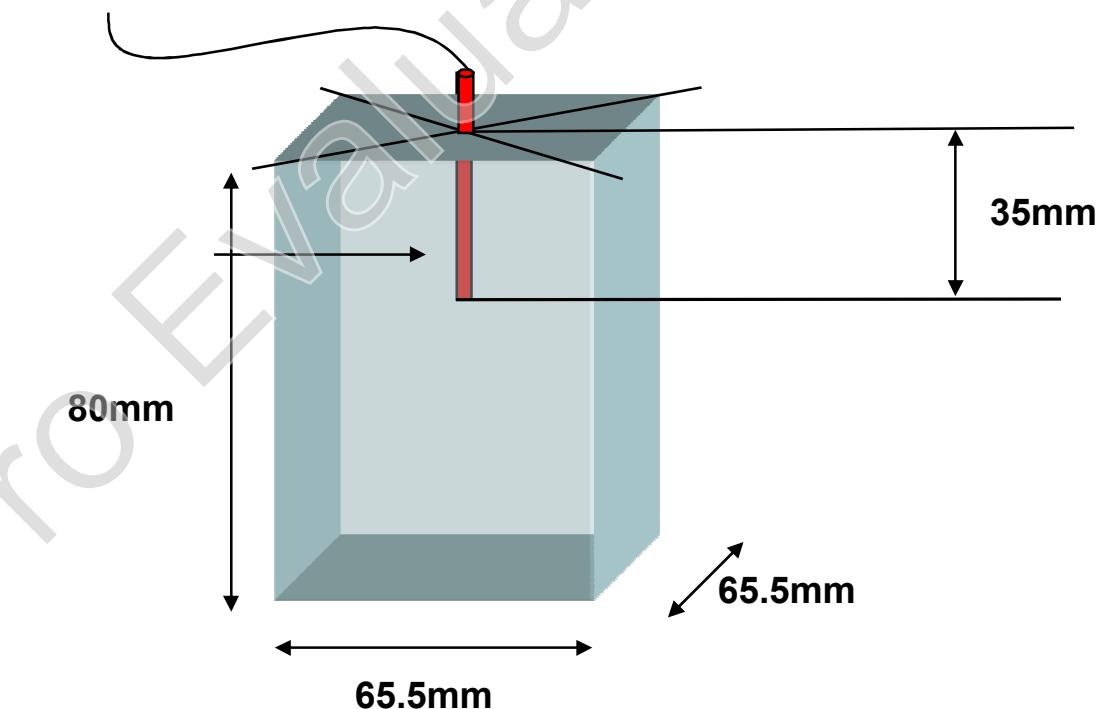
**MULTI-FUNCTIONAL PHONONIC  
CRYSTAL**

### Présentation de l'échantillon

- Le CP est constitué d'un réseau de 20 par 20 cylindres d'acier dans une matrice de résine époxy

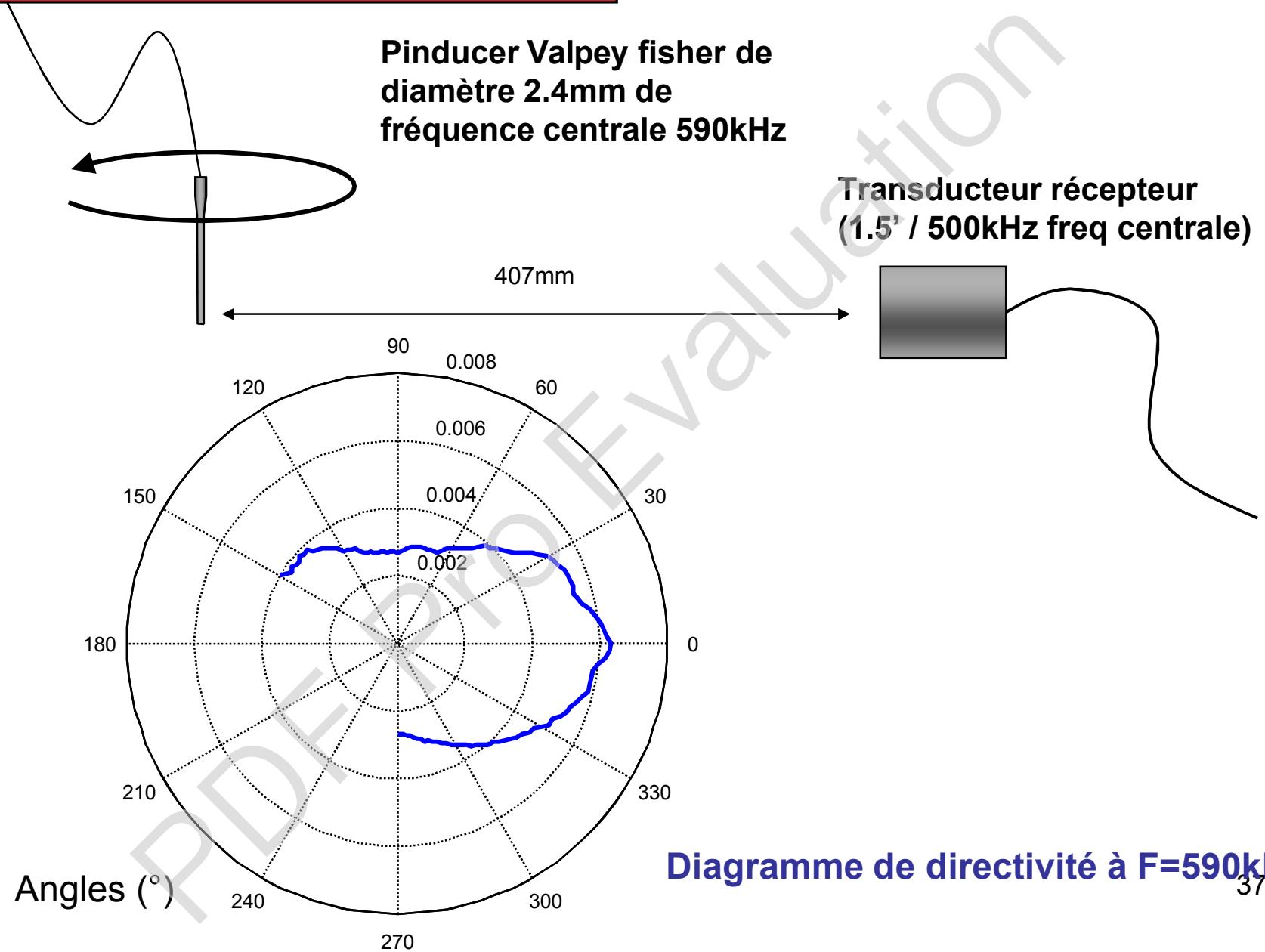


### Collimated beam



Square array of steel cylinders  
embedded in an epoxy matrix.

## Pinducer characterization

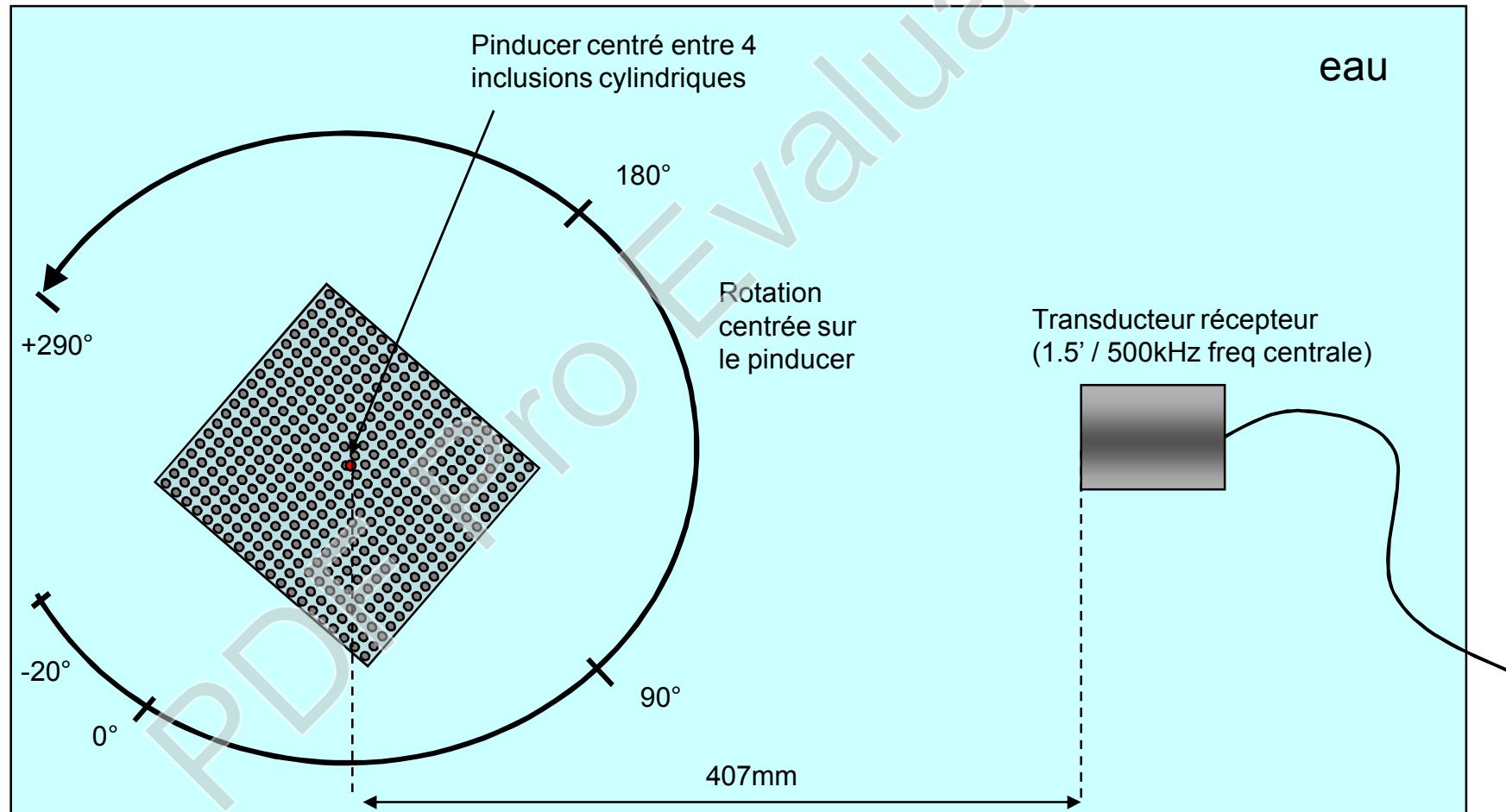


## Square array of steel cylinders embedded in an epoxy matrix.

## Experimental set-up

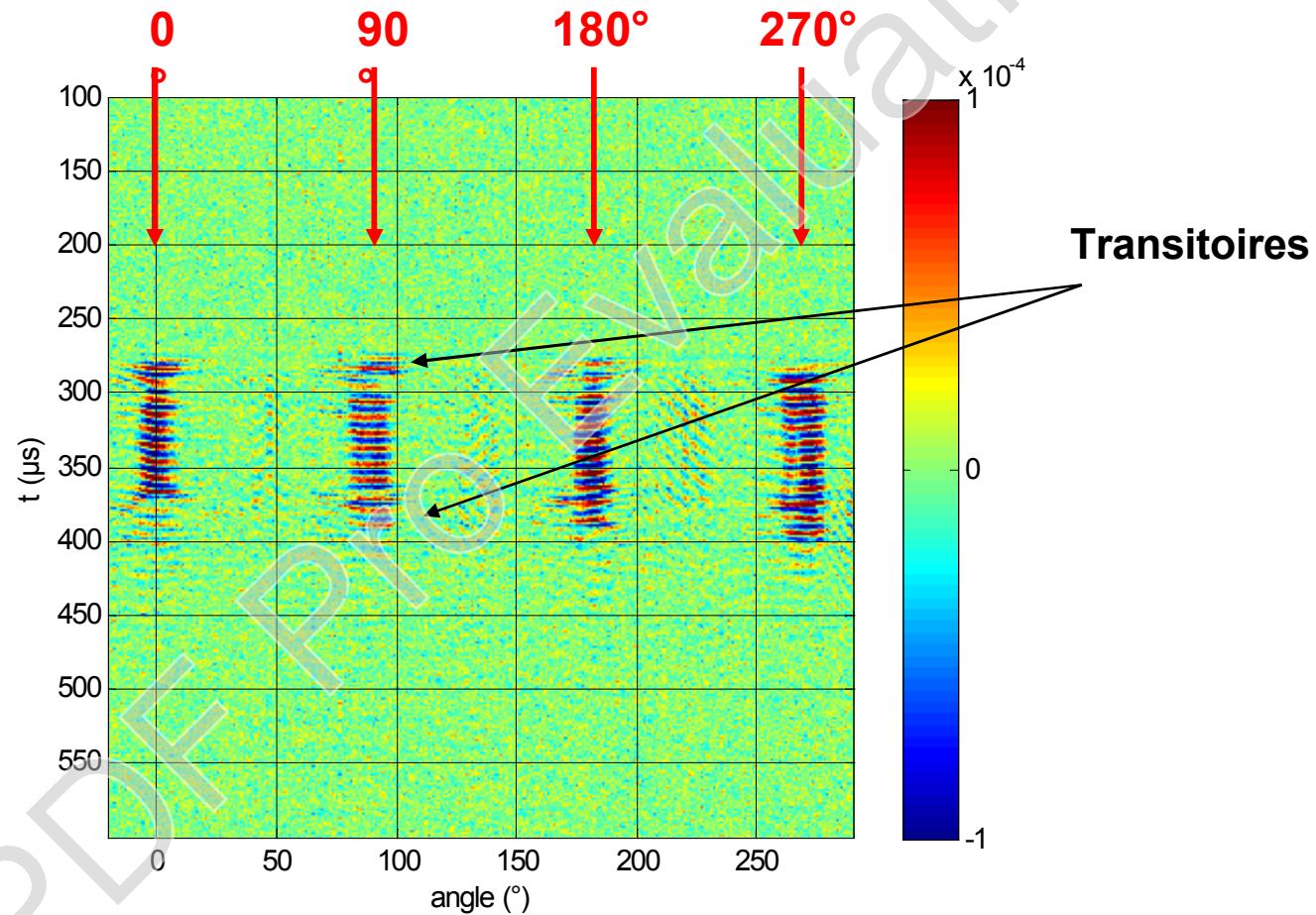
Le pinducer et le transducteur récepteur sont fixes, seul le CP tourne autour de son axe.

Signal d'excitation : train d'ondes de 50 périodes d'amplitude 50V et de fréquence 590kHz



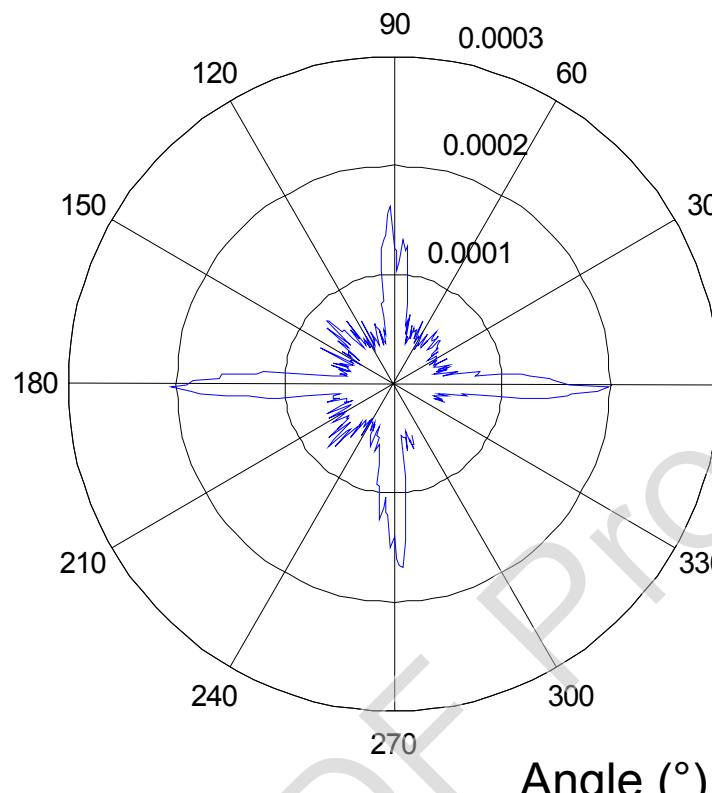
Square array of steel cylinders  
embedded in an epoxy matrix.

Signaux temporels en fonction de  
l'angle de rotation du CP



## Square array of steel cylinders embedded in an epoxy matrix.

Amplitude en fonction de l'angle de rotation du CP  
(dans le train d'onde (régime établi) entre 320 et 350 $\mu$ s)



JOURNAL OF APPLIED PHYSICS 116, 214901 (2014)



**Ultra-directional source of longitudinal acoustic waves based on a two-dimensional solid/solid phononic crystal**

B. Morvan,<sup>1</sup> A. Tinti,<sup>1</sup> J. O. Vasseur,<sup>2</sup> R. Sainidou,<sup>1</sup> P. Rembert,<sup>1</sup> A.-C. Hladky-Hennion,<sup>2</sup>

N. Swinteck,<sup>3</sup> and P. A. Deymier<sup>1</sup>  
<sup>1</sup>Laboratoire Ondes et Milieux Complexes, UMR CNRS 6294, Université du Havre, 75 rue Bellot, 76058 Le Havre, France

<sup>2</sup>Institut d'Électronique, de Micro-Électronique et de Nanotechnologie, UMR CNRS 8520, Cité Scientifique, 59652 Villeneuve d'Ascq Cedex, France

<sup>3</sup>Department of Materials Science and Engineering, University of Arizona, Tucson, Arizona 85721, USA

## Diagramme de directivité

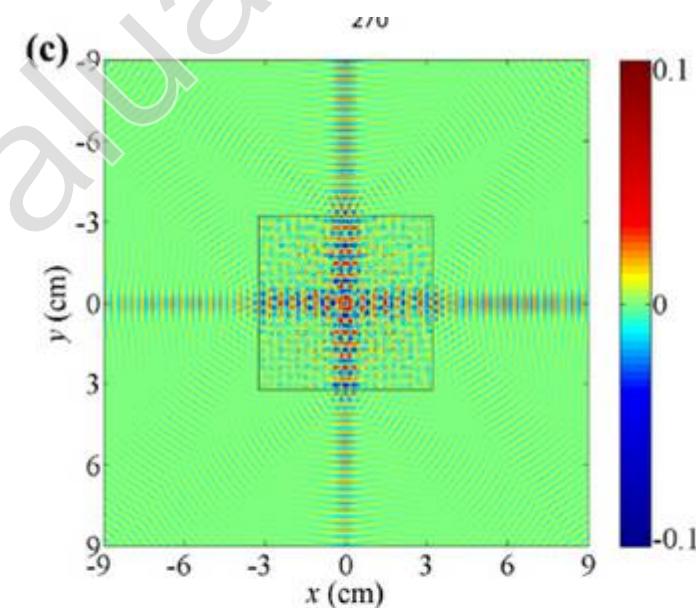
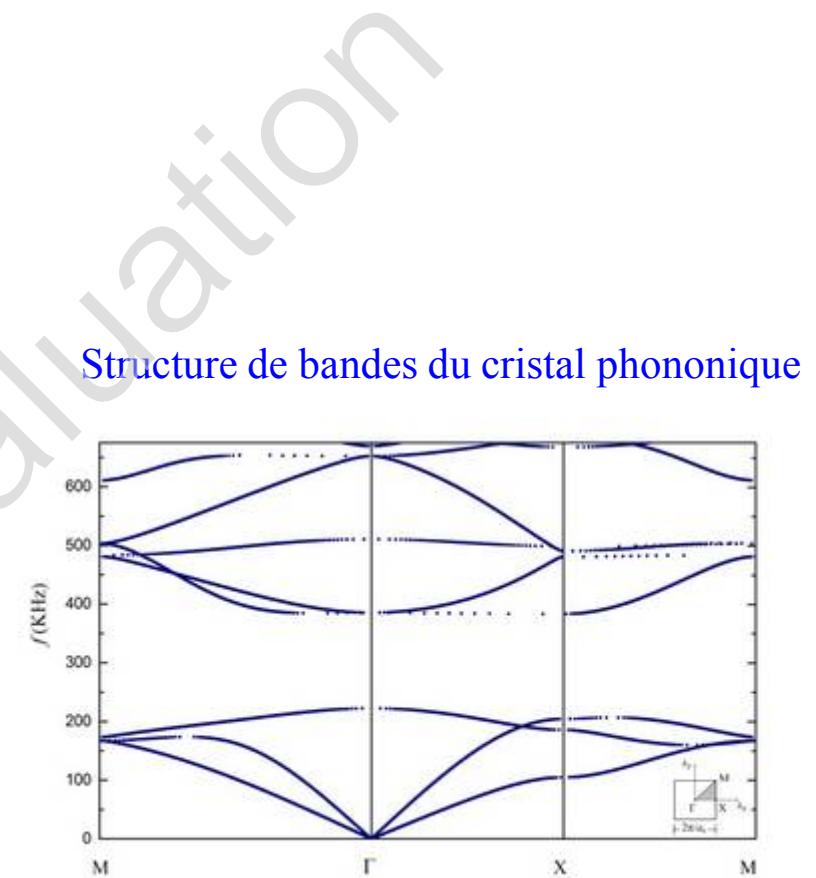
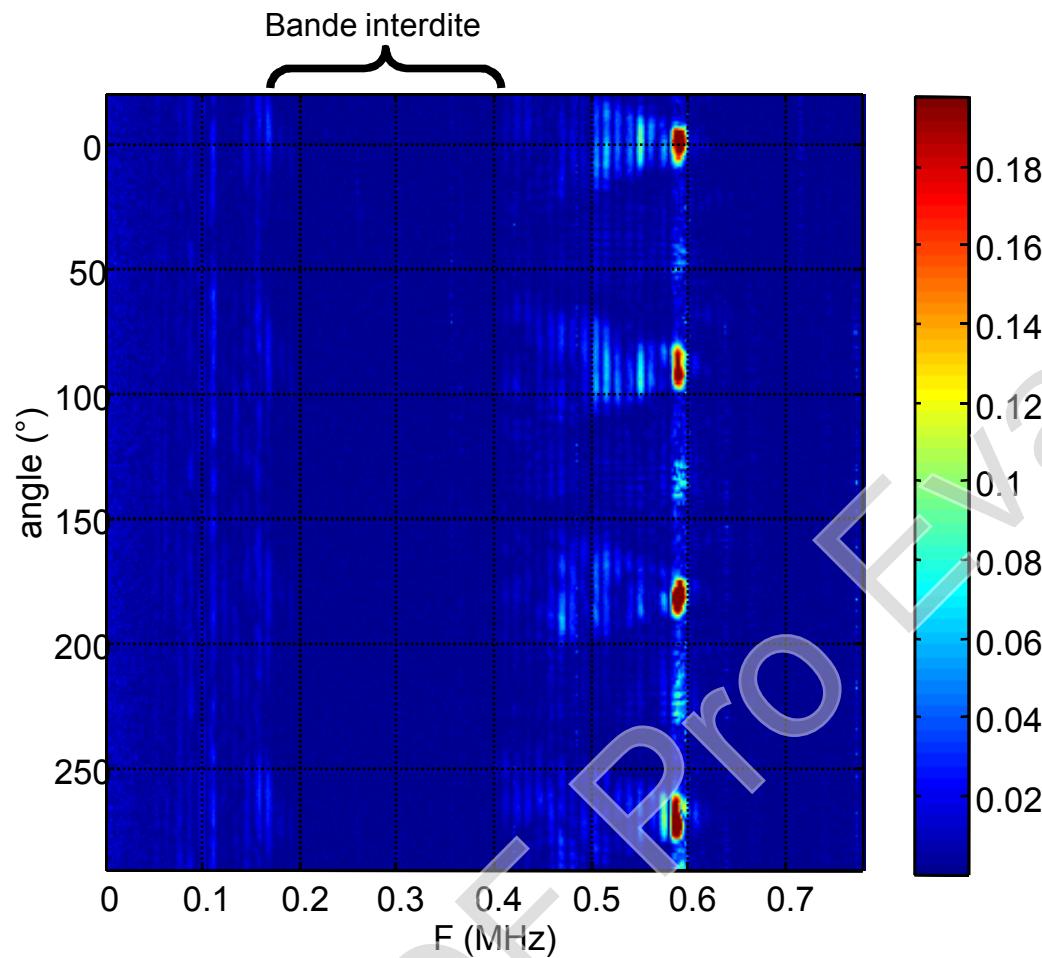


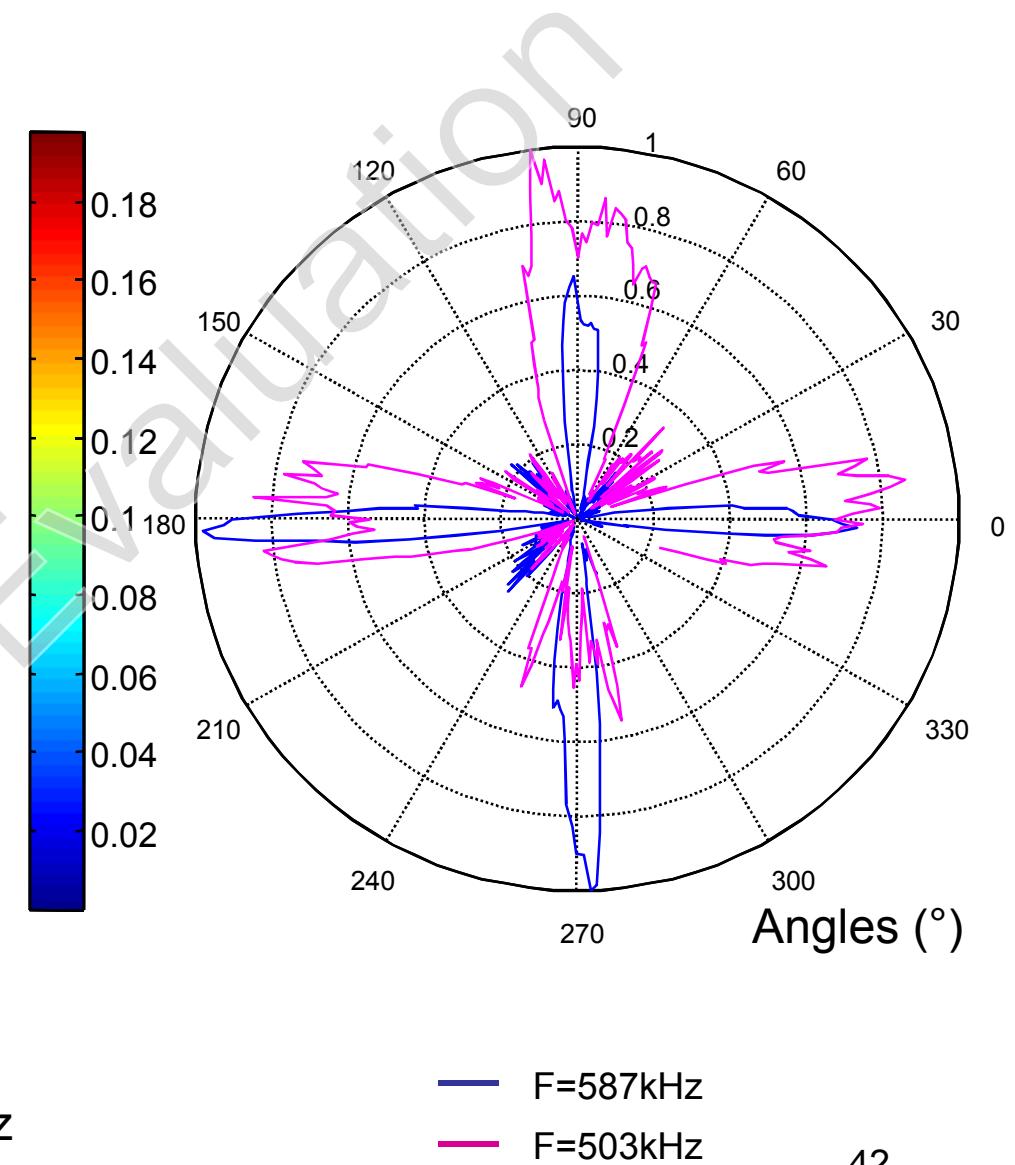
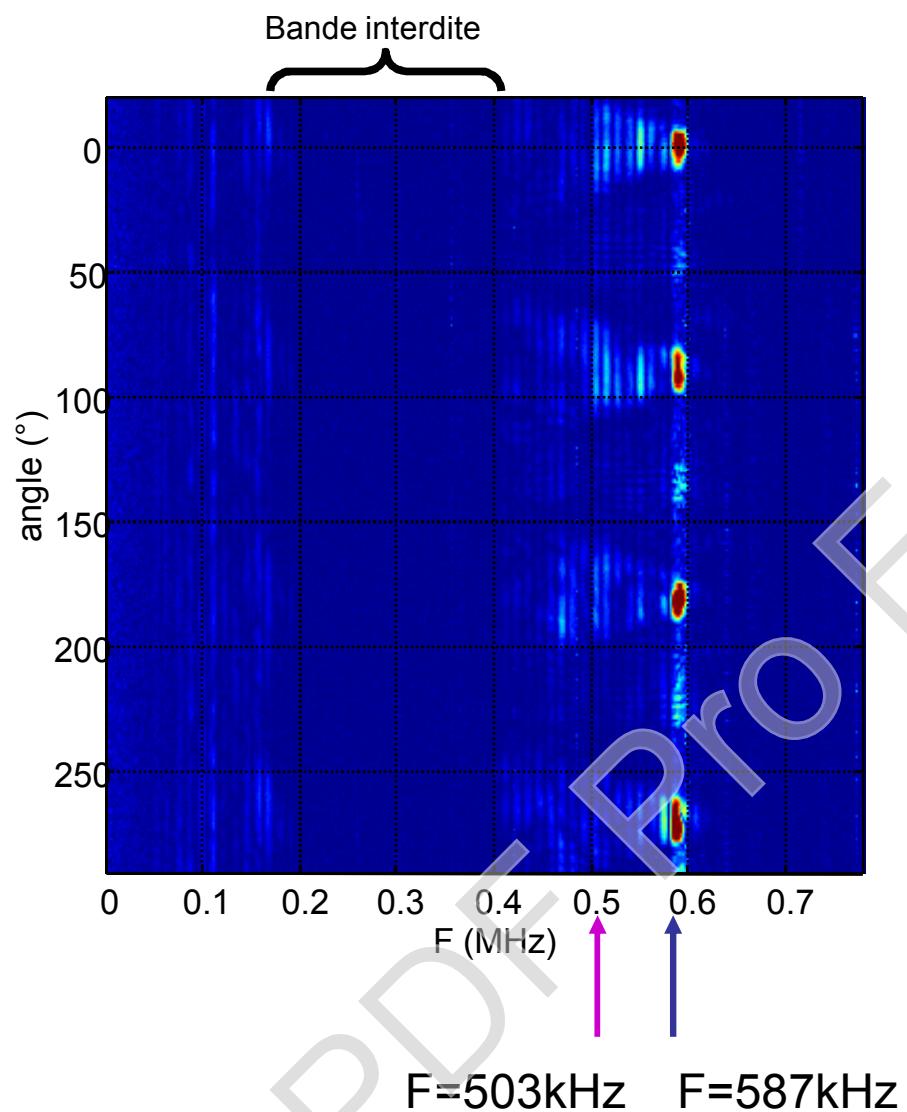
FIG. 4. Experimental maximum-amplitude (in arbitrary units) angular plot of signal received from the pinducer (a) immersed in water, (b) embedded in the PC block and immersed in water, and (c) pressure field (in arbitrary units) calculated using the FDTD method for case (b).

Simulation FDTD (N. Swinteck)  
40

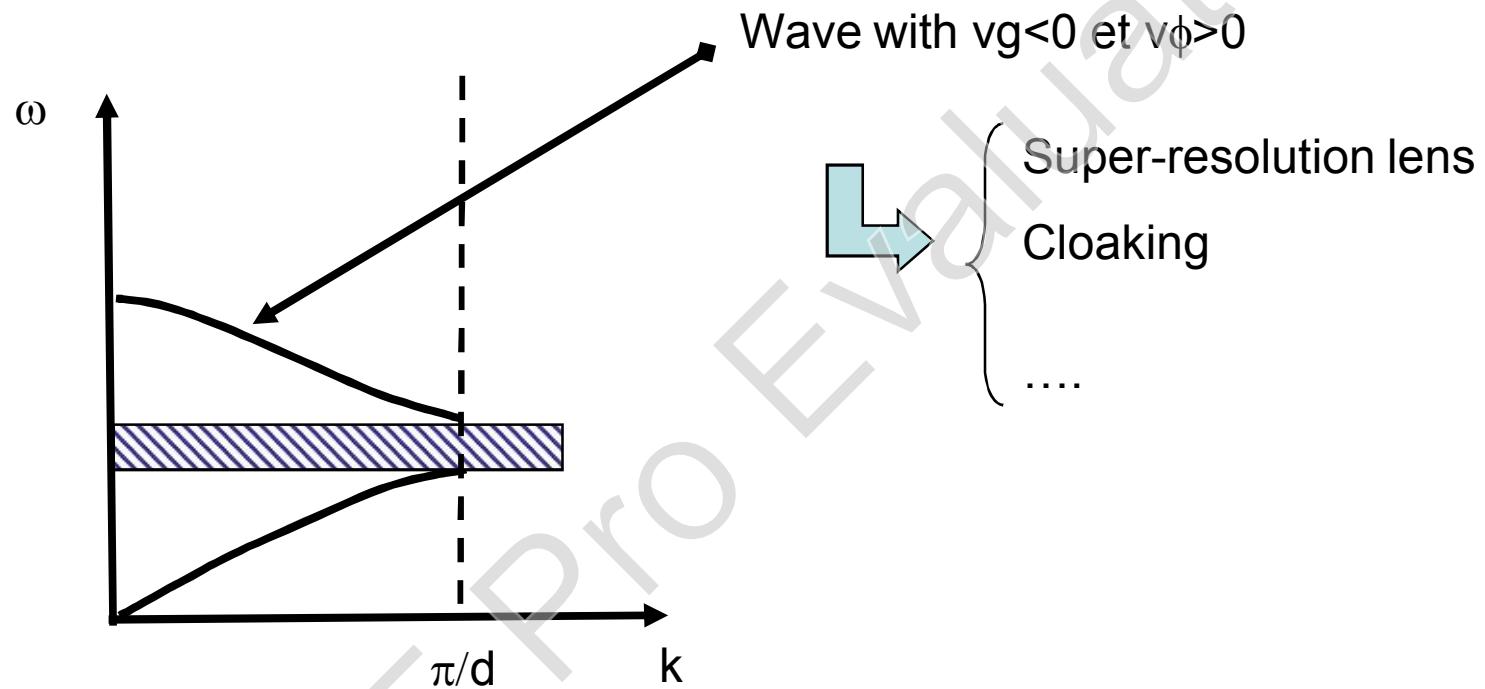
## Spectres en fonction de l'angle de réception.



## Spectres en fonction de l'angle de réception.



## PART 2 : Experimental demonstration of the negative refraction in a solid PC



# Negative refraction

Point de départ de cette étude .....

Proposition de Veselago en 1968 dans son article :

*“The electrodynamics of substances with simultaneously negative values of  $\epsilon$  and  $\mu$ ”, Soviet Physics Uspekhi, vol. 10, No 4 (1968).*

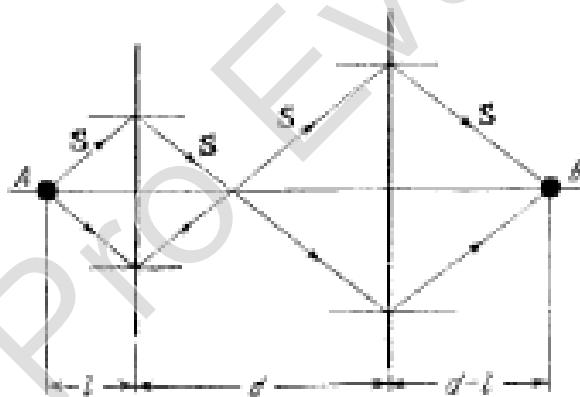
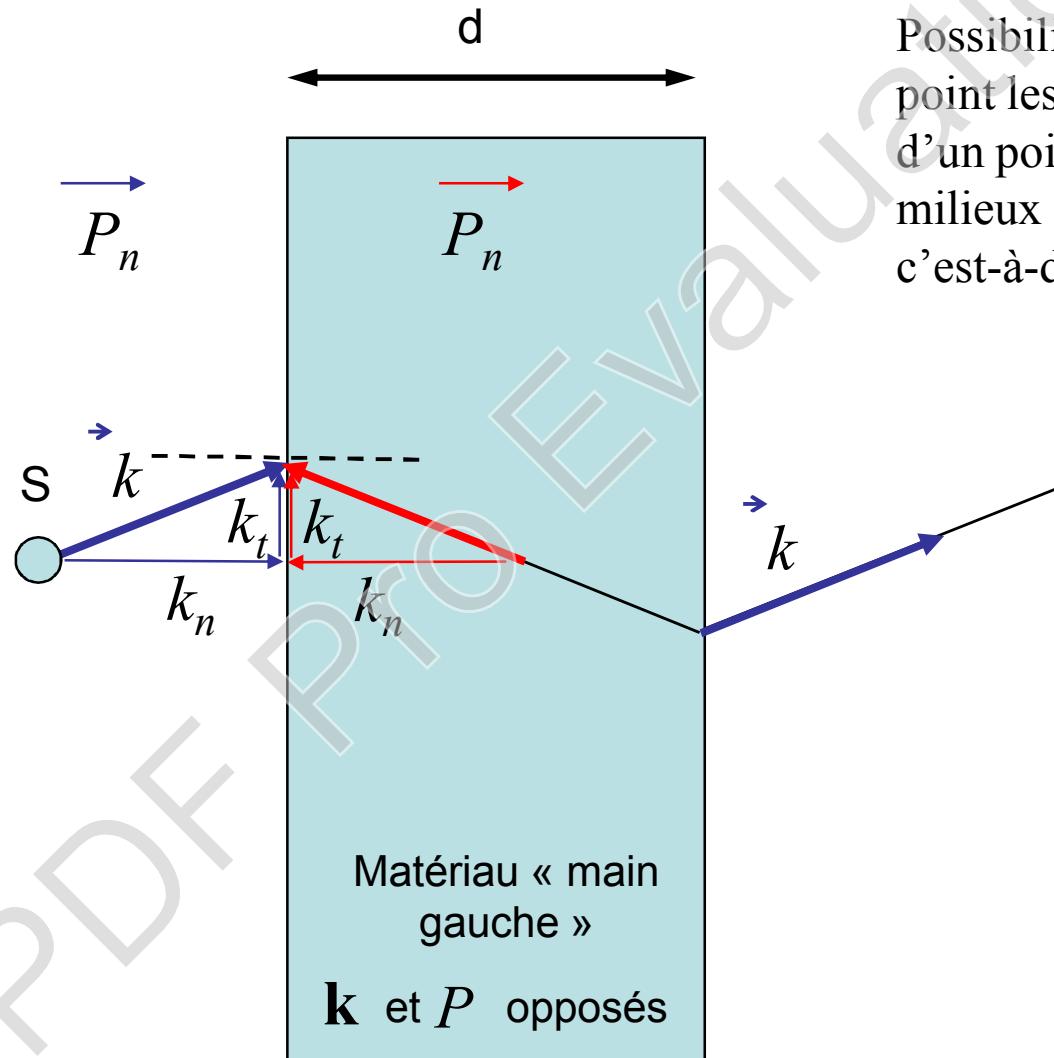


FIG. 4. Passage of rays of light through a plate of thickness  $d$  made of a left-handed substance. A = source of radiation; B = detector of radiation.

# Negative refraction

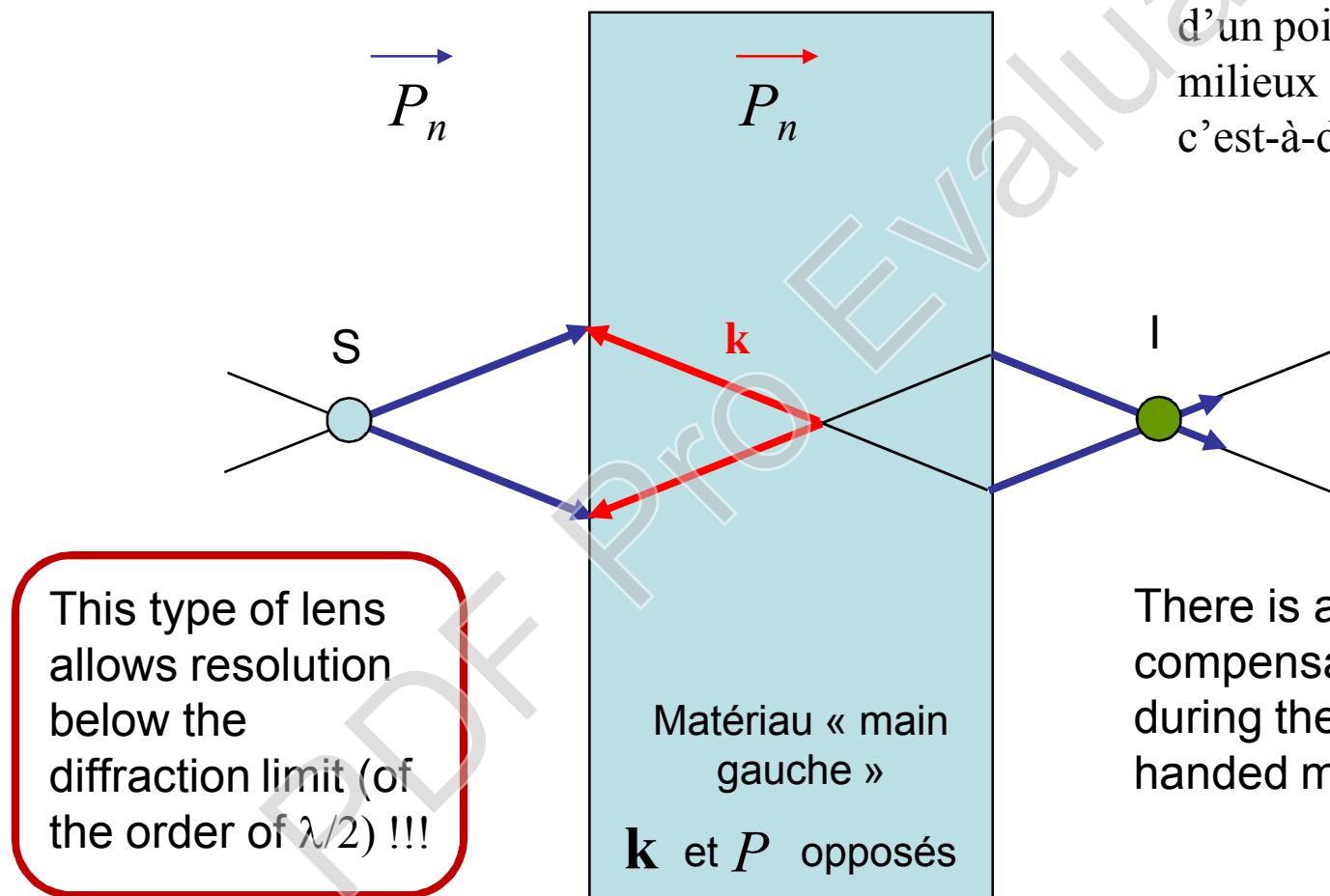
## Lentille super-résolution : principe



Possibilité de focaliser en un point les radiations issues d'un point source grâce à des milieux tels que  $e = -1$  et  $m = -1$  c'est-à-dire  $n = -1$

# Negative refraction

## Lentille super-résolution : principe

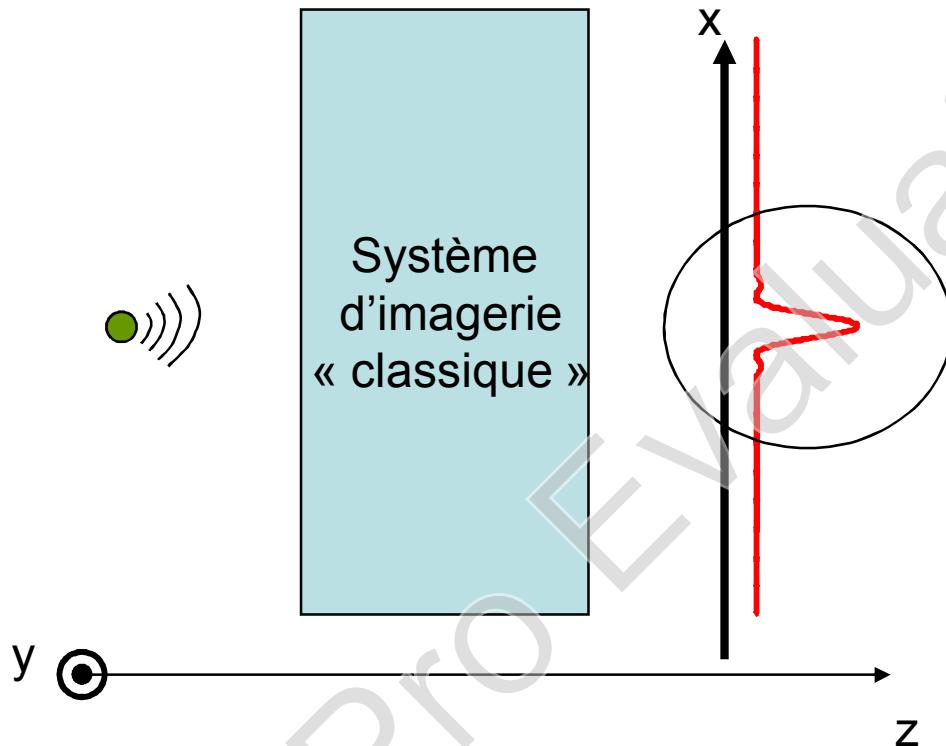


Possibilité de focaliser en un point les radiations issues d'un point source grâce à des milieux tels que  $\epsilon = -1$  et  $\mu = -1$  c'est-à-dire  $n = -1$

There is an exact compensation of the phase during the path in the left handed material

## Negative refraction

Origin of the limit  $\lambda/2$  in the resolution of the image



Impose une limite  $k_{\max} = \frac{\omega}{c}$

et donc une limitation de la résolution spatiale du système d'imagerie :

$$\Delta k_{\max} \cdot \Delta x = 2\pi \quad \rightarrow \quad \Delta x \approx \lambda$$

Un point source donnera une « tache » image de largeur nécessairement supérieure à  $\lambda$

L'image de la source est formée à partir composantes propagatives du champ dans la direction z c'est-à-dire telles que :

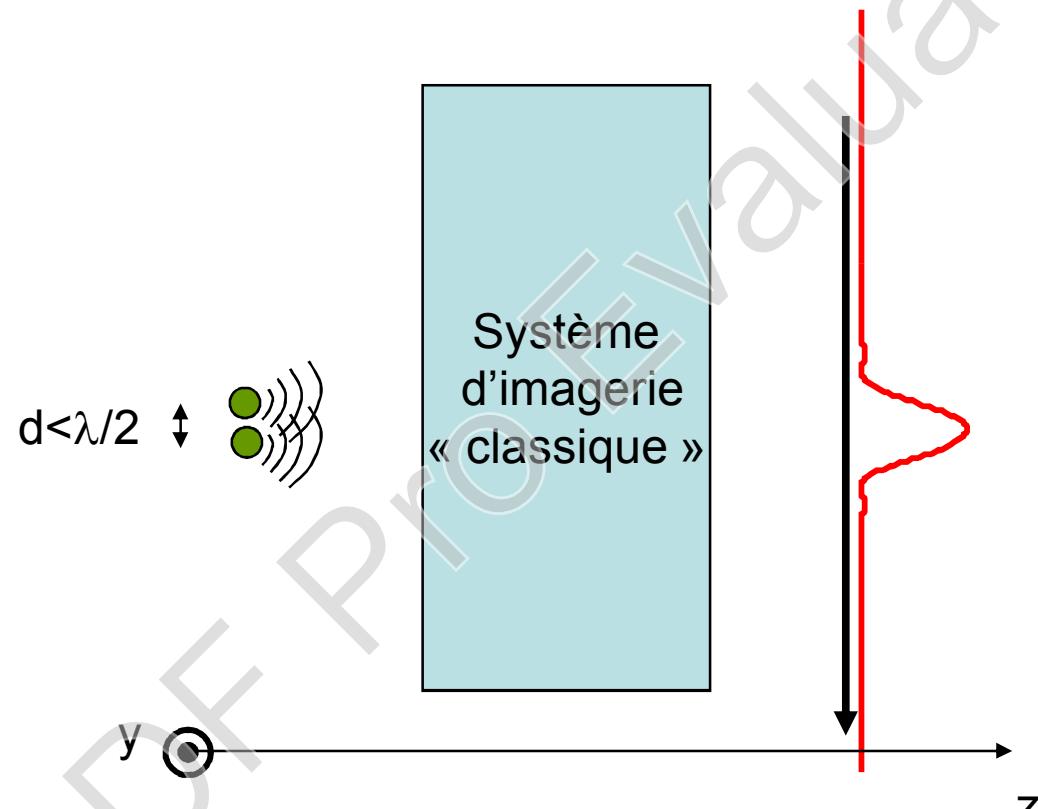
$$k_z = \sqrt{\frac{\omega^2}{c^2} - k_x^2}$$
$$k_x^2 < \frac{\omega^2}{c^2}$$

## Negative refraction

Lentille super-résolution : principe

Limite « classique » de résolution d'image

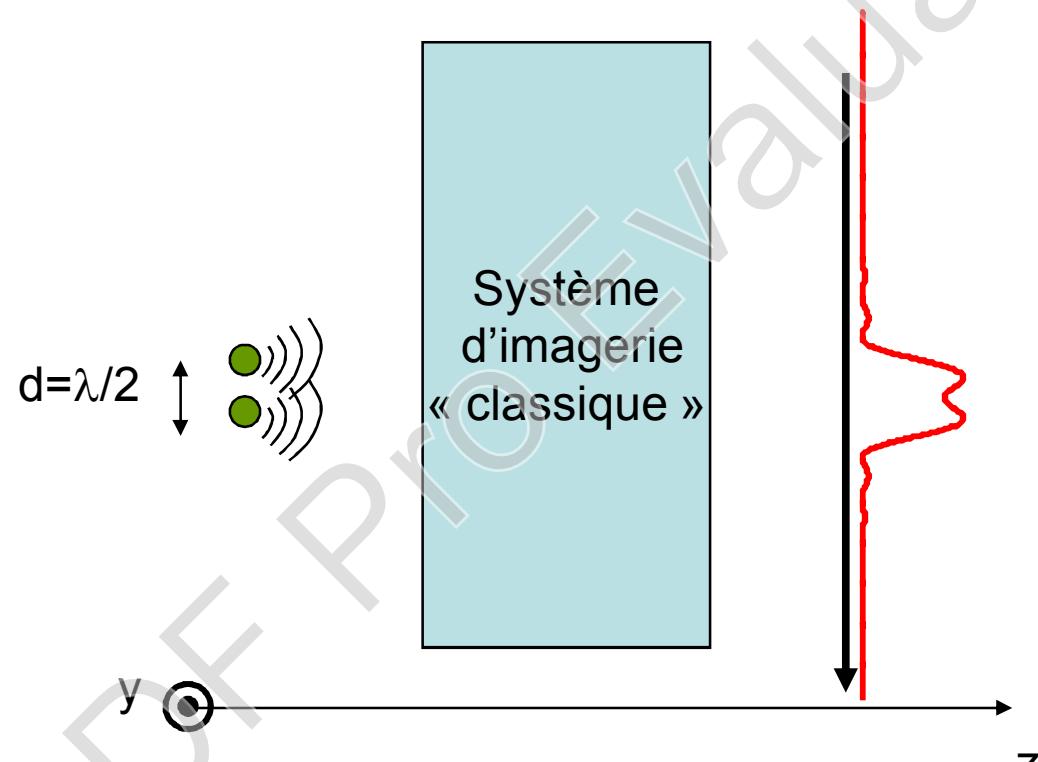
Critère de Rayleigh indique que la résolution D ne peut être meilleure que  $\lambda/2$ .



## Negative refraction

Lentille super-résolution : principe  
Limite « classique » de résolution d'image

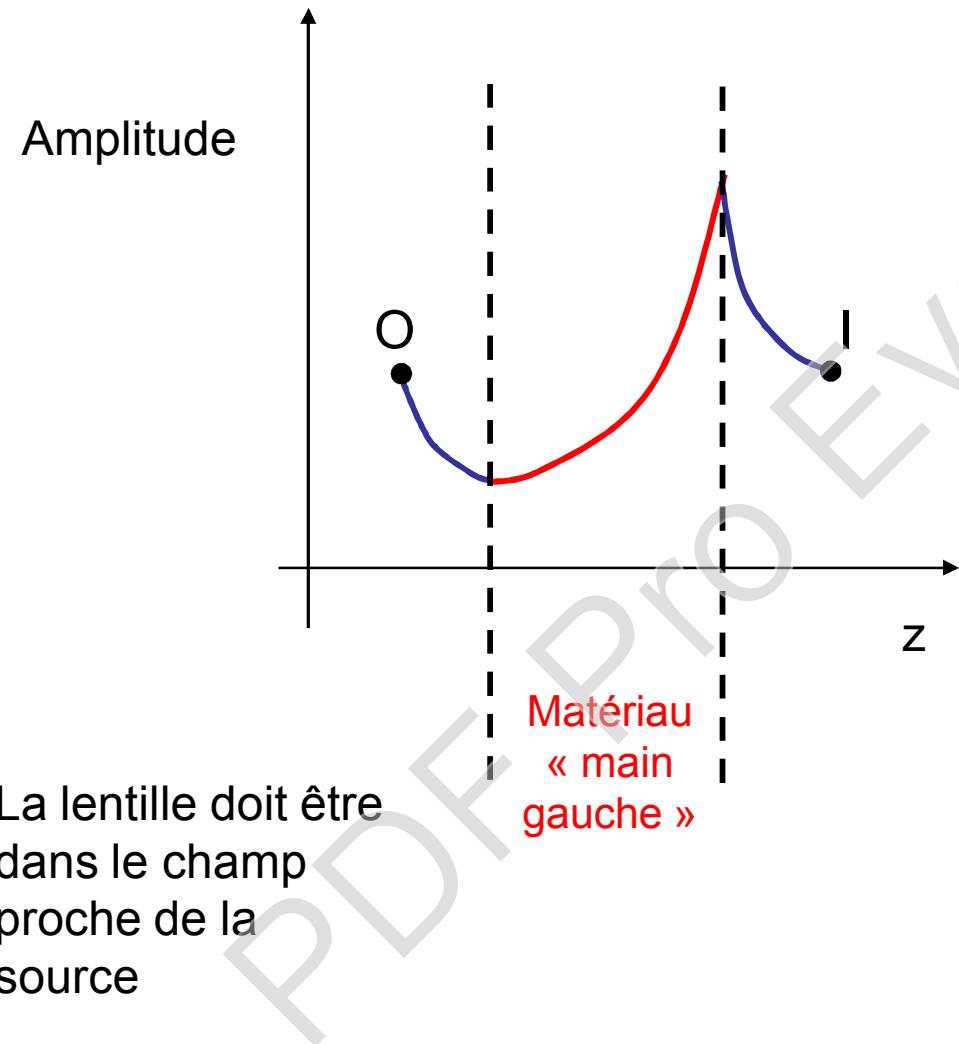
Critère de Rayleigh indique que la résolution D ne peut être meilleure que  $\lambda/2$ .



## Negative refraction

Super resolution lens : principe

J. B. Pendry (*Phys. Rev. Lett.*, 2000) reprend l'idée et montre que la lentille à réfraction négative permet de focaliser également les ondes « évanescentes » .



Compensation des phases mais aussi des amplitudes entre le point source et le point image

L'onde évanescante peut contribuer à la construction de l'image

Résolution meilleure que  $\lambda/2$

## Negative refraction

« Left handed » acoustic media ?

- L'équivalent acoustique du matériau « main gauche » proposé en électromagnétisme est obtenu pour  $\rho_0 < 0$  et  $\chi_s < 0$ .

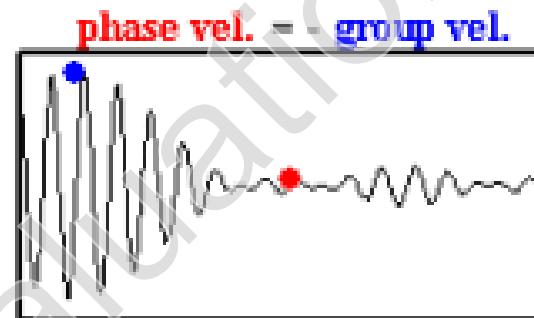
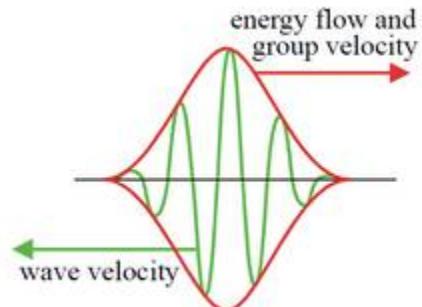
*J. Li and C.T. Chan (Phys. Rev. E 70, 2004)*

- Le vecteur d'onde et vecteur de Poynting pointent alors dans des directions opposées

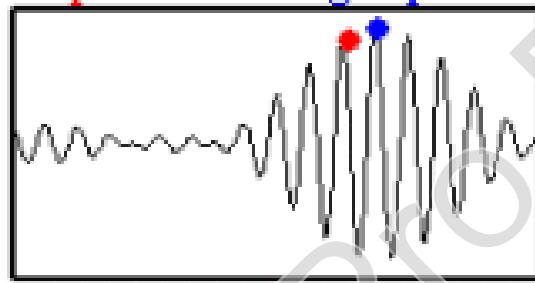
Pour une onde plane harmonique  $e^{+j(kz-\omega t)}$

Équation d'Euler  $p \cdot k = \rho_0 \omega v \rightarrow p v \cdot k = \rho_0 \omega |v|^2 < 0$

## Negative refraction



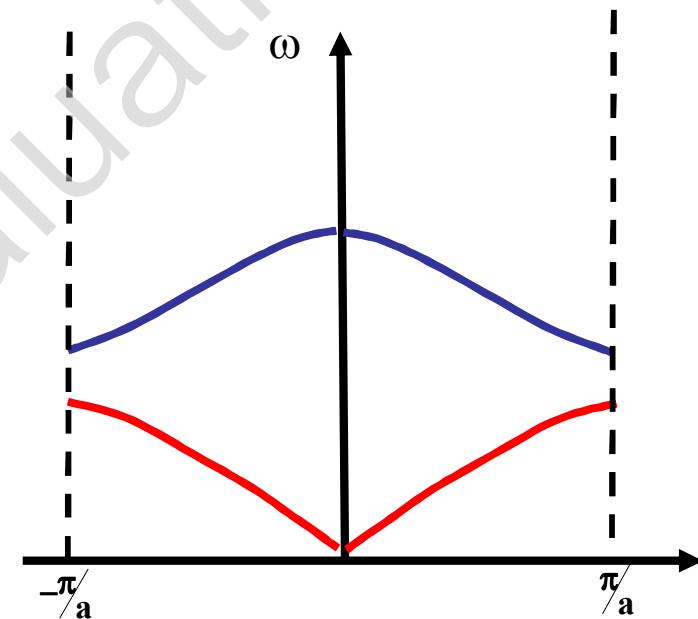
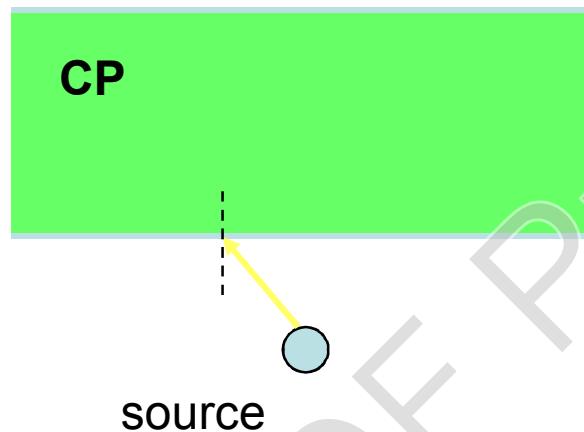
phase vel. > group vel.



Une onde pour laquelle la vitesse de phase est opposée à la vitesse de groupe

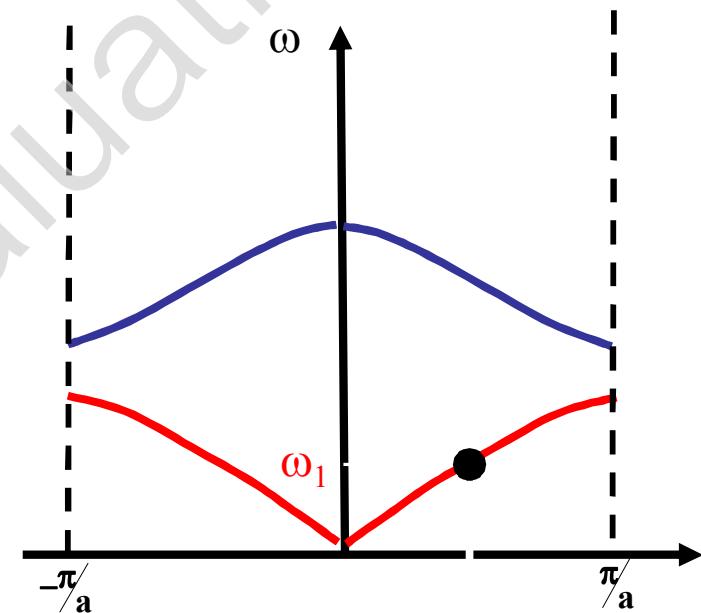
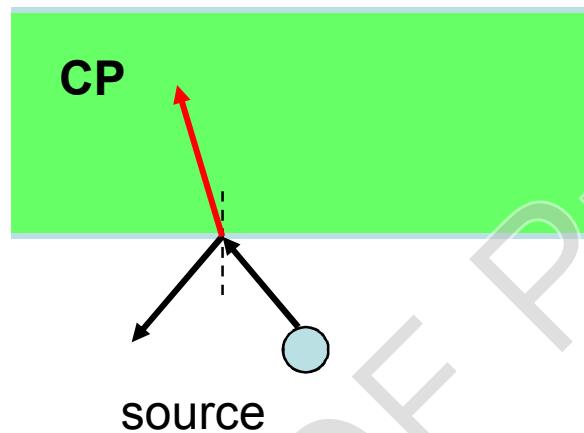
## **Réfraction négative et lentille super résolution**

ANR « SUPREME » : SUPperlentille à REfraction négative à base de MEtamériaux et cristaux phononiques, ANR-08-BLAN-0101-01



## **Réfraction négative et lentille super résolution**

ANR « SUPREME » : SUPperlentille à REfraction négative à base de MEtamériaux et cristaux phononiques, ANR-08-BLAN-0101-01

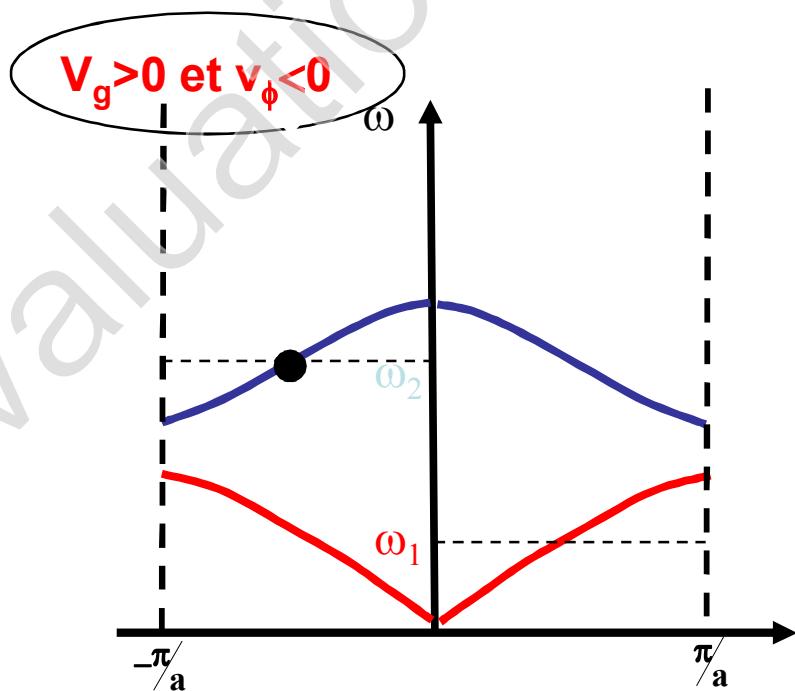
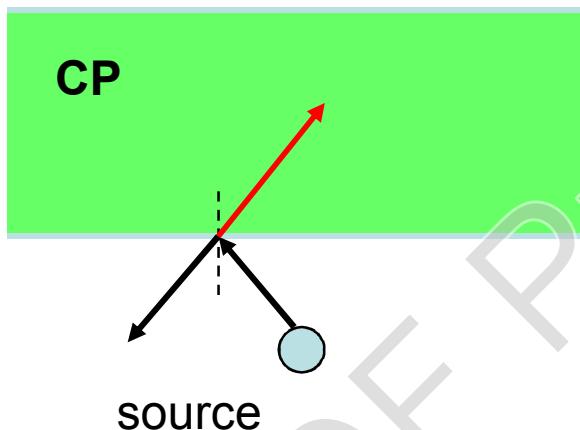


$$V_g > 0 \text{ et } v_\phi > 0$$

## Réfraction négative et lentille super résolution

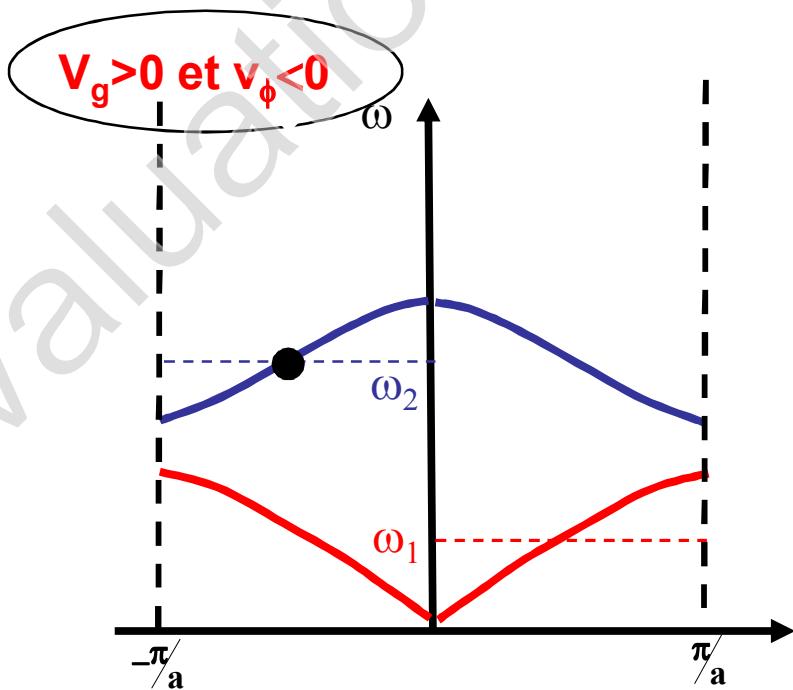
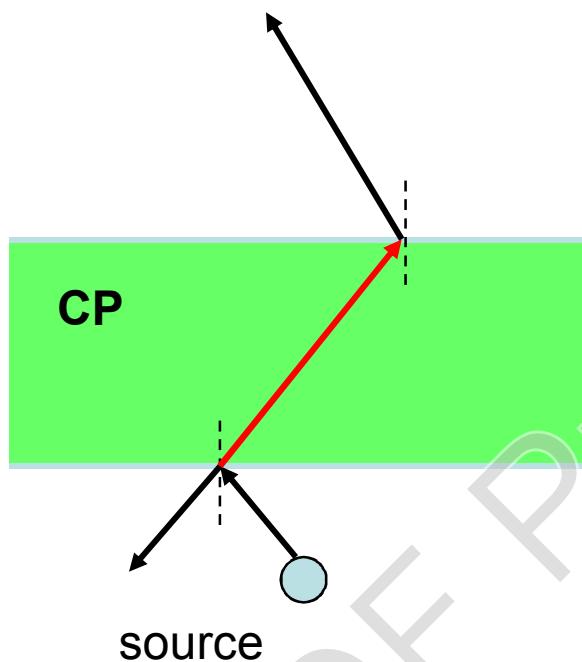
ANR « SUPREME » : SUPperlentille à REfraction négative à base de MEtamériaux et cristaux phononiques, ANR-08-BLAN-0101-01

- Ondes à vitesses de groupe et de phase opposées : conséquence sur les lois de la réfraction.



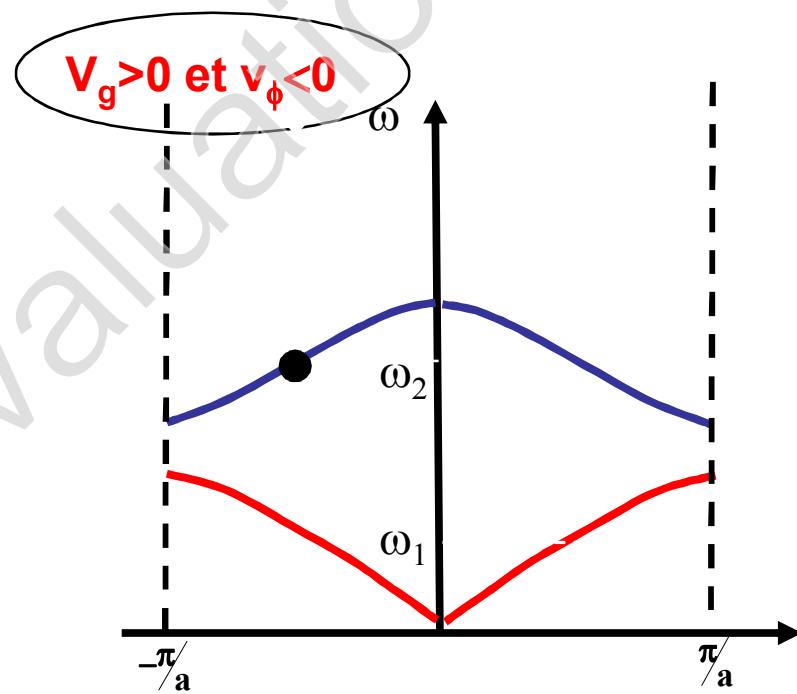
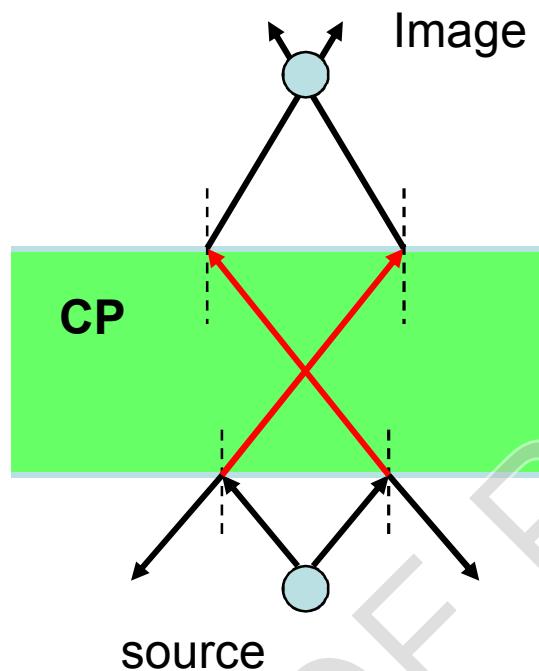
## **Réfraction négative et lentille super résolution**

ANR « SUPREME » : SUPperlentille à REfraction négative à base de MEtamériaux et cristaux phononiques, ANR-08-BLAN-0101-01



## **Réfraction négative et lentille super résolution**

ANR « SUPREME » : SUPperlentille à REfraction négative à base de MEtamériaux et cristaux phononiques, ANR-08-BLAN-0101-01



# Réfraction négative et lentille super résolution

ANR « SUPREME » : SUPperlentille à REfraction négative à base de MEtamériaux et cristaux phononiques, ANR-08-BLAN-0101-01

PHYSICAL REVIEW B 77, 014301 (2008)

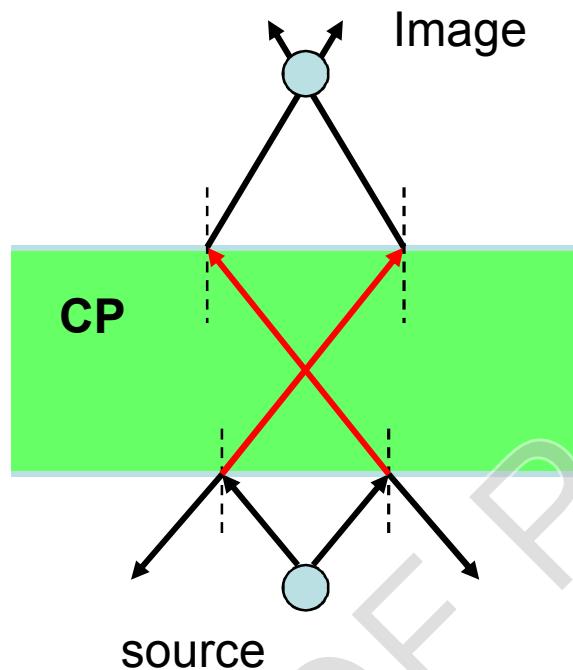
Negative refraction and focusing of ultrasound in two-dimensional phononic crystals

Alexey Sukhovich,<sup>1</sup> Li Jing,<sup>2</sup> and John H. Page<sup>1</sup>

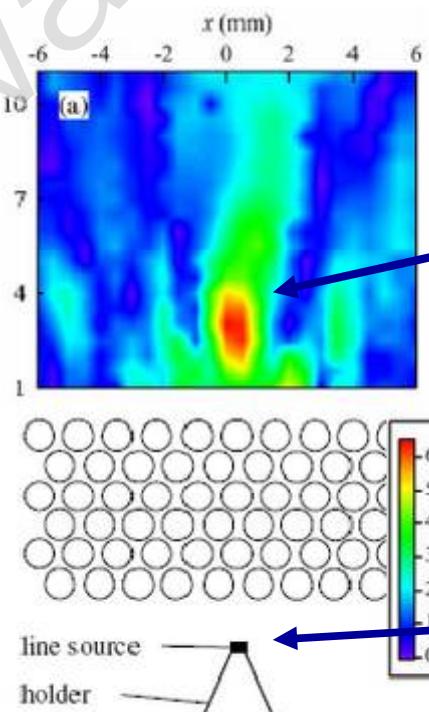
<sup>1</sup>Department of Physics and Astronomy, University of Manitoba, Winnipeg, Manitoba, Canada R3T 2N2

<sup>2</sup>Department of Physics, Wuhan University, Wuhan 430072, People's Republic of China

(Received 30 August 2007; published 16 January 2008)



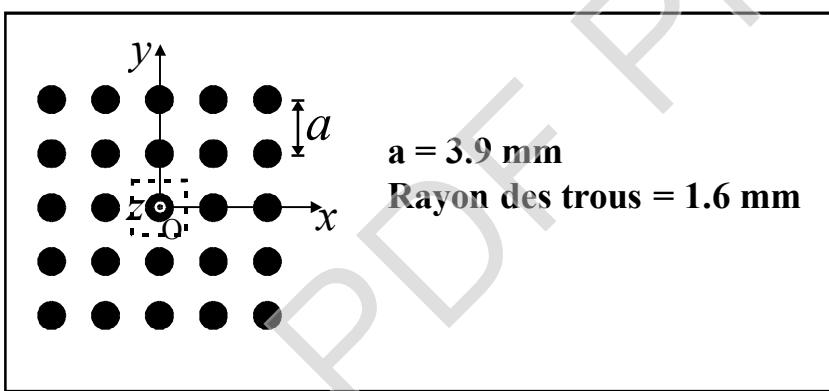
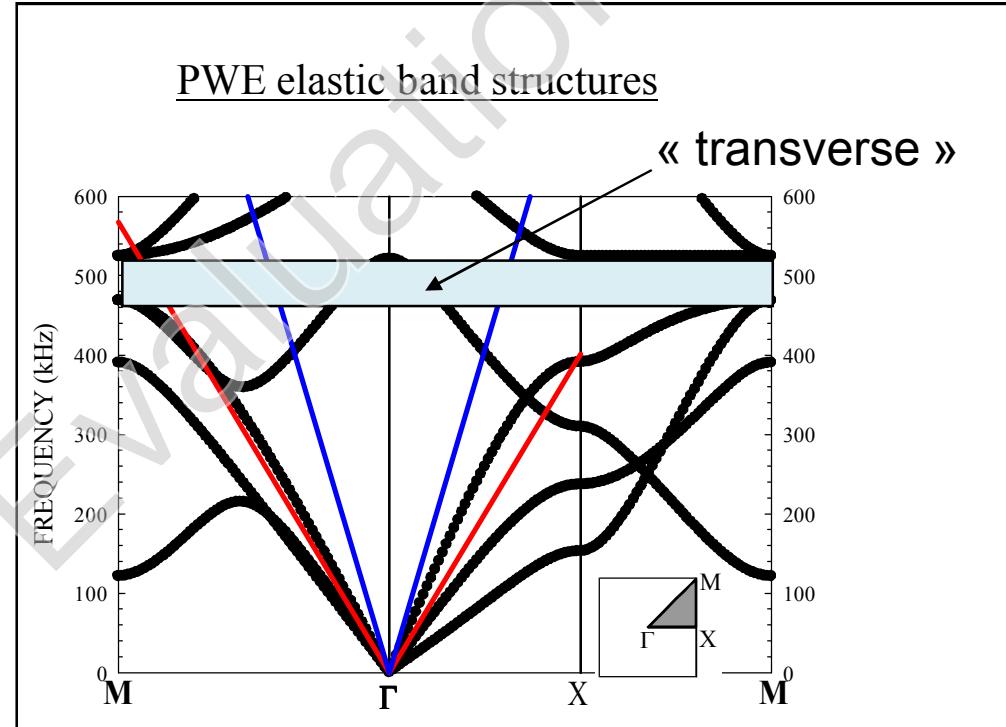
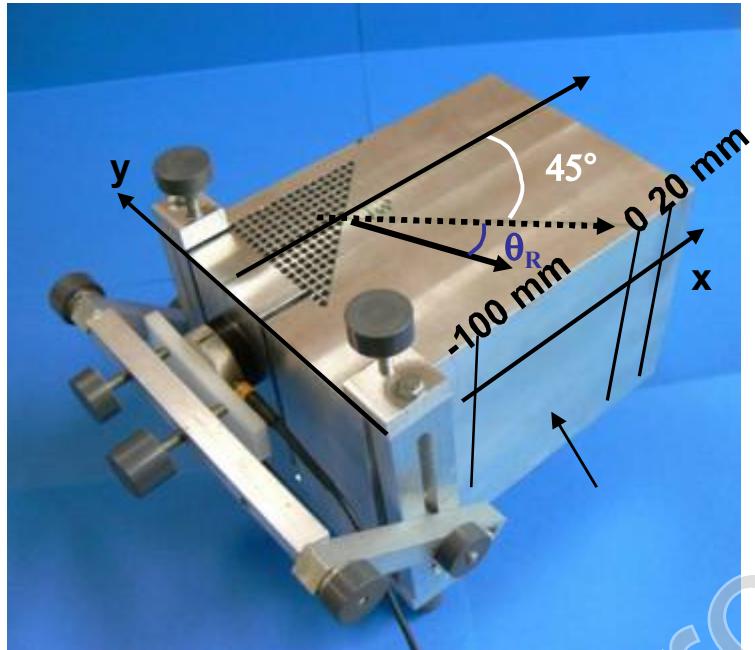
Ce type de lentille autorise des résolutions inférieures à la limite de diffraction (de l'ordre de  $\lambda/2$ ) !!!



Au-delà du cristal phononique, on retrouve l'image de la source avec une résolution de  $0.5\lambda$ .

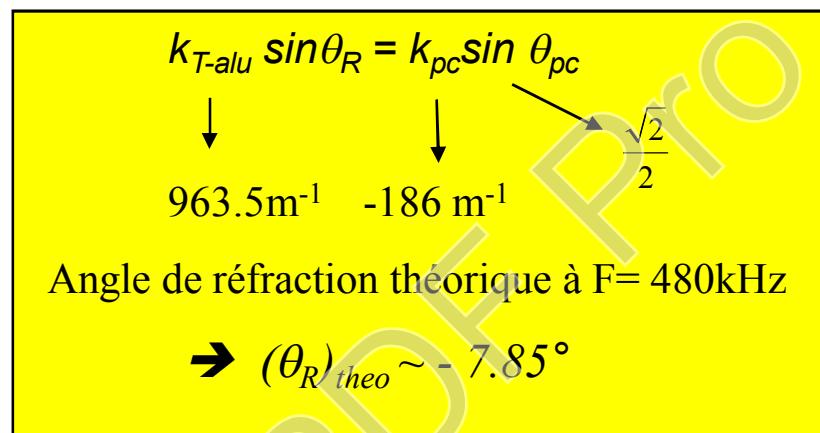
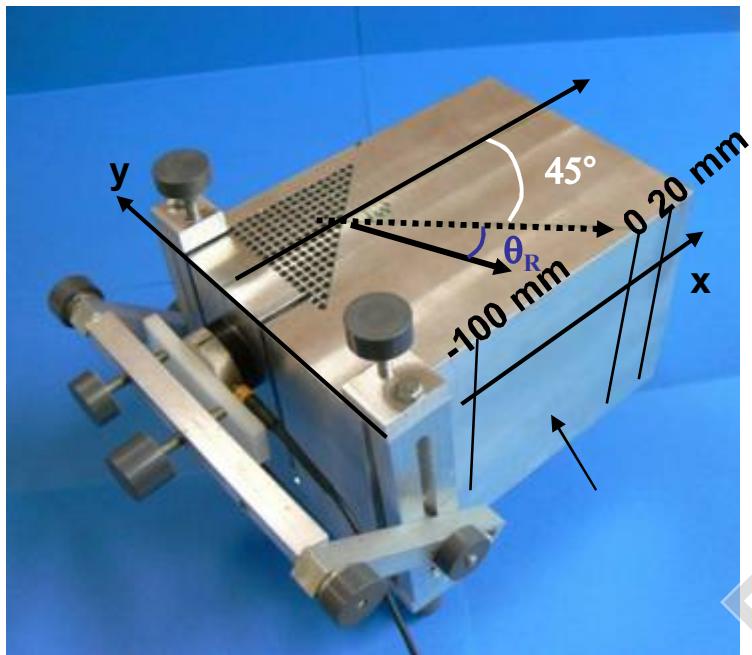
Source linéaire de fréquence 0.55MHz

## Réfraction négative d'une onde transversale

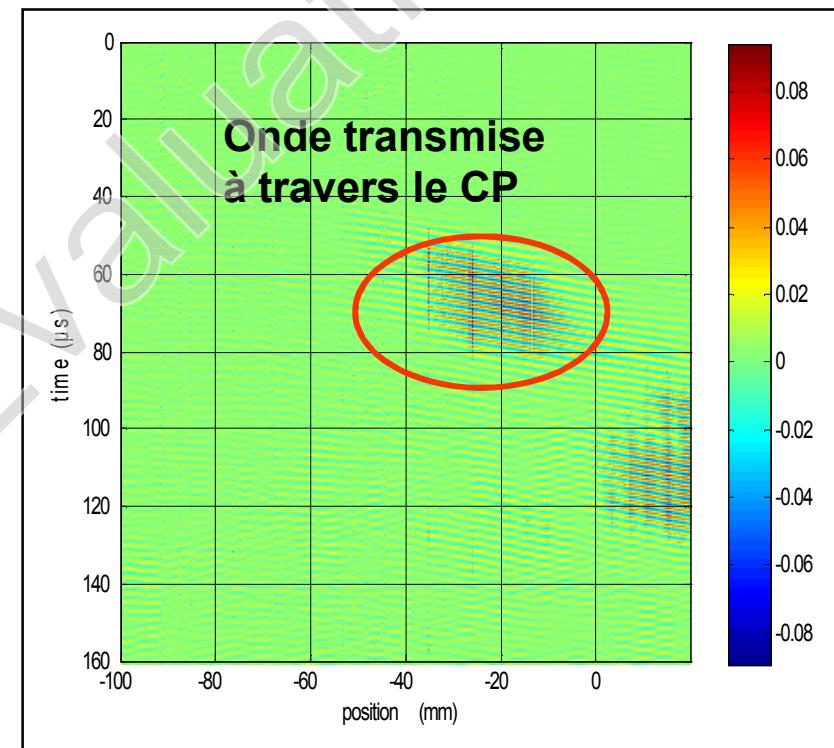


Objectif : étudier le phénomène de réfraction négative dans un milieu solide.

## Réfraction négative d'une onde transversale



Un vibromètre laser Polytec® (VD09) est utilisé pour mesurer les déplacements normaux en surface le long de l'axe x. L'échantillon est traduit par pas de 0.2 mm



Angle de réfraction expérimental à  $F = 480 \text{ kHz}$

$\rightarrow (\theta_R)_{\text{exp}} \sim -5^\circ$

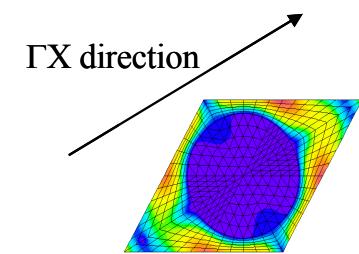
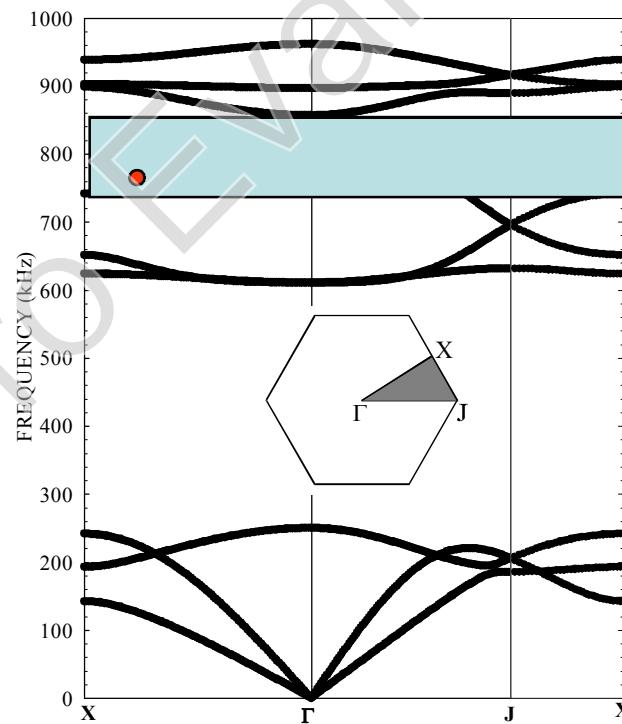
Dans le CP, très grandes longueurs d'onde (de l'ordre de 30mm) à comparer au paramètre de maille  $a=3.9 \text{ mm}$  !!!

## *Réfraction négative d'une onde longitudinale*



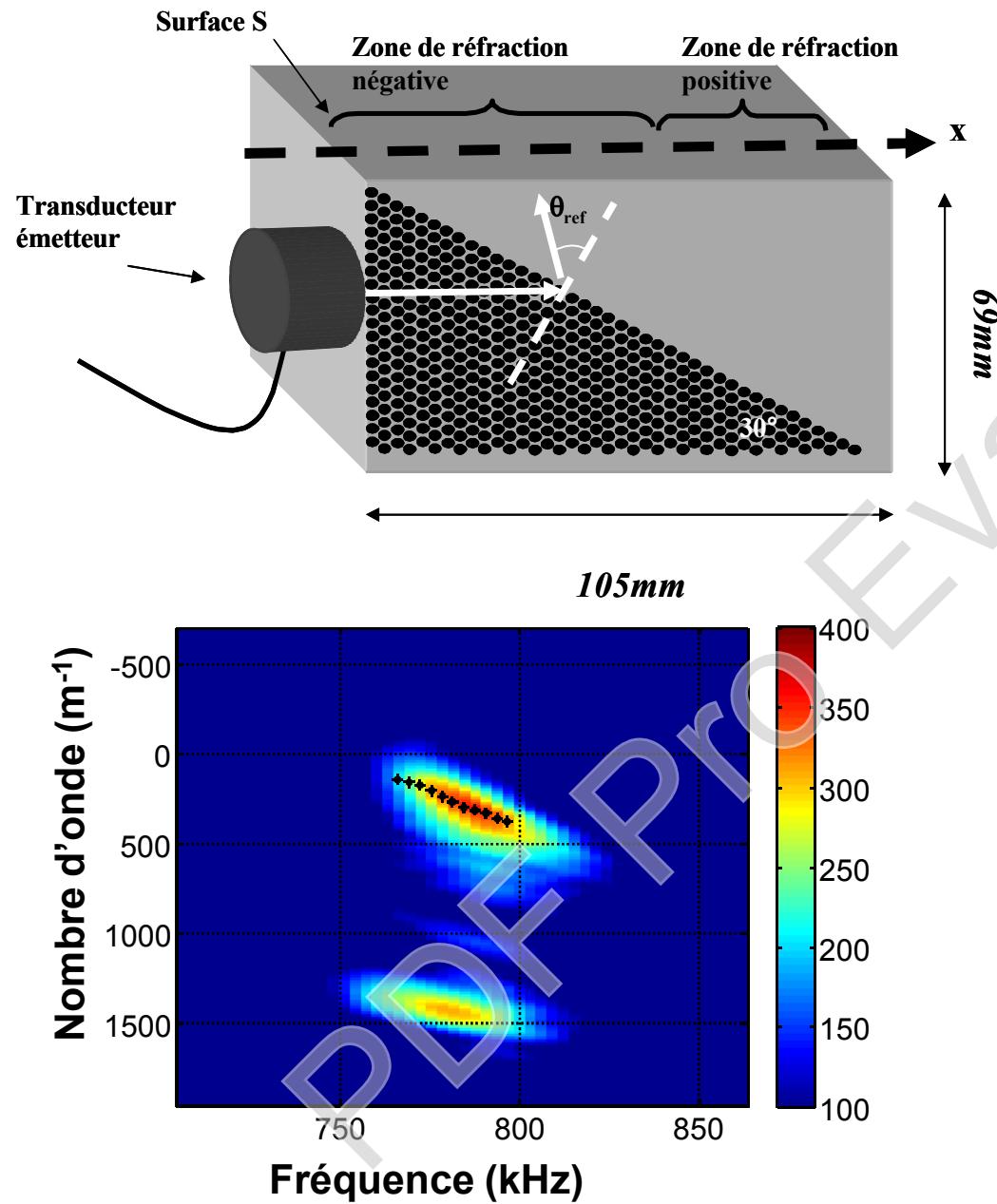
Résine époxy coulée dans le réseau de tiges d'acier inox (rayon 1mm)

Structure de bande du CP 2D.  
Réseau triangulaire ( $a=2.84\text{mm}$ )  
de cylindres d'acier dans une matrice époxy.

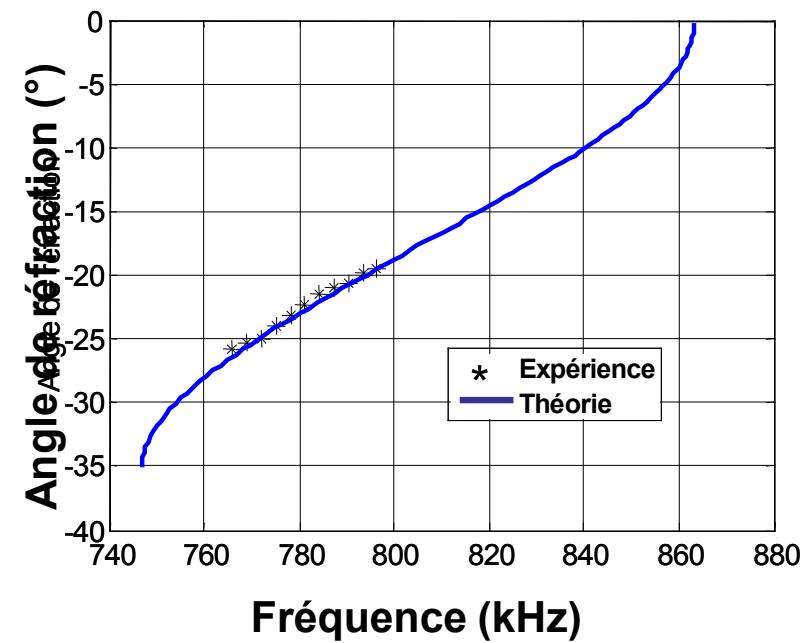


Champ de déplacement dans le CP pour  $k = 900 \text{ m}^{-1}$  et  $f = 780 \text{ kHz}$

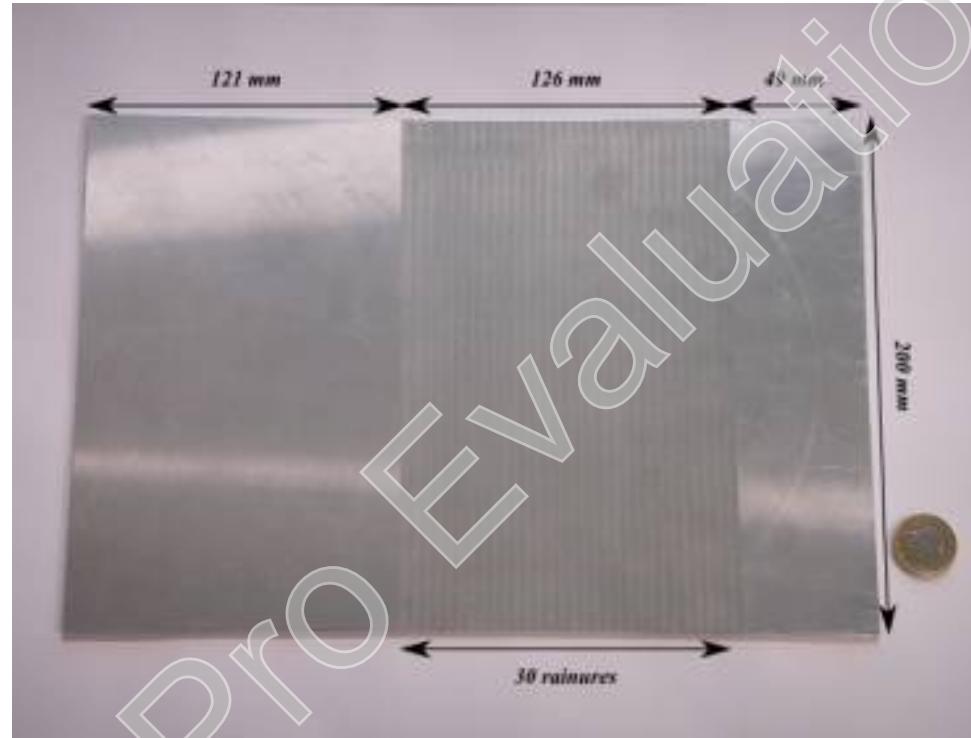
## Réfraction négative d'une onde longitudinale



Dans la bande de fréquence étudiée la plus grande longueur d'onde dans le CP est de l'ordre de 4mm, la distance parcourue dans le CP est donc de l'ordre de 10 longueurs d'onde.



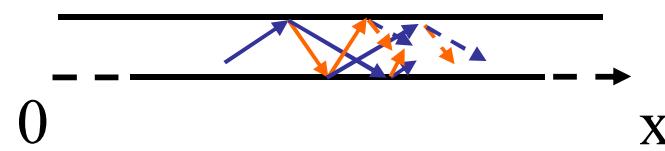
## Lamb waves with opposite group and phase velocities in a plate with periodic corrugation



- Laboratoire d'Acoustique de l'Université du Maine (LAUM UMR CNRS 6613).  
**Catherine Potel, Claude Depollier et Michel Bruneau**
- Institut d'Electronique, de Microélectronique et de Nanotechnologie, IEMN UMR CNRS 852.  
**Anne Christine Hladky, Bertrand Dubus, Jérôme Vasseur**

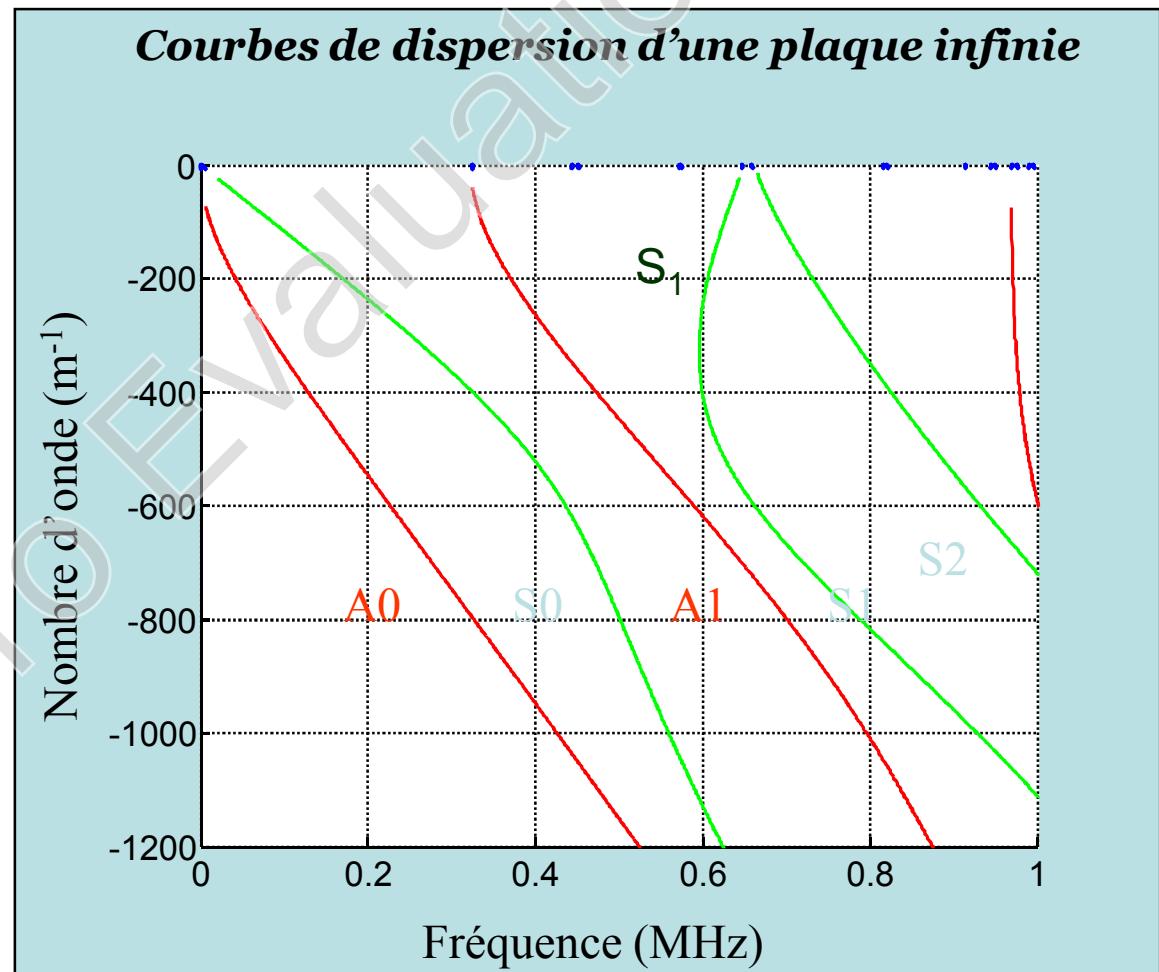
## Lamb waves with opposite $V_g$ and $V_\phi$

### Plaque infinie surfaces planes



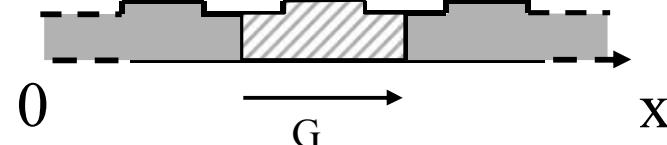
Epaisseur de la plaque  
 $E=5\text{mm}$

Couplage modal  
associé à l'ouverture  
d'une bande interdite  
Ondes de Lamb



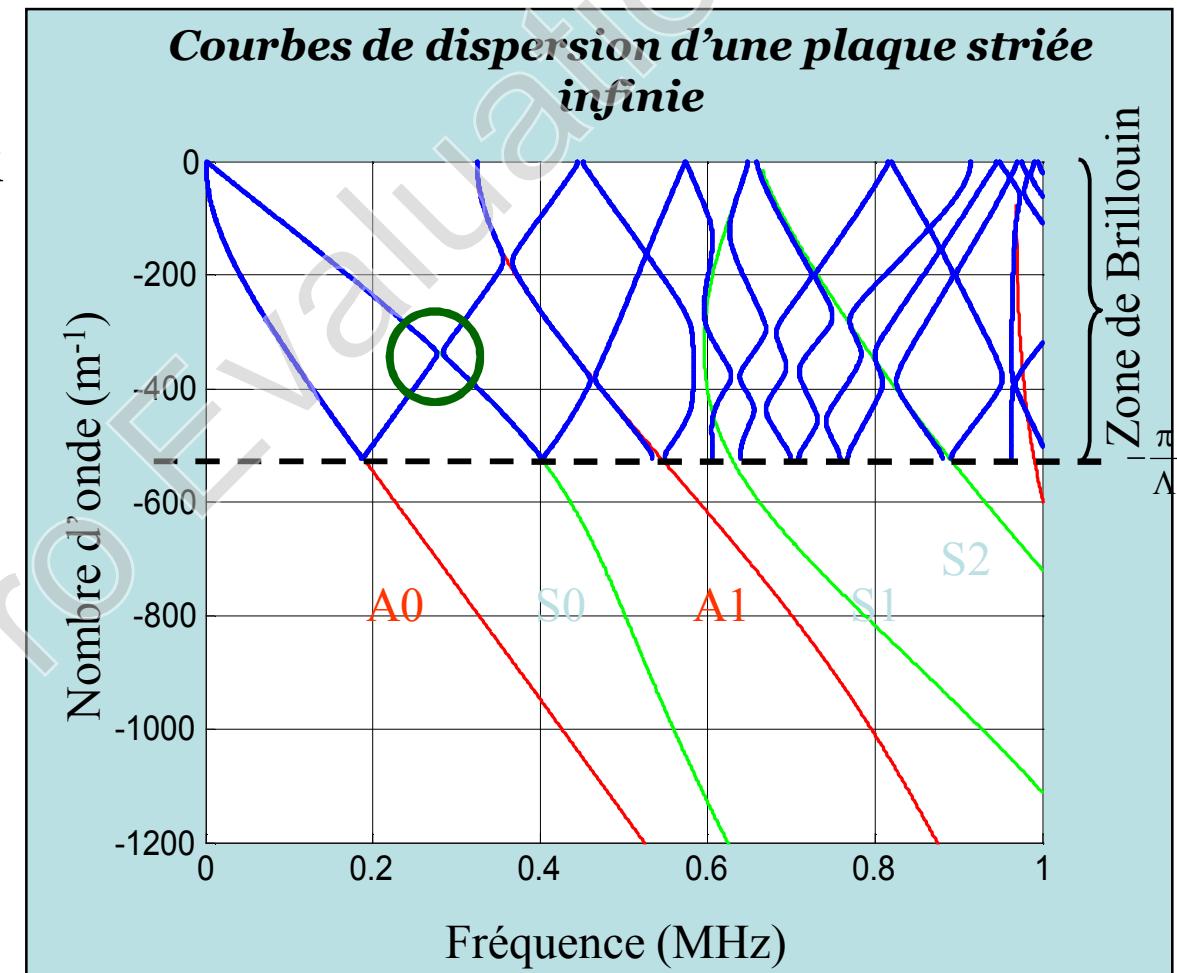
## Lamb waves with opposite $V_g$ and $V_\phi$

### Plaque avec réseau de surface

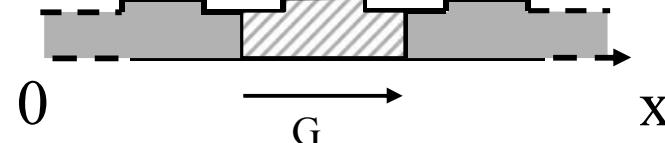


**Epaisseur de la plaque**  
 $E=5\text{mm}$

**Profondeur des stries**  
 $p=200\mu\text{m}$



## Lamb waves with opposite $V_g$ and $V_\phi$

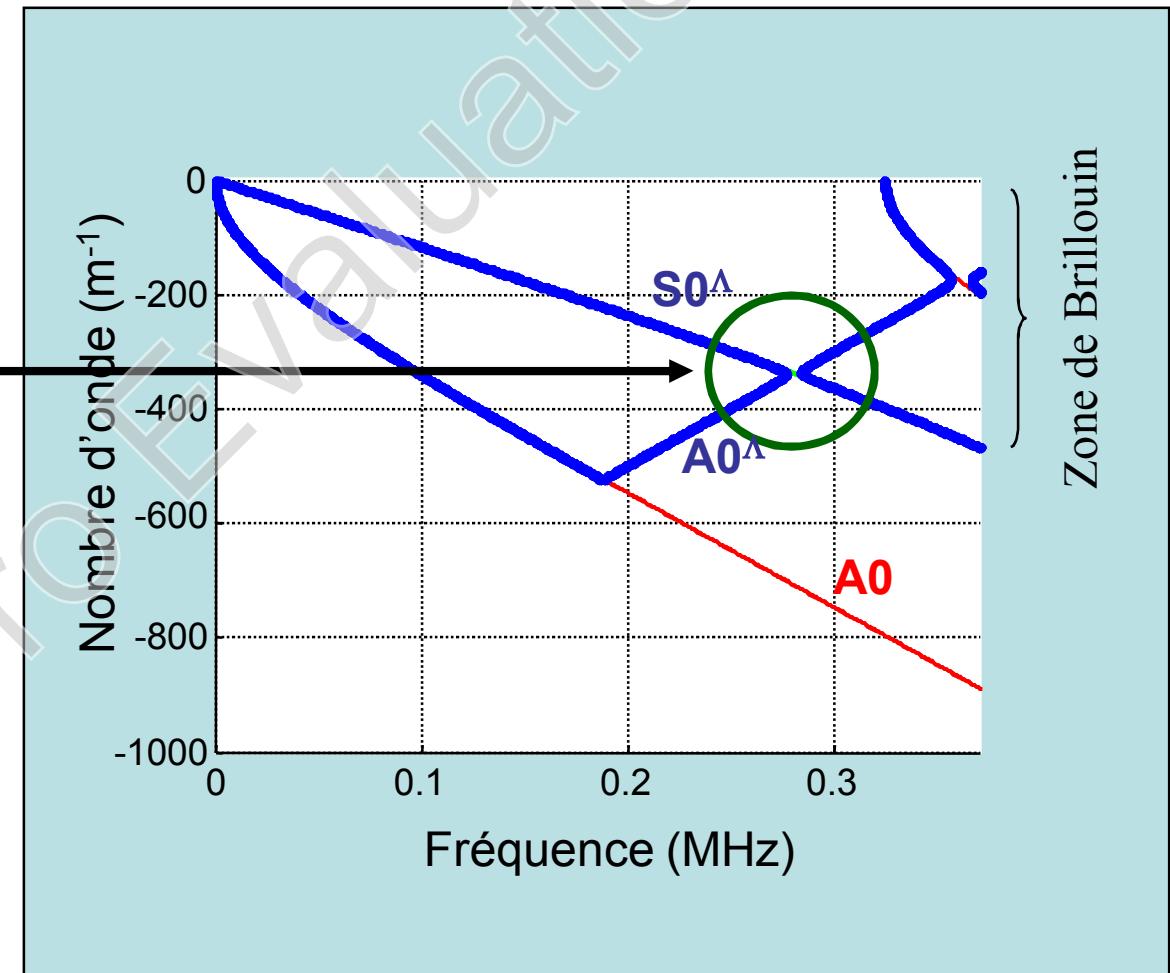


Couplage des modes  $A_0$  et  $S_0$

$$-k_{A_0} = k_{S_0} - \mathbf{G}$$

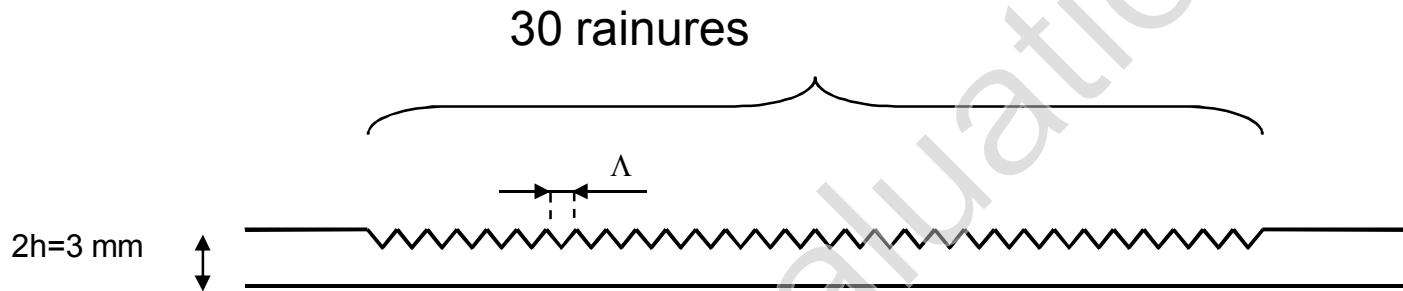
Avec  $\mathbf{G}$  vecteur de base du réseau réciproque défini par

$$\mathbf{G} = \frac{2\pi}{\Lambda} \mathbf{u}_x$$

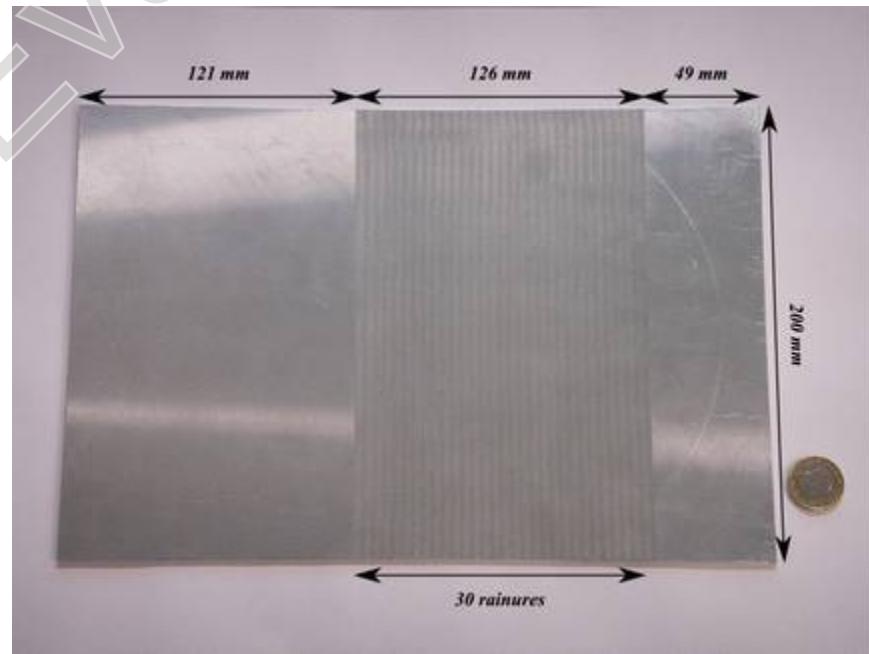


## Lamb waves with opposite $V_g$ and $V_\phi$

- Sample presentation

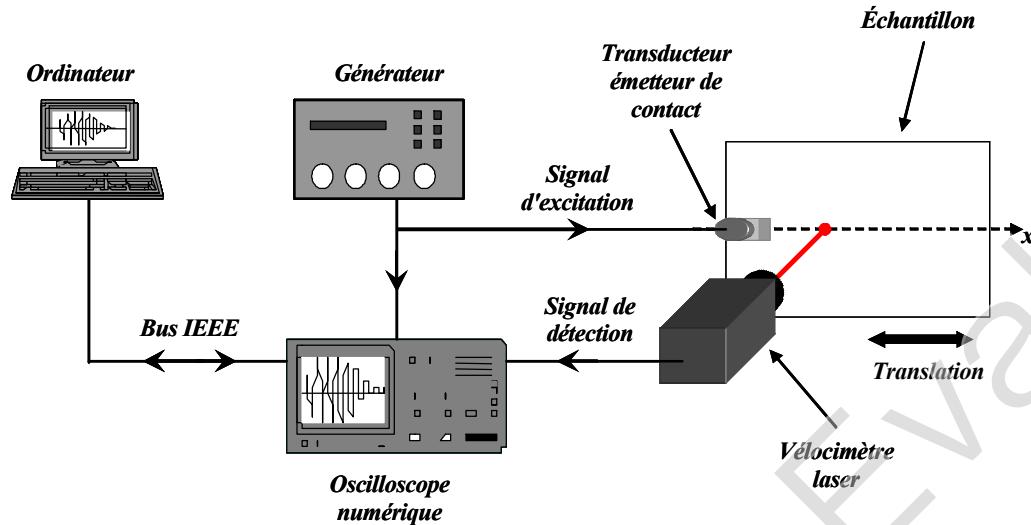


*Plaque d'aluminium  
+ réseau de stries triangulaires  
Profondeur = 120 µm  
Période spatiale  $\Lambda$  = 4.2 mm*

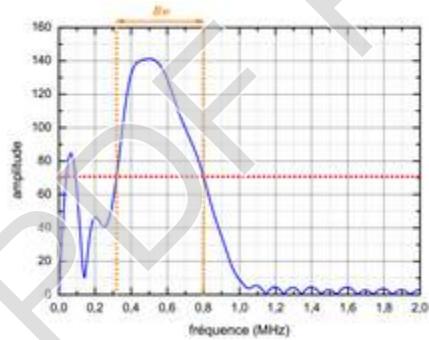


# Lamb waves with opposite $V_g$ and $V_\phi$

## Expérimental set up



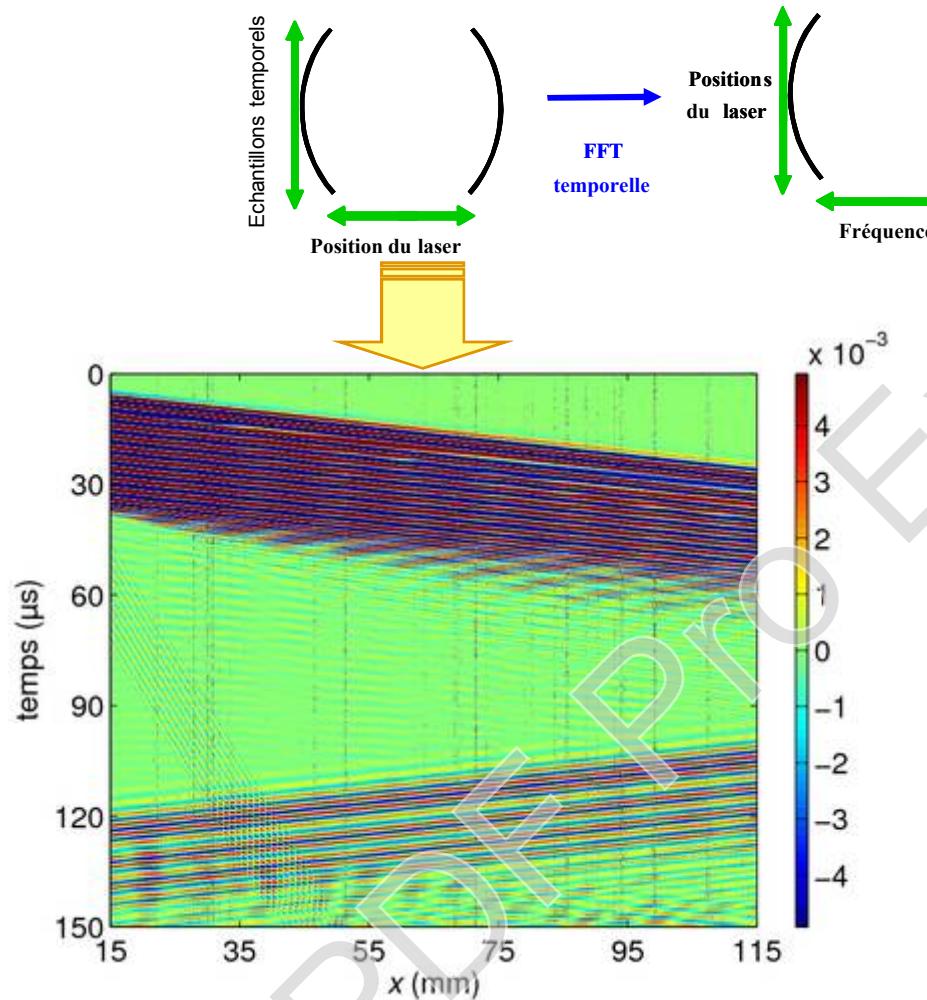
Émission : Transducteur Panametrics ( $f=500\text{kHz}$ )  
Réception : Laser POLYTEC® OFV-505 + decodeur  
VD09 calibre 20 mm/s/V (fréquence max 1MHz)



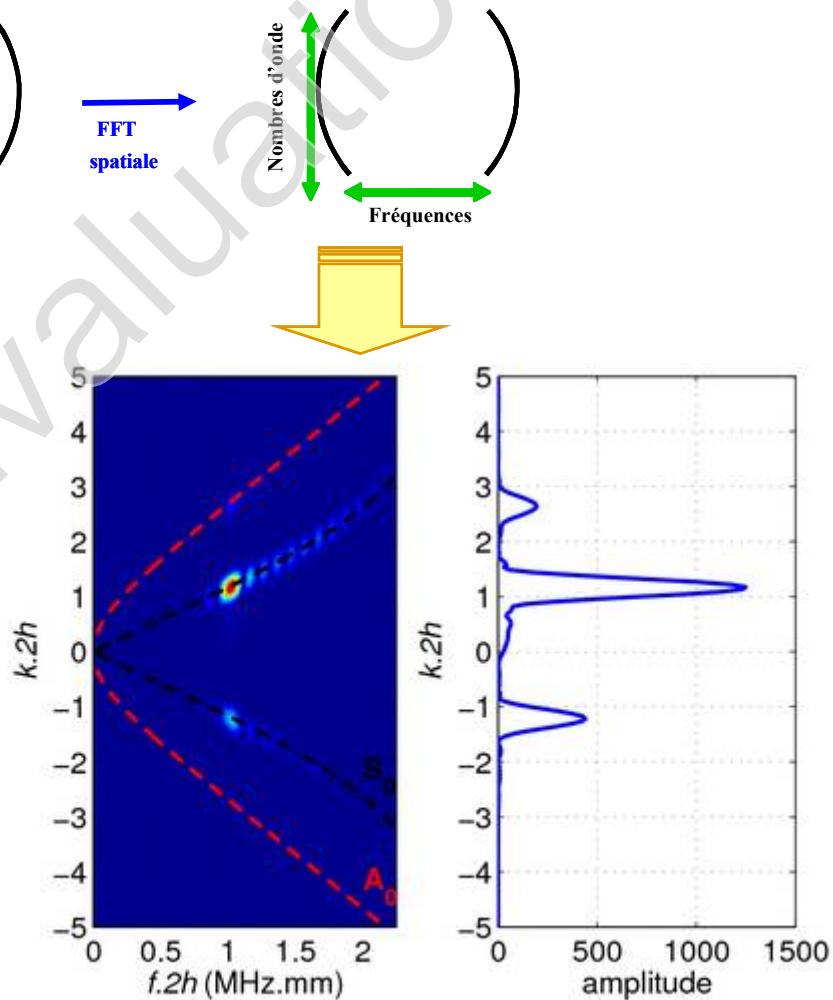
# Lamb waves with opposite $V_g$ and $V_\phi$

- Plate without corrugation

Espace temps/position



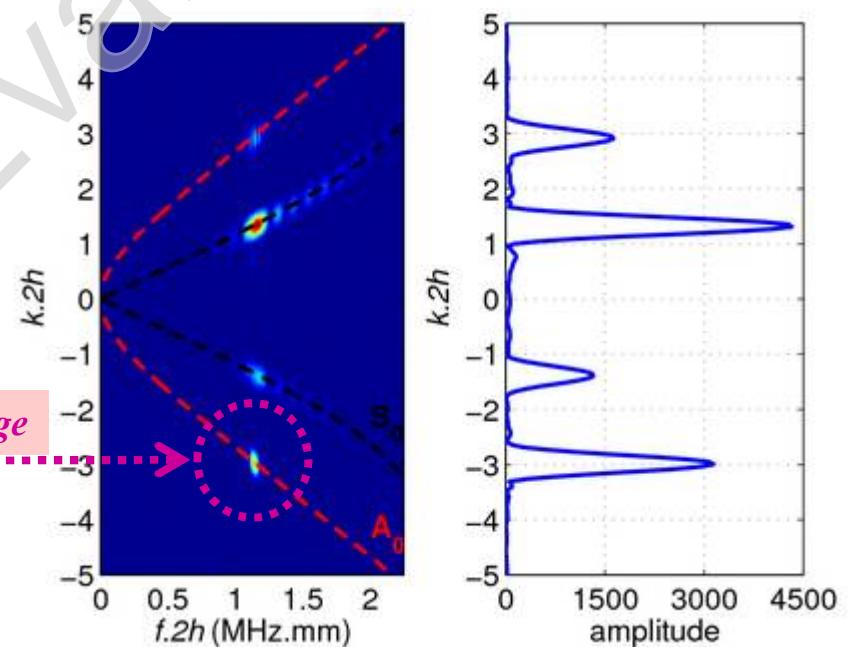
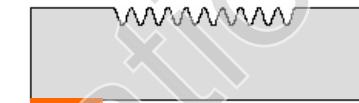
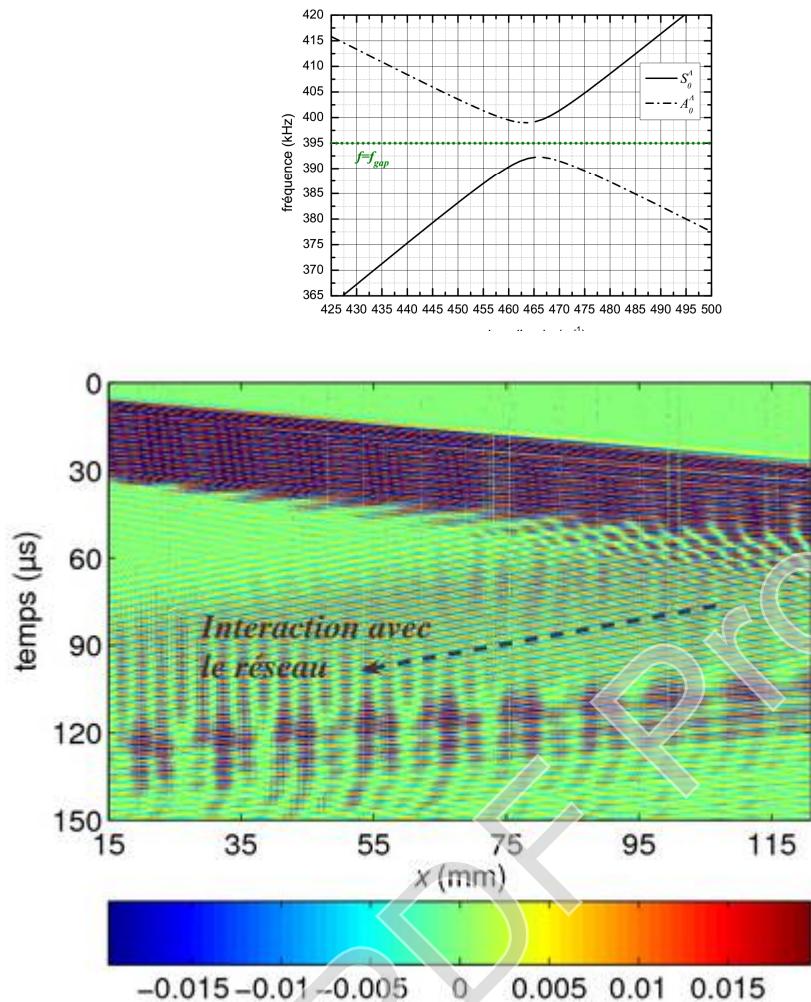
Espace fréquence/nombre d'onde



## Lamb waves with opposite $V_g$ and $V_\phi$

- Plate with corrugation

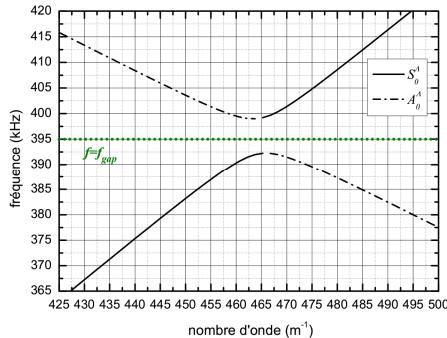
- Plaque striée : Propagation avant le réseau à  $f \approx f_{gap}$



# Lamb waves with opposite $V_g$ and $V_\phi$

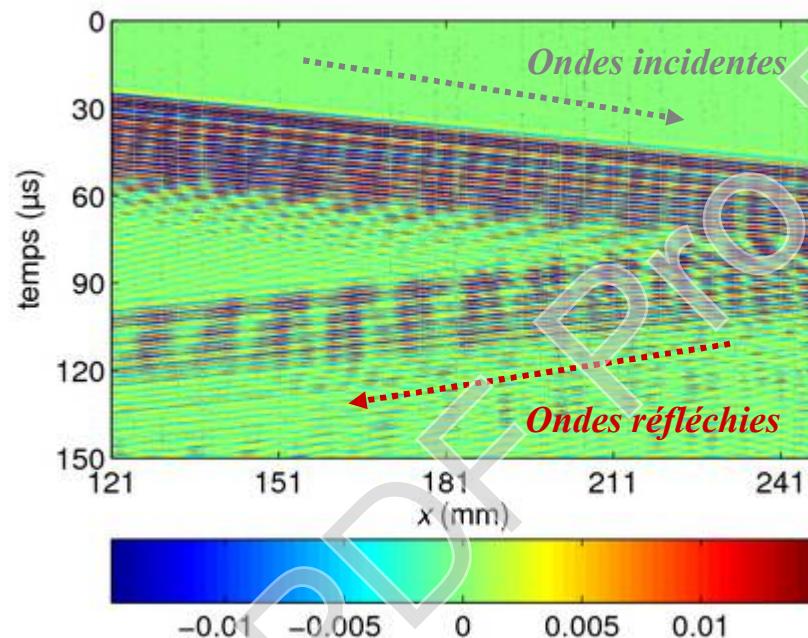
- Plate with corrugation

- Plaque striée : Propagation sous le réseau à  $f < f_{gap}$

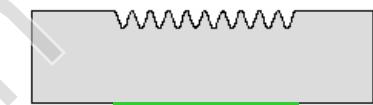
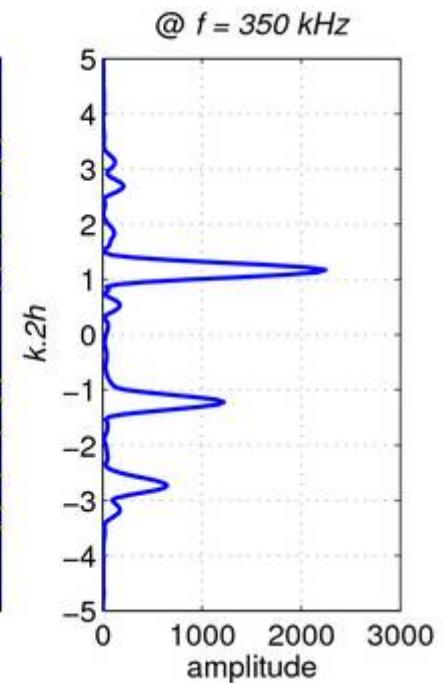
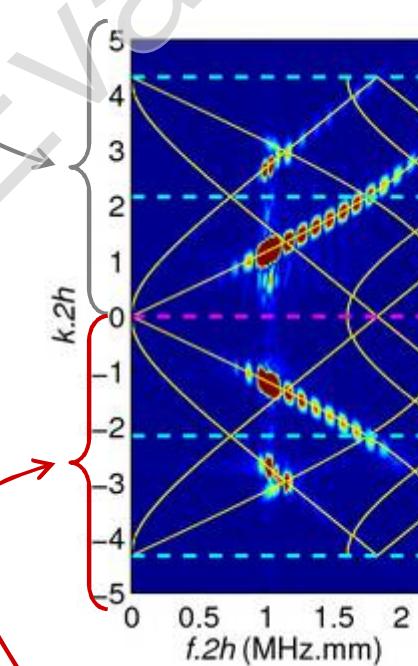


## Identification de pseudo-modes de Lamb

Ondes incidentes



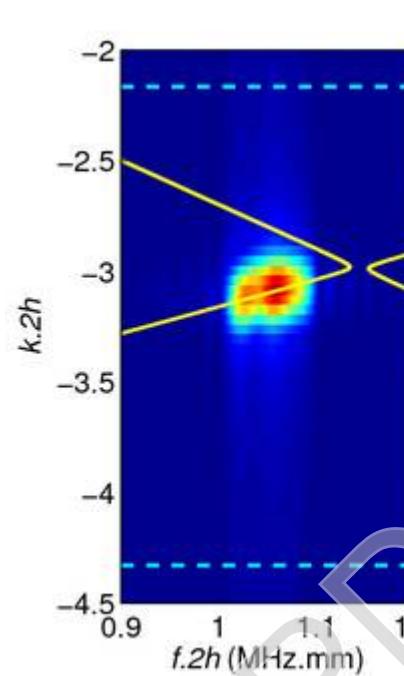
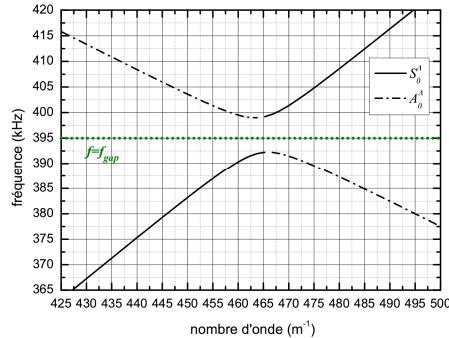
Ondes réfléchies



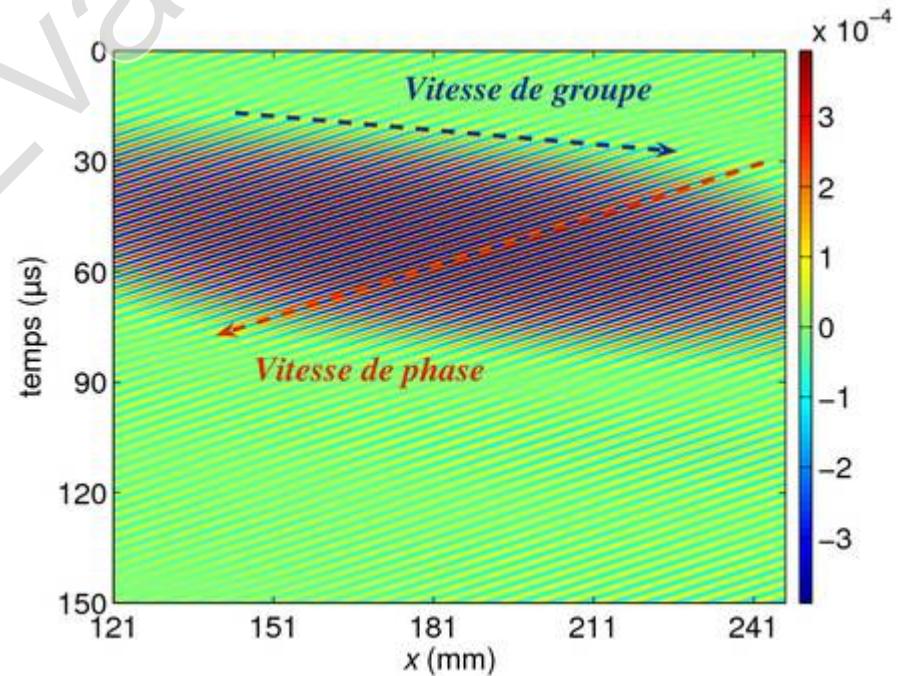
## Lamb waves with opposite $V_g$ and $V_\phi$

- Plate with corrugation

- Plaque striée : Propagation sous le réseau à  $f < f_{gap}$



*Identification de pseudo-modes de Lamb*



PDF Pro Evaluation